



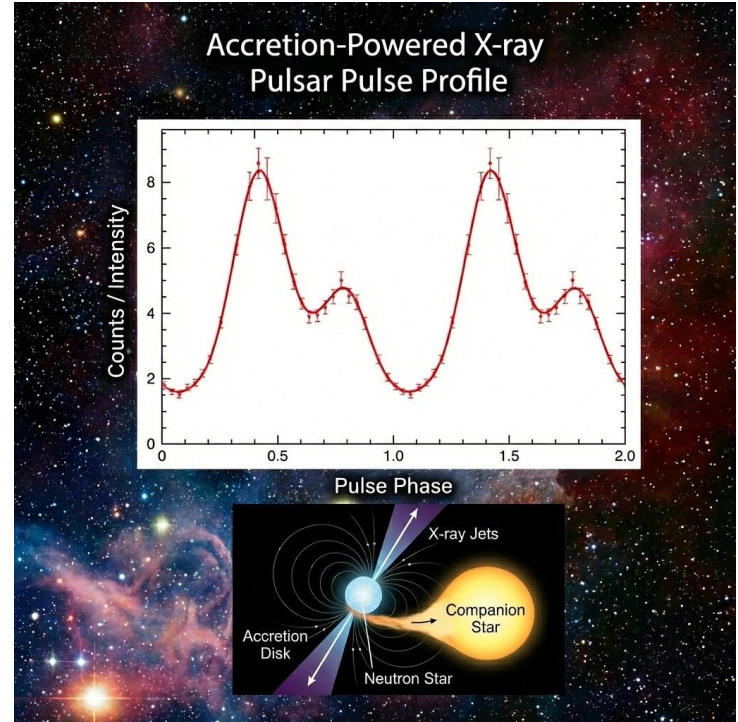
# Mapping the Pulsar Environment with Pulsed Fraction Spectroscopy

*Antonino D'Ai (IASF Palermo)*

*D. K. Maniadakis, E. Ambrosi, G. Cusumano, C. Ferrigno (Uni Genève), E. Sokolova-Lapa, P. Kretchmar, F. Furst and many others*

# Talk Outline: what pulse profiles tell us

- > Research objectives and methods
- > Energy-resolved pulse profiles as spectroscopic diagnostic tool
- > Application of these methods to a sample of **HMXB**
- > Future directions



# Methodology

# Pulse profiles have been widely studied ...

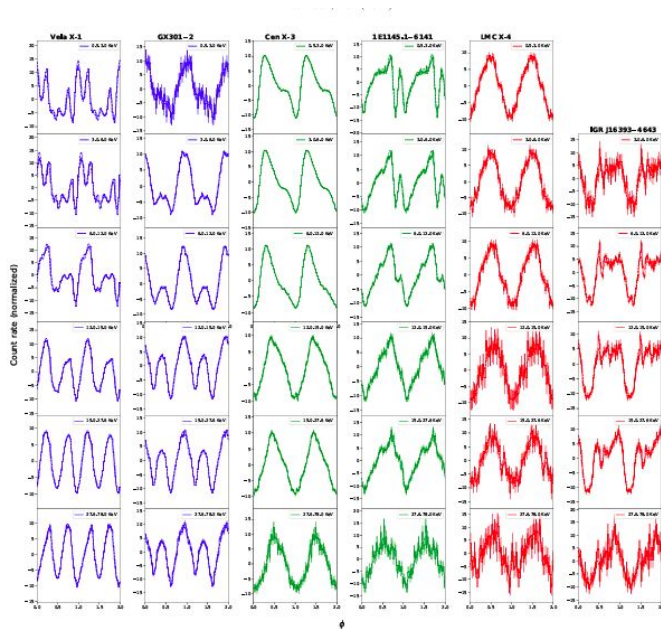


Fig. 3. Comparison of the normalized pulse profiles of different sources of the sample studied at different energy ranges. The sources are in order from left to right: Vela X-1 (type 2), GX 301 - 2 (type 2), Cen X-3 (type 1), 1E1145.1-6141 (type 1), LMC X-4 (type 0), and IGR J16393-4643 (type 0). The measured profiles are represented by solid lines, whereas the Fourier fits are represented by dashed lines. The boundaries of the energy ranges are [0.5, 3, 6, 12, 15, 27.6, and 78] keV. The pulse profiles were phase shifted by hand to align the maximums of the pulse profiles of two observations (in cases with observations of both telescopes) and coloured according to their respective pulse profile types in order to better show a comparison between them.

# Pulse profiles have been widely studied

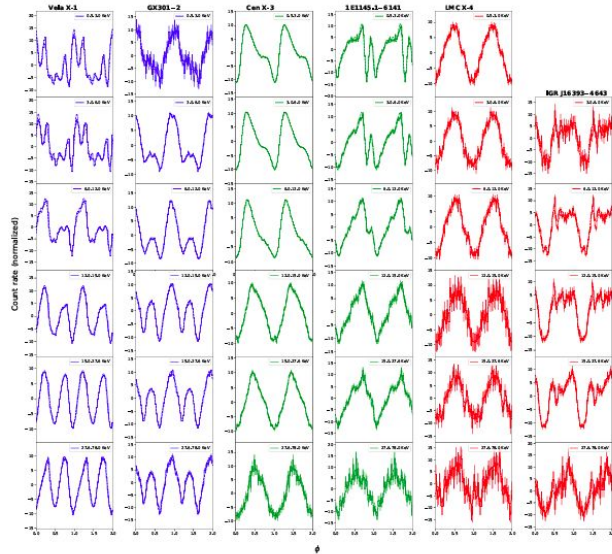
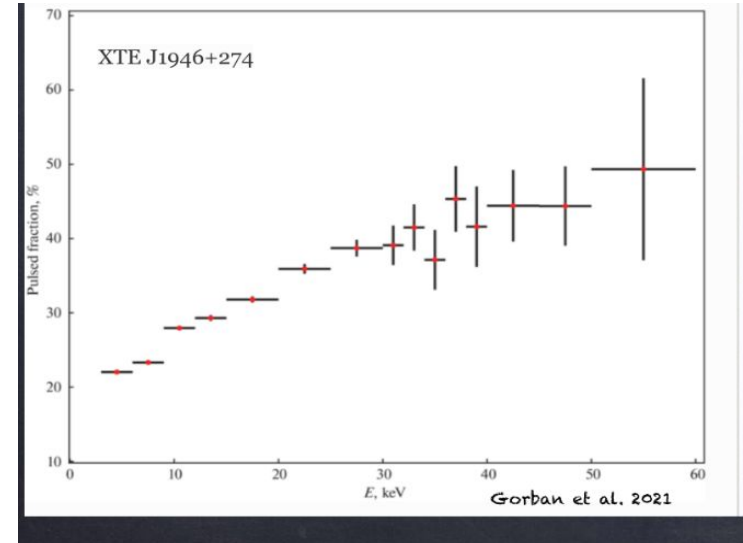
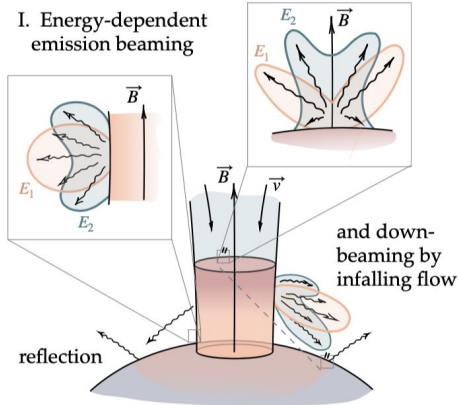


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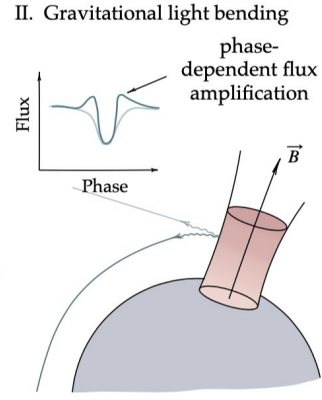
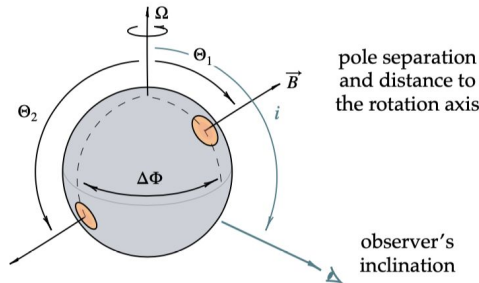
## Energy dependence of the pulsed fraction



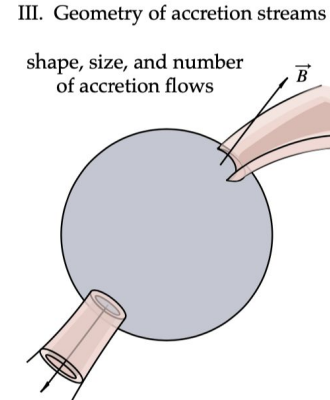
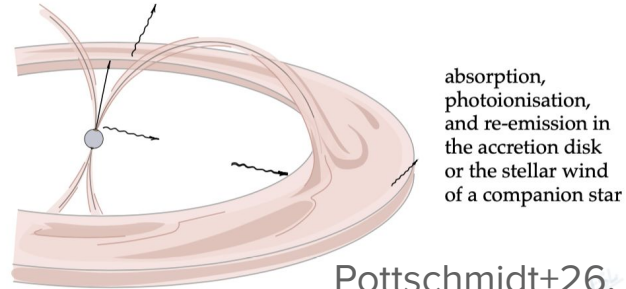
# The close and distant pulsar environments



IV. Location of the poles and the viewing angle



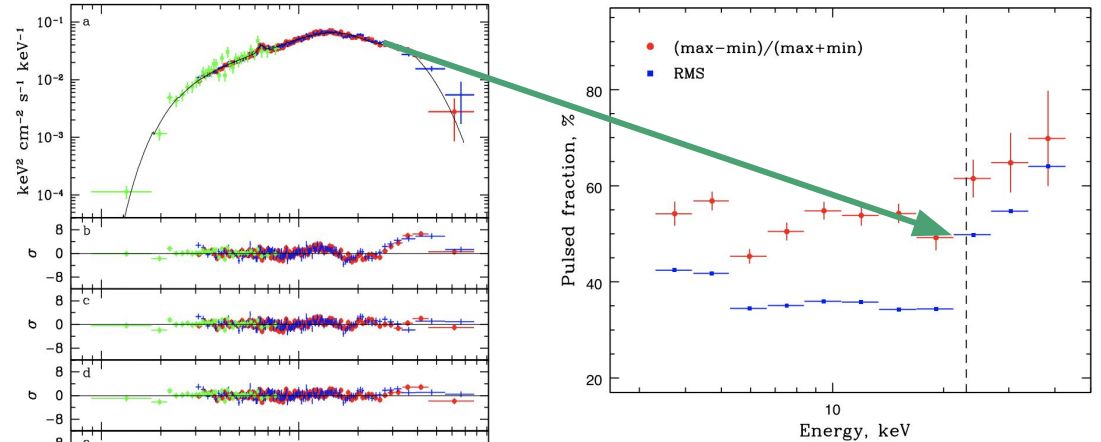
V. Reprocessing in a circumstellar environment



# Cyclotron resonant scattering features in the energy spectra of accreting X-ray pulsars

The absorption cyclotron line in AXP is caused by resonant absorption and scattering of photons between Landau levels.

Abrupt changes in the pulsed fraction at the fundamental cyclotron energy have been previously reported in several sources.



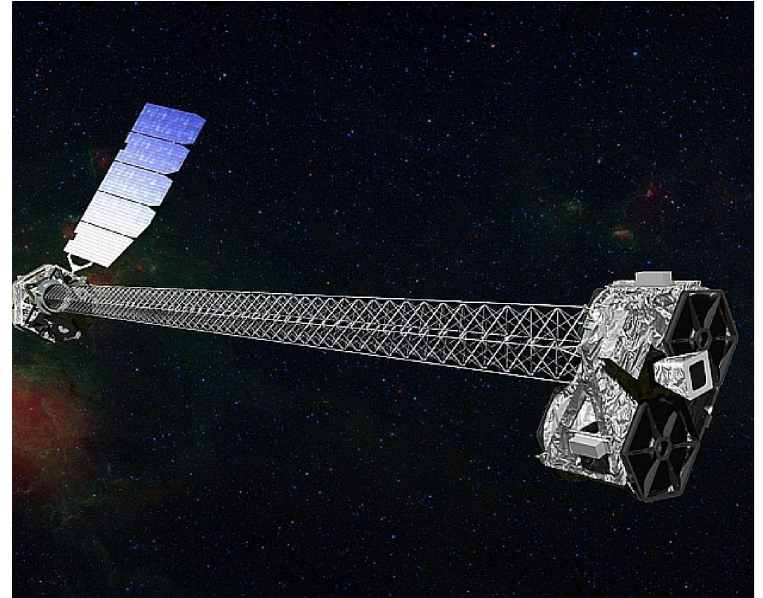
**Figure 5.** Dependence of the pulsed fraction of IGR J18027–2016 on energy calculated in two different ways (see the text for details). The dashed line shows the position of the cyclotron line that may be present in the source spectrum.

Lutovinov+2017

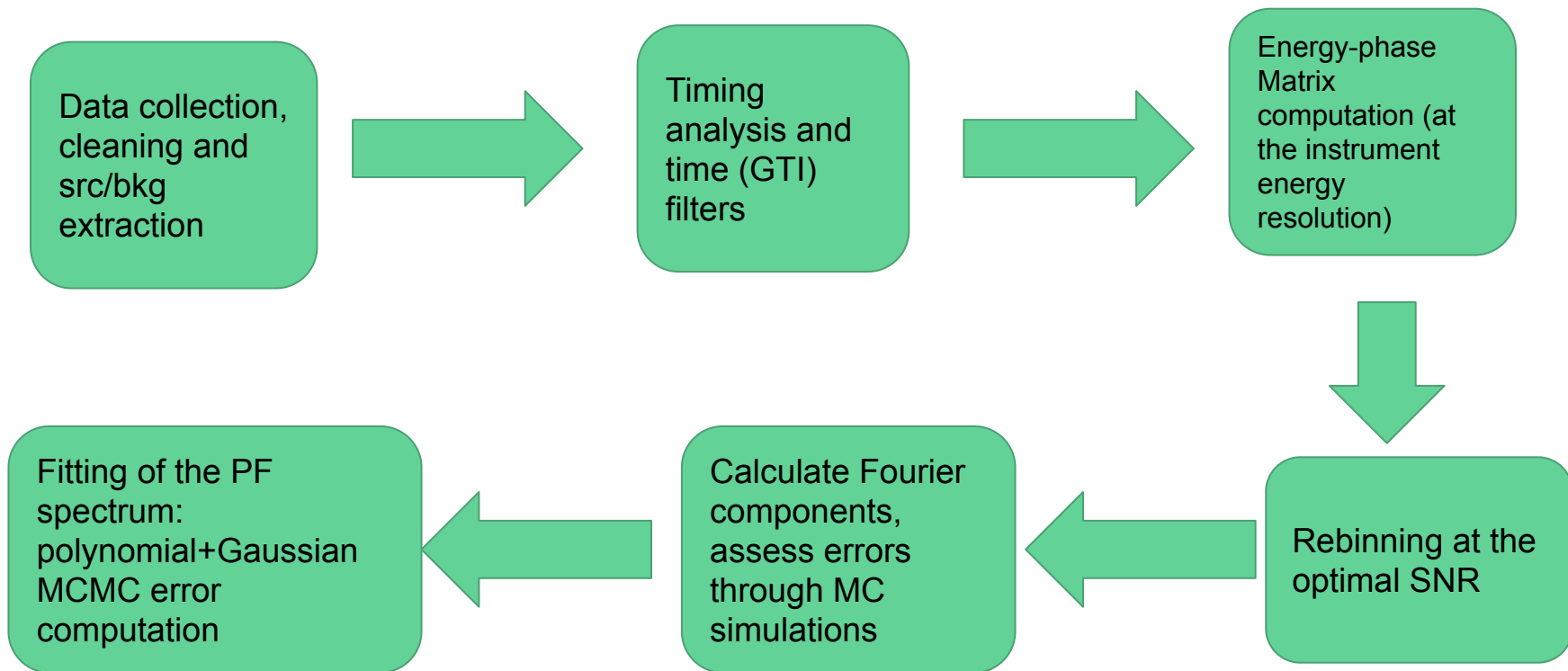
doi: 10.1093/mnras/stw3058

## Research objectives

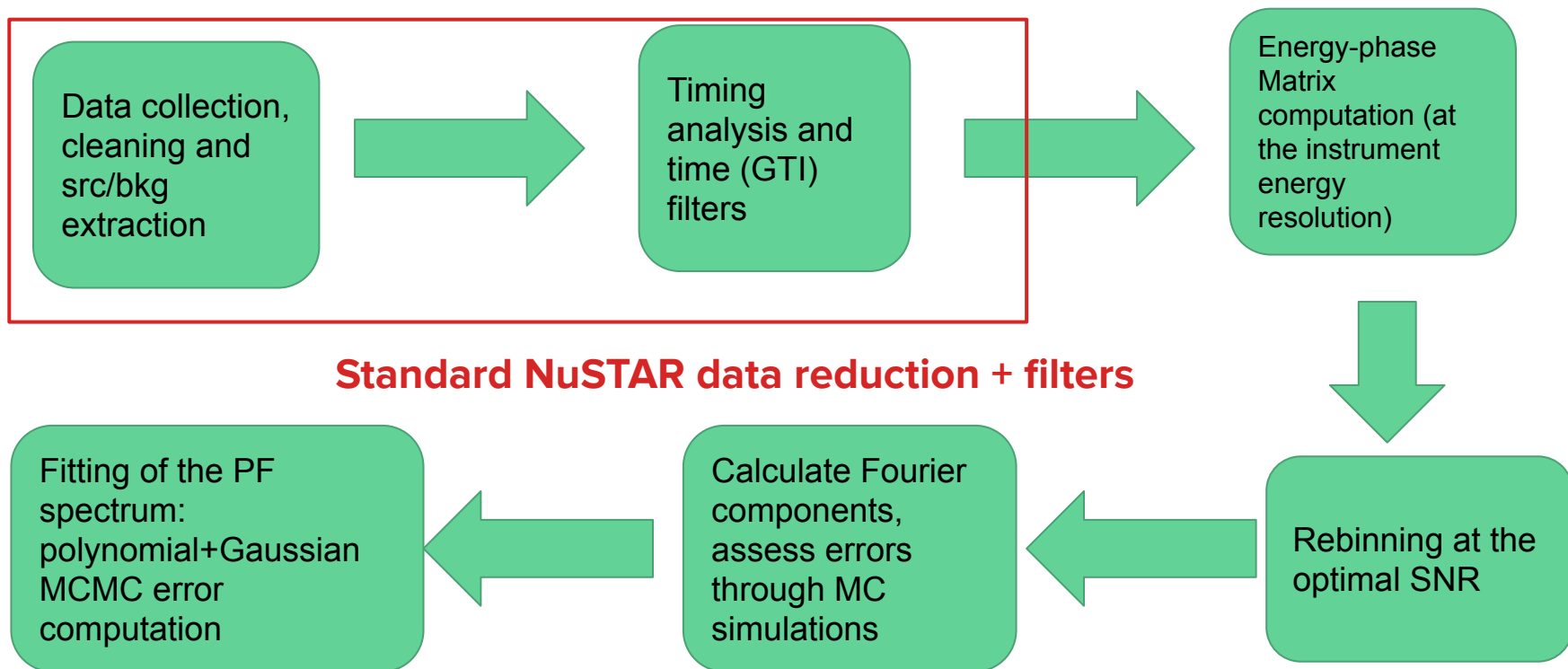
- Create a “catalogue” of energy-resolved pulse profiles based on **NuSTAR** data for all pulsars which have a clear cyclotron line detection.
- A database with uniform, easily cross-checkable, timing products.
- **Study the amplitude energy dependence in conjunction with spectroscopic results**
- Test and compare results from benchmark sources
- Exploit all the accessible parameter space from pulse profile decomposition.



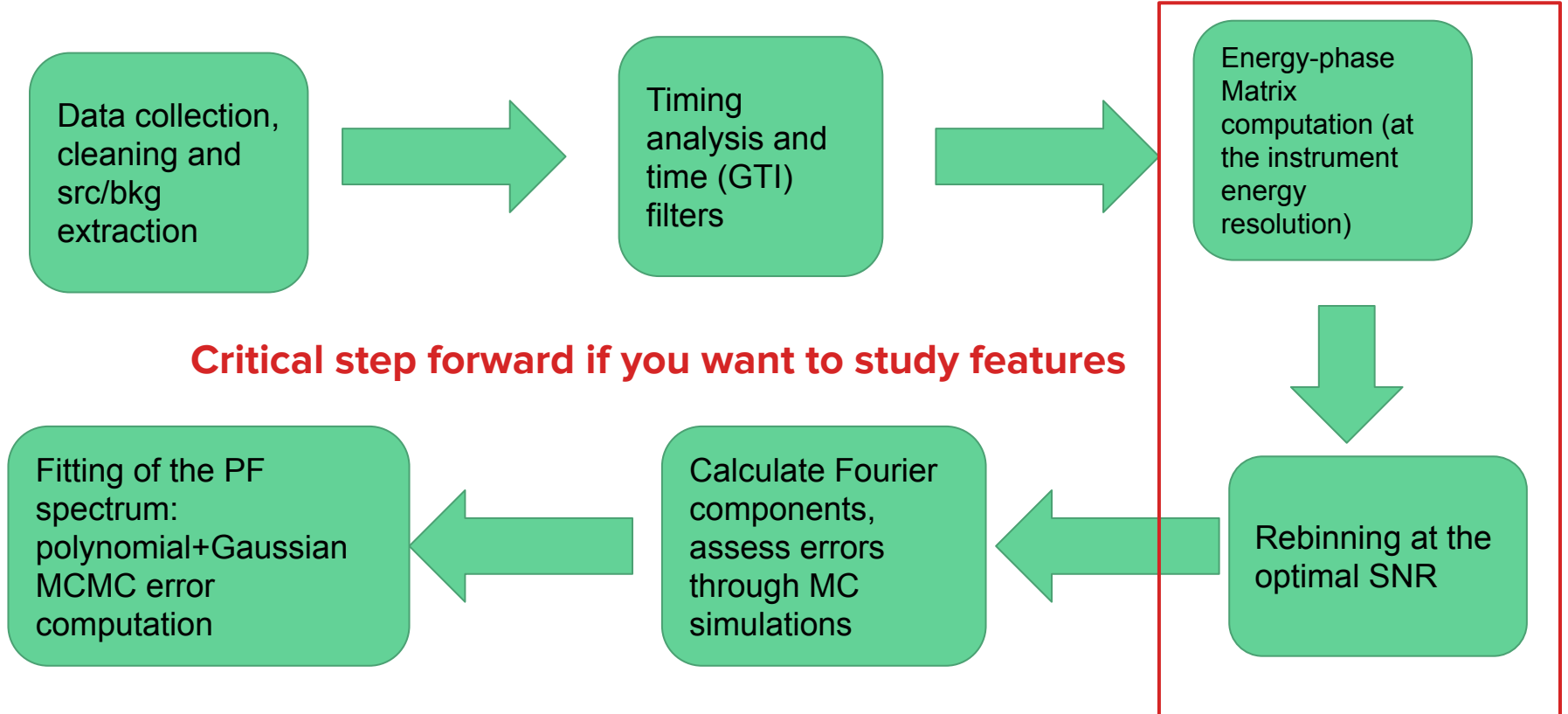
# Methods: a pipeline for automatic analysis of PP



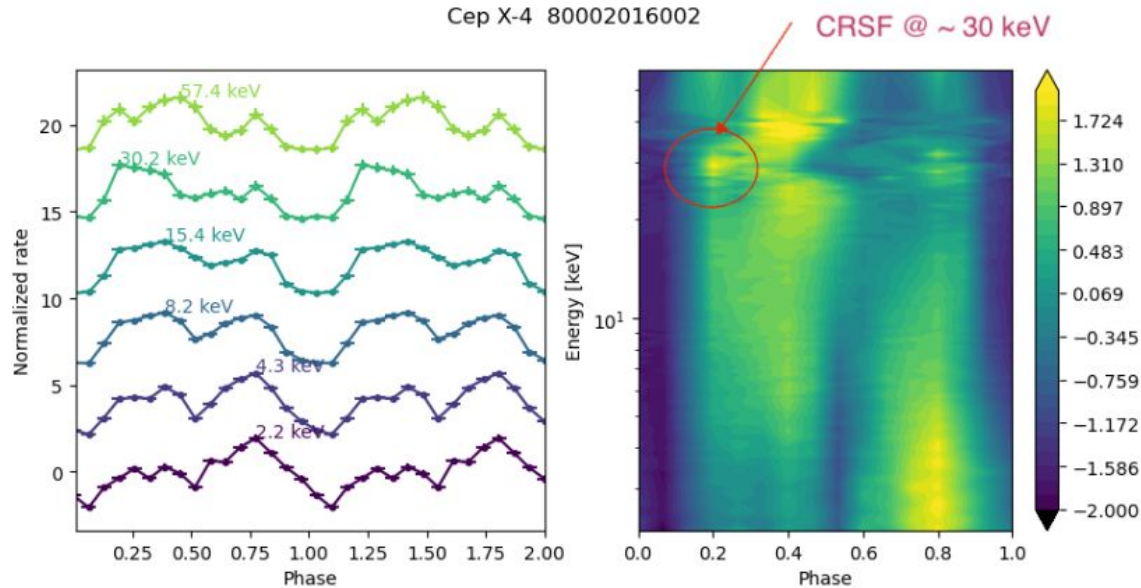
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# Methods: a pipeline for automatic analysis of PP

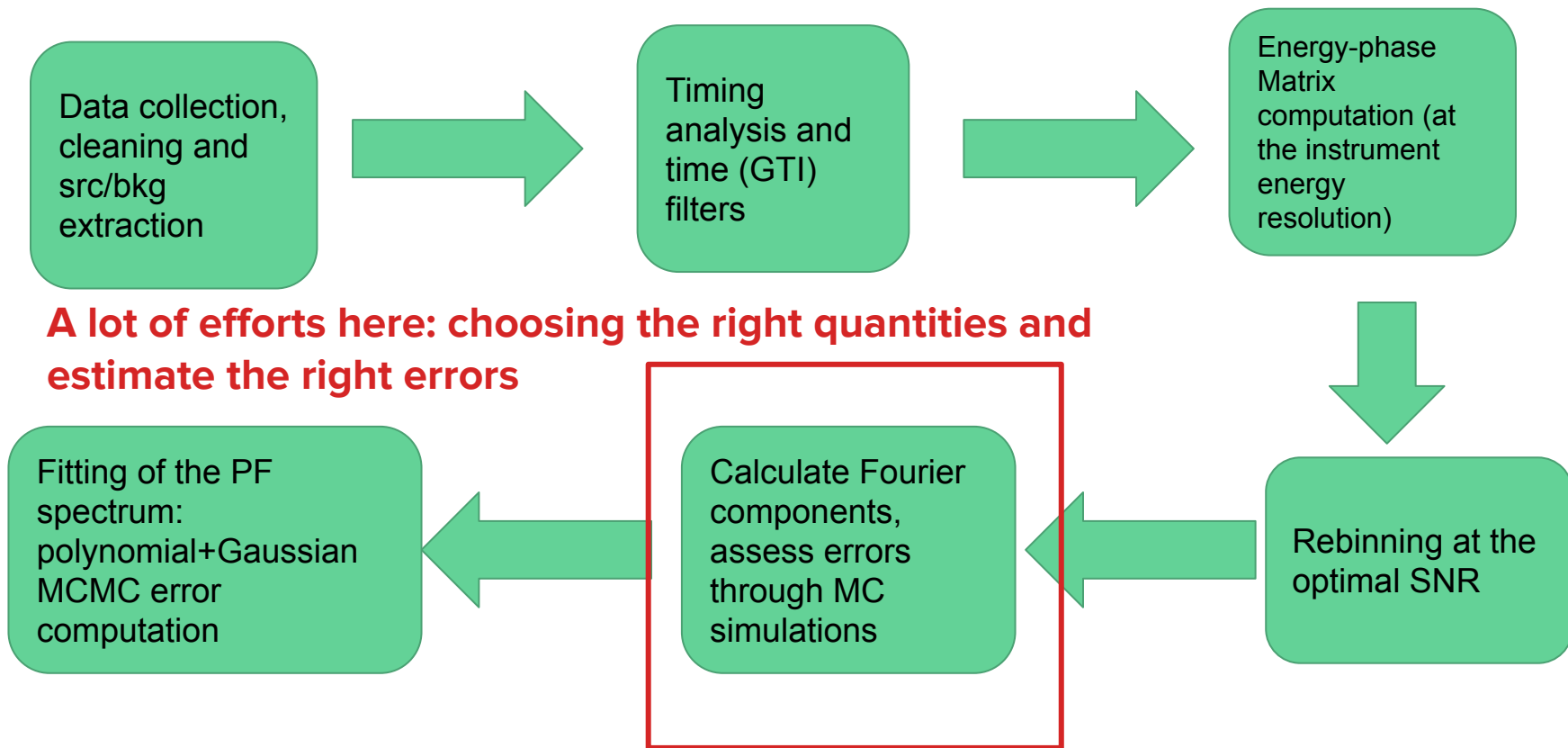


# Energy-phase matrices



**Fig. 12** Representative energy-selected pulse profiles (left, offset for visualization) of the full phase-energy map (right) for a *NuSTAR* observation of Cep X-4. The map shows a clear discontinuity in the energy range associated with the presence of a cyclotron resonance scattering feature. It also highlights the strong energy dependence of the amplitude of the peak at phase  $\sim 0.8$ . Adapted from [Ferrigno et al. \(2023\)](#).

# Methods: a pipeline for automatic analysis of PP



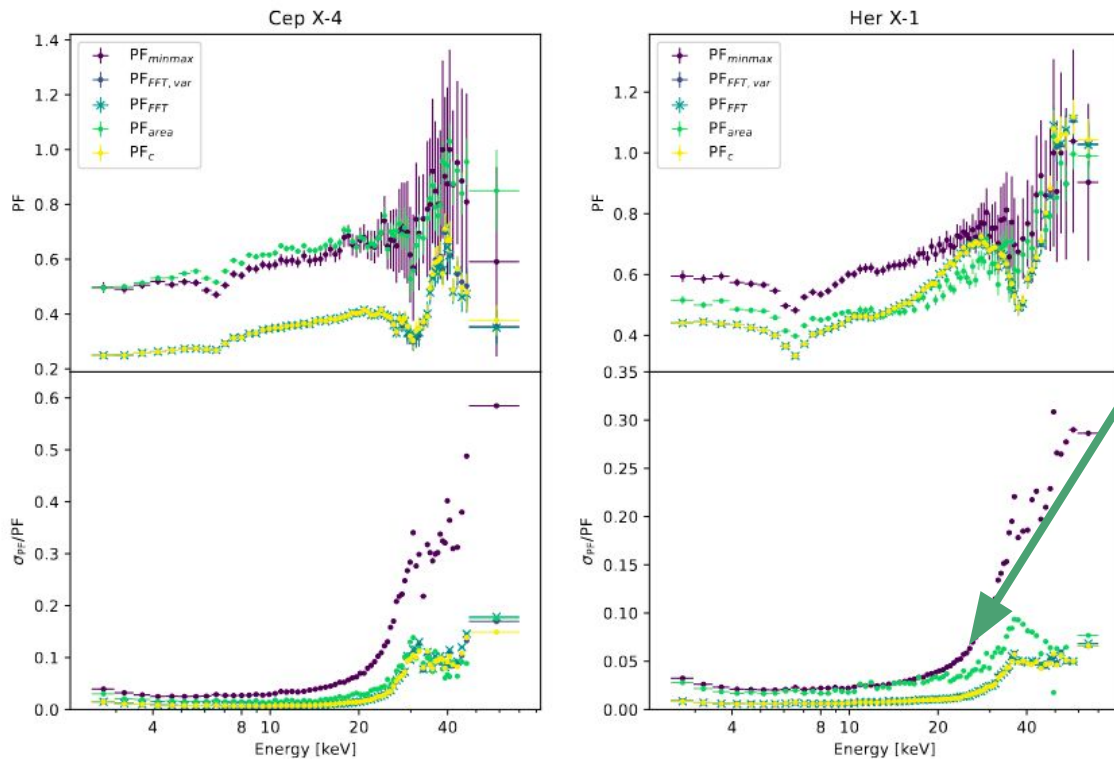
# What is meant by **pulsed fraction (PF)**?

No general consensus, but always understood as the power of the modulated signal. It can be normalised with respect to the total observed emission (that's why it is a fraction). But the “*exact numeric value*” can be known only in the limit of very high statistics. In general “the PF value” depends a lot on the method and on the user-defined binning of the pulse profile.

$$\text{PF}_{\text{area}} = \frac{1}{\sum_{j=1}^{N_{\text{bin}}} C_j} \sum_{j=1}^{N_{\text{bin}}} (C_j - C_{\text{min}}), \quad \text{PF}_{\text{minmax}} = \frac{C_{\text{max}} - C_{\text{min}}}{C_{\text{max}} + C_{\text{min}}}, \quad \text{PF}_{\text{fit}} = \frac{\int_0^1 (f(\phi) - C_{\text{min}}) d\phi}{\int_0^1 f(\phi) d\phi}.$$

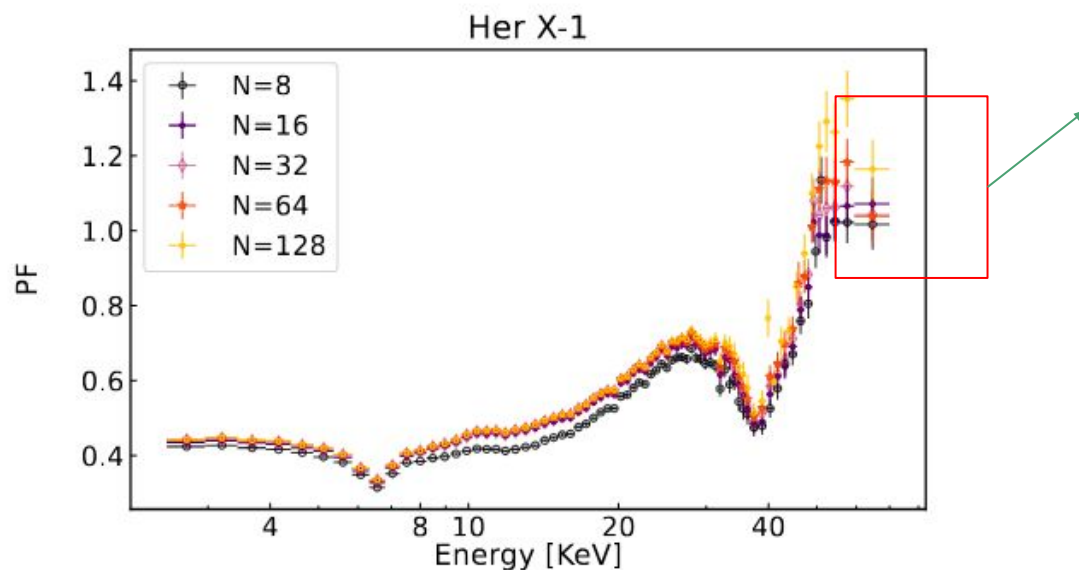
$$\text{PF}_{\text{FFT}} = \frac{1}{a_0} \sqrt{2 \sum_{k=1}^{N_{\text{harm}}} [(a_k^2 + b_k^2) - (\sigma_{a_k}^2 + \sigma_{b_k}^2)]}, \quad \text{PF}_{\text{RMS}} = \frac{1}{C_{\text{avg}}} \sqrt{\frac{\sum_{j=1}^{N_{\text{bin}}} [(C_i - C_{\text{avg}})^2 - \sigma_{C_i}^2]}{N_{\text{bin}}}}$$

# Not all the definitions are equally effective



At low statistics some definitions result in much larger uncertainty, which comes not from data but on the definition itself.

# So the PF values are method-dependent?

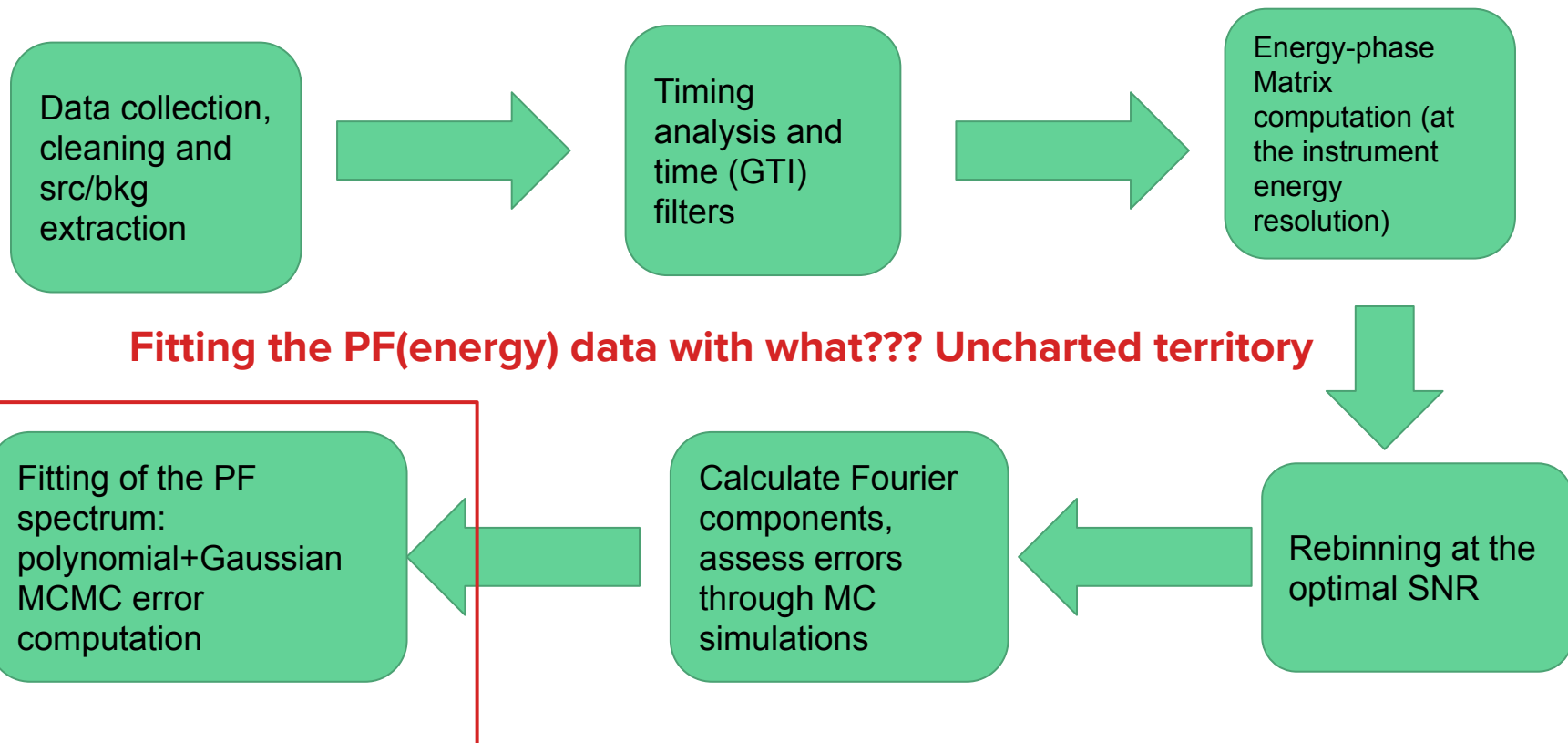


**Fig. A.3.**  $PF_{\text{FFT}}$  obtained with different  $N_{\text{bins}}$  for the pulse profile of Her X - 1 analyzed in this work.

FFT/RMS methods can slightly go even above 1. They are not really “fractions”.

But they offer the advantage to be less biased against the  $N_{\text{bins}}$  choice and to have the minimum relative uncertainty.

# Methods: a pipeline for automatic analysis of PP



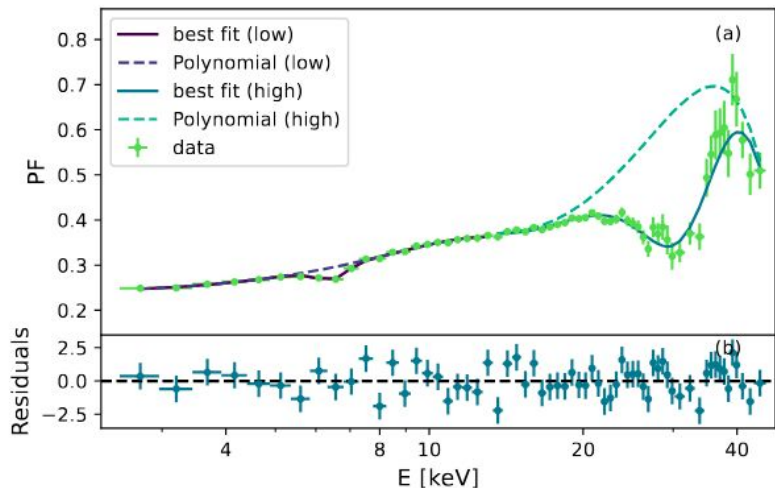
# Giving quantitative estimates

The key objective in decomposing the PPs was to pass from qualitative descriptions to quantitative estimates. To give numbers and errors associated with. Treat the PF values vs energy as it were a “**energy spectrum**”. We called it the **Pulsed Fraction Spectrum (PFS)**

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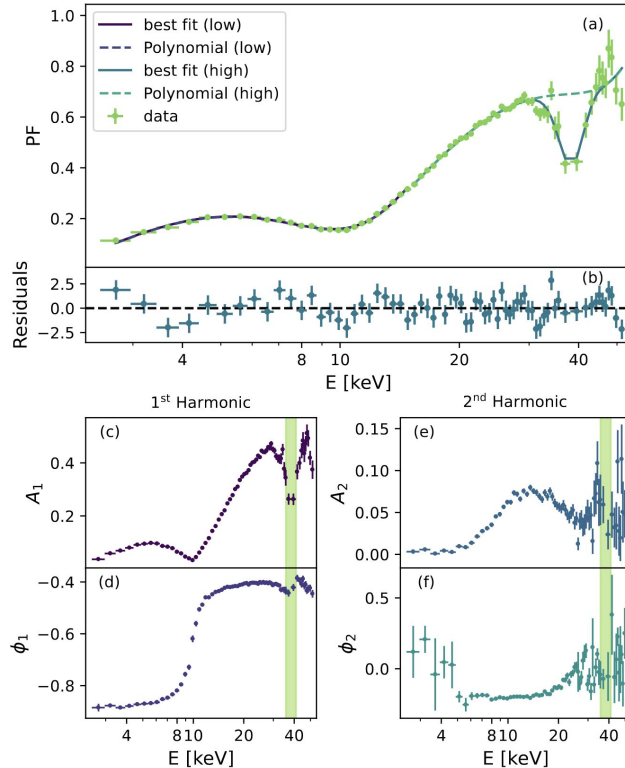
Treat the PF values vs energy as it were a “**energy spectrum**”. We called it the **Pulsed Fraction Spectrum (PFS)**



Phenomenological approach:

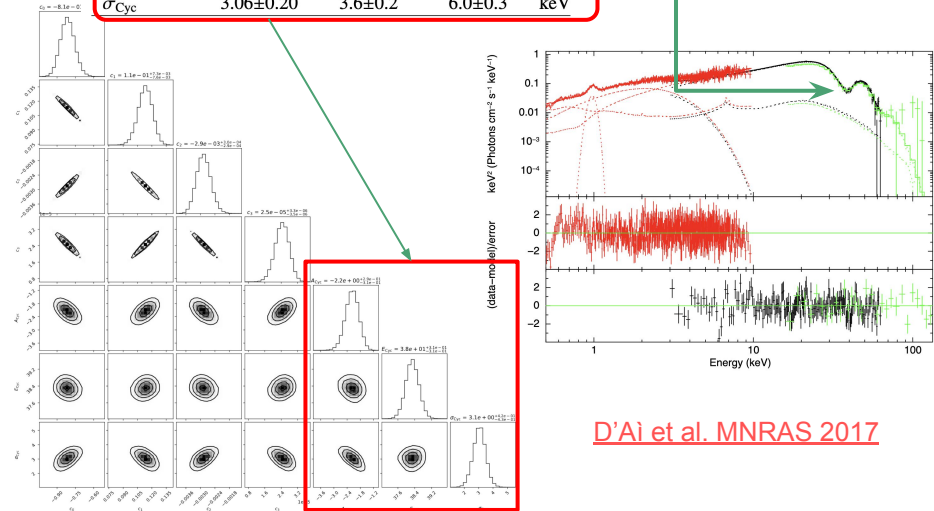
- use polynomials for the continuum (raise the polynomial degree until the description is ok)
- use Gaussians for the features
- split the energy range to avoid too high n-polynomials
- use MCMC for error estimates

# Pulsed fraction as a spectroscopic diagnostic tool



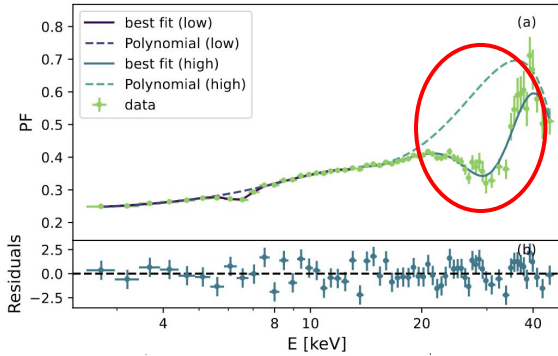
**Table 2.** Best-fit parameters of the 4U 1626-67 ObsID 30101029002 pulse and amplitude models compared to spectral results. The last column values from the spectral best-fit of the same data set (see Model BWM3 of Table 1 in D’Ai et al. 2017).

|  | PF               | 1 <sup>st</sup>      | Spectral             |
|--|------------------|----------------------|----------------------|
| $\chi^2_{\text{red,lo}}/\text{d.o.f.}$ | 1.1/17           | 1.6/13               | —                    |
| $\chi^2_{\text{red,hi}}/\text{d.o.f.}$ | 1.4/40           | 1.1/40               | —                    |
| $n_{\text{pol}}^{(\text{lo})}$         | 4                | 6                    | —                    |
| $n_{\text{pol}}^{(\text{hi})}$         | 3                | 5                    | —                    |
| $E_{\text{split}}^{\pm}$               | 13.21            | 12.33                | — keV                |
| $A_{\text{Cyc}}^{\pm}$                 | $-2.16 \pm 0.14$ | $-2.2^{+0.2}_{-0.3}$ | $23.0 \pm 0.9$       |
| $E_{\text{Cyc}}^{\pm}$                 | $38.29 \pm 0.15$ | $39.07 \pm 0.19$     | $37.90 \pm 0.15$ keV |
| $\sigma_{\text{Cyc}}^{\pm}$            | $3.06 \pm 0.20$  | $3.6 \pm 0.2$        | $6.0 \pm 0.3$ keV    |



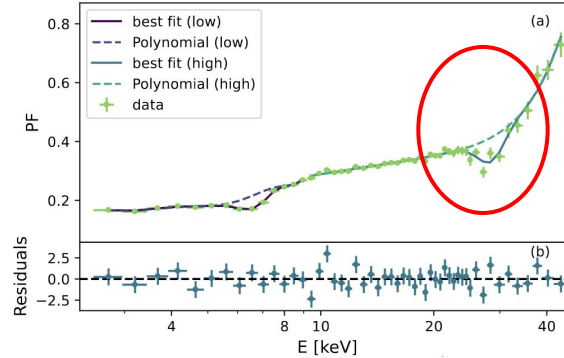
# Other examples from [Ferrigno, D'Ai, Ambrosi \(A&A 2023\)](#)

## Cep X-4



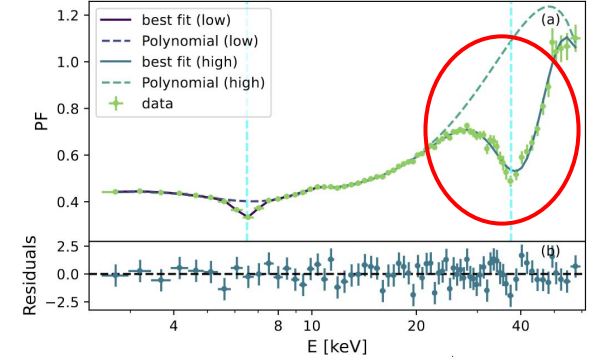
|  | PF                   | 1 <sup>st</sup>             | Spectral                         |     |
|--|----------------------|-----------------------------|----------------------------------|-----|
| $\chi^2_{\text{red,lo}}/\text{d.o.f.}$ | 1.4/15               | 0.8/8                       | —                                |     |
| $\chi^2_{\text{red,hi}}/\text{d.o.f.}$ | 1.5/35               | 1.3/39                      | —                                |     |
| $n_{\text{lo}}$                        | 3                    | 6                           | —                                |     |
| $n_{\text{hi}}$                        | 3                    | 3                           | —                                |     |
| $E_{\text{split}}$                     | 13.35                | 11.18                       | —                                | keV |
| $A_{\text{Fe}}$                        | $-0.0308 \pm 0.0019$ | $(-8 \pm 2) \times 10^{-3}$ | $(1.39 \pm 0.16) \times 10^{-3}$ |     |
| $E_{\text{Fe}}$                        | $6.444 \pm 0.019$    | $6.62 \pm 0.04$             | $6.47 \pm 0.03$                  | keV |
| $\sigma_{\text{Fe}}$                   | $0.46 \pm 0.02$      | $0.33 \pm 0.05$             | $0.42 \pm 0.05$                  | keV |
| $A_{\text{Cyc}}$                       | $-4.1 \pm 0.7$       | $-2.08 \pm 0.12$            | $20^{\pm 5}$                     |     |
| $E_{\text{Cyc}}$                       | $31.00 \pm 0.18$     | $30.32 \pm 0.10$            | $30.39^{\pm 0.17}_{-0.14}$       | keV |
| $\sigma_{\text{Cyc}}$                  | $5.3 \pm 0.3$        | $3.75 \pm 0.12$             | $5.8 \pm 0.4$                    | keV |

## Cen X-3

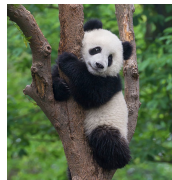


|  | PF                      | 1 <sup>st</sup>        | 2 <sup>nd</sup>      | Spectral                  |     |
|--|-------------------------|------------------------|----------------------|---------------------------|-----|
| $\chi^2_{\text{red,lo}}/\text{d.o.f.}$ | 1.6/4                   | 2.0/8                  | 0.8/17               | —                         |     |
| $\chi^2_{\text{red,hi}}/\text{d.o.f.}$ | 1.3/31                  | 2.1/27                 | 1.1/24               | —                         |     |
| $n_{\text{lo}}$                        | 3                       | 7                      | 1                    | —                         |     |
| $n_{\text{hi}}$                        | 6                       | 2                      | 2                    | —                         |     |
| $E_{\text{split}}$                     | 9.40                    | 9.40                   | 13.78                | —                         | keV |
| $A_{\text{Fe}}$                        | $-0.09^{+0.02}_{-0.03}$ | $-0.0239 \pm 0.0018$   | $-0.0271 \pm 0.0015$ | $0.117^{+0.007}_{-0.011}$ | keV |
| $E_{\text{Fe}}$                        | $6.69 \pm 0.04$         | $6.42 \pm 0.02$        | $6.55 \pm 0.03$      | $6.67^{\pm}$              | keV |
| $\sigma_{\text{Fe}}$                   | $0.64 \pm 0.06$         | $0.47 \pm 0.03$        | $0.56 \pm 0.03$      | $0.53^{\pm} \pm 0.03$     | keV |
| $A_{\text{Cyc}}$                       | $-0.53 \pm 0.08$        | $0.04^{+0.15}_{-0.24}$ | $-1.68 \pm 0.12$     | $0.40 \pm 0.13$           |     |
| $E_{\text{Cyc}}$                       | $28.8 \pm 0.3$          | $29^{\pm 3}_{-3}$      | $28.5 \pm 0.3$       | $30.3 \pm 0.6$            | keV |
| $\sigma_{\text{Cyc}}$                  | $2.5 \pm 0.3$           | $5 \pm 1$              | $7.2 \pm 0.3$        | $5.0 \pm 0.9$             | keV |

## Her X-1

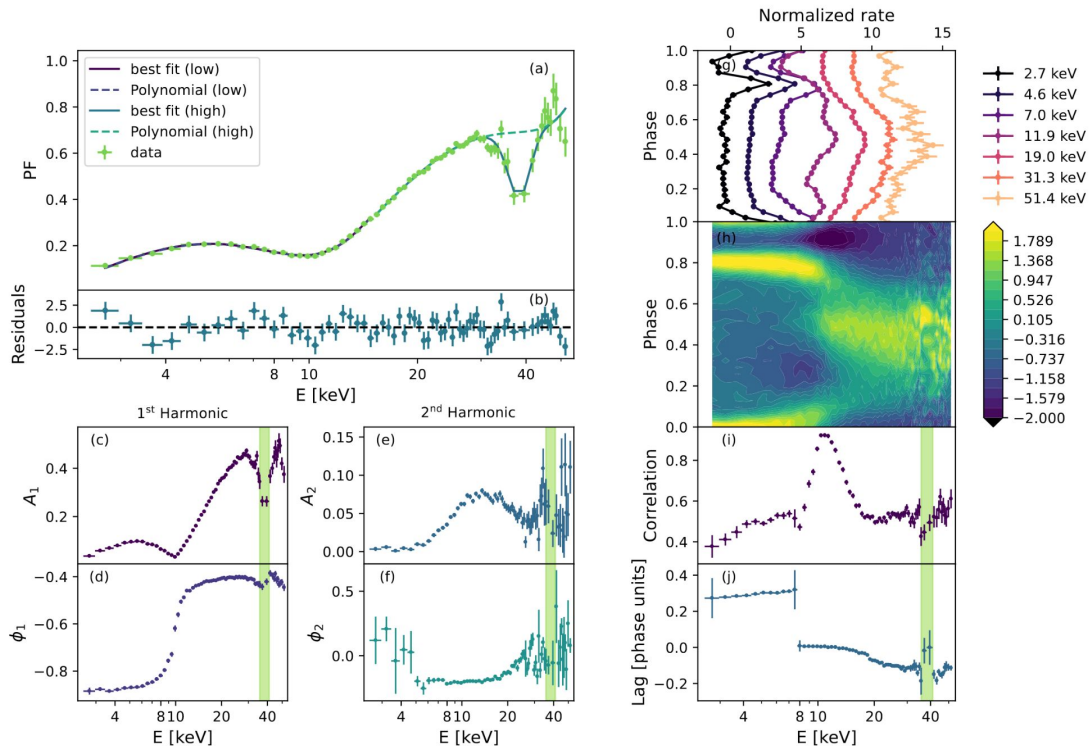


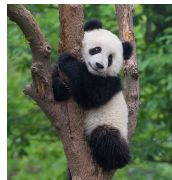
|  | PF                 | 1 <sup>st</sup>      | 2 <sup>nd</sup>            | Spectral                       |     |
|--|--------------------|----------------------|----------------------------|--------------------------------|-----|
| $\chi^2_{\text{red,lo}}/\text{d.o.f.}$ | 0.7/10             | 0.5/10               | 1.5/14                     | —                              |     |
| $\chi^2_{\text{red,hi}}/\text{d.o.f.}$ | 1.0/47             | 1.2/47               | 1.2/45                     | —                              |     |
| $n_{\text{lo}}$                        | 4                  | 4                    | 3                          | —                              |     |
| $n_{\text{hi}}$                        | 3                  | 3                    | 2                          | —                              |     |
| $E_{\text{split}}$                     | 11.17              | 11.01                | 12.82                      | —                              | keV |
| $A_{\text{Fe}}$                        | $-0.072 \pm 0.002$ | $-0.0486 \pm 0.0016$ | $-0.019^{+0.003}_{-0.004}$ | $(6.3 \pm 0.7) \times 10^{-3}$ | keV |
| $E_{\text{Fe}}$                        | $6.503 \pm 0.008$  | $6.524 \pm 0.008$    | $6.51 \pm 0.05$            | $6.55 \pm 0.05$                | keV |
| $\sigma_{\text{Fe}}$                   | $0.418 \pm 0.010$  | $0.422 \pm 0.010$    | $0.64^{+0.11}_{-0.08}$     | $0.82^{+0.13}_{-0.10}$         | keV |
| $A_{\text{Cyc}}$                       | $-10.4 \pm 0.7$    | $-6.9 \pm 0.5$       | $-2.36 \pm 0.09$           | $0.6 \pm 0.3$                  |     |
| $E_{\text{Cyc}}$                       | $40.44 \pm 0.15$   | $40.32 \pm 0.16$     | $40.10 \pm 0.16$           | $37.4 \pm 0.2$                 | keV |
| $\sigma_{\text{Cyc}}$                  | $6.82 \pm 0.19$    | $7.2 \pm 0.2$        | $5.18 \pm 0.14$            | $5.8 \pm 0.3$                  | keV |



# Pulse Profiles of Accreting Neutron stars Deeply Analysed - PPANDA

4U 1626-67 30101029002

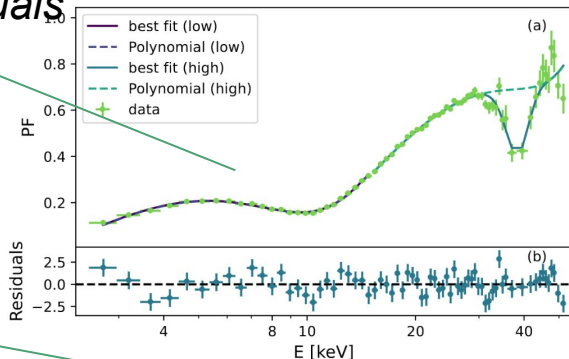




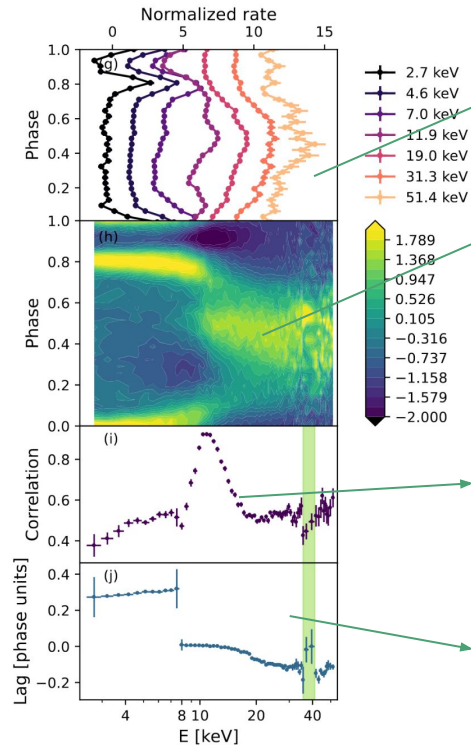
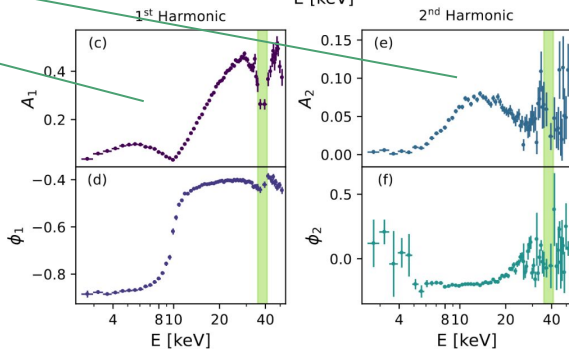
# Pulse Profiles of Accreting Neutron stars Deeply Analysed - PPANDA

4U 1626-67 30101029002

*Pulsed Fraction Spectrum  
best-fit and residuals*



*full harmonic  
decomposition:  
amplitudes and  
phases of the  
harmonics*



*Pulse profiles*

*Heat map  
Energy-phase  
matrix*

*Correlation  
spectrum*

*Lag spectrum*

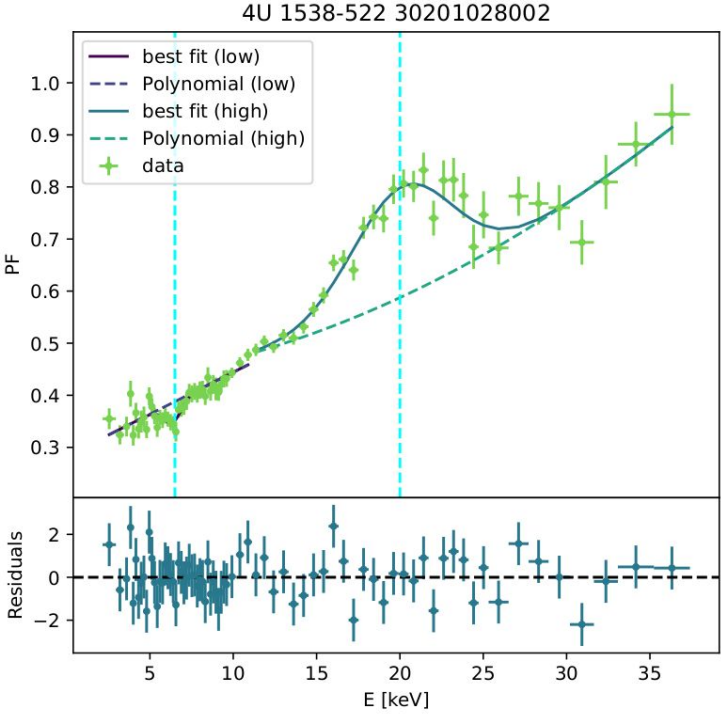
Fantastic, let's analyse all the sources with cyclotron lines !!!

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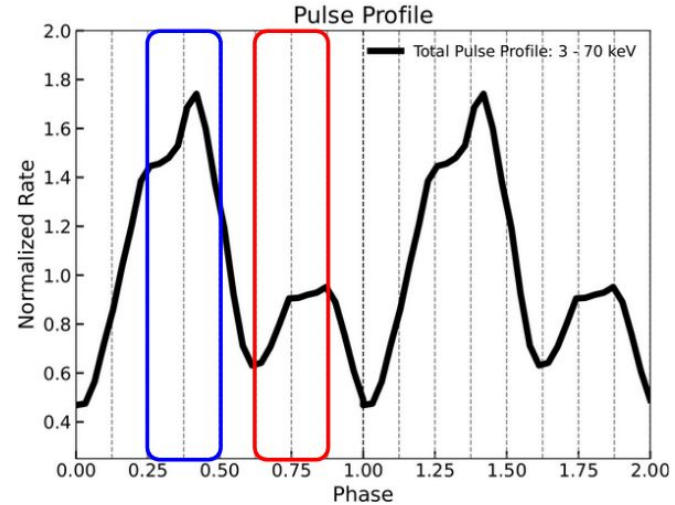
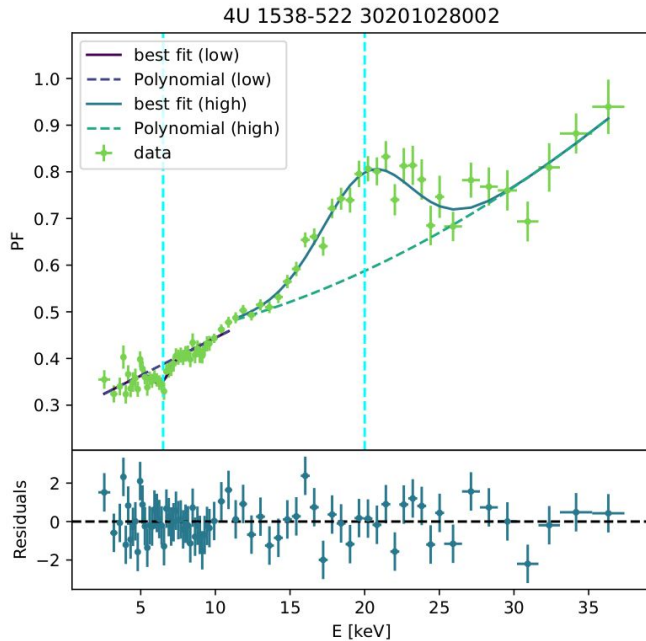
Dips and bumps

# Sometimes there are bumps at the Ecycl



# PFS: dips and bumps at the cyclotron line energy

Not a dip, but some sort of bump...

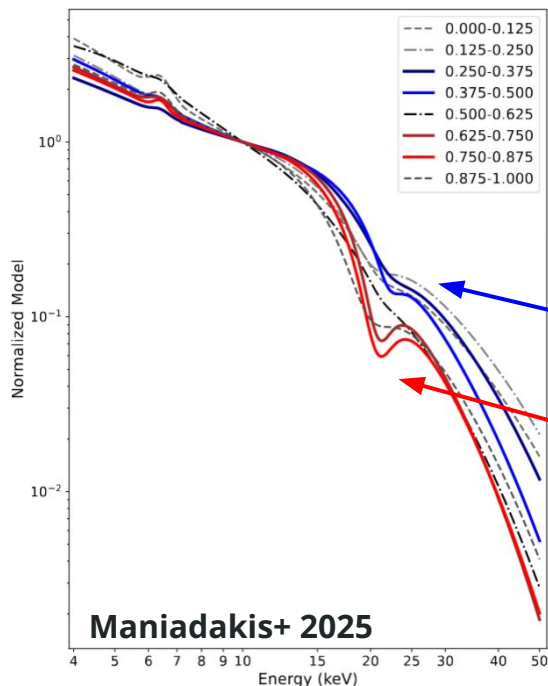


Maniadakis, Sokolova-Lapa, D'Ai et al., A&A, 2025,

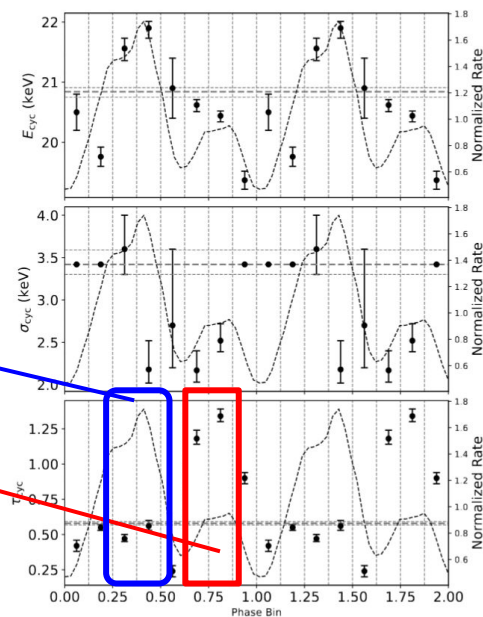
*How the spin-phase variability of cyclotron lines shapes the pulsed fraction spectra: Insights from 4U1538–52.*

# Cyclotron line energy spin dependence

Spectra of all 8 phase bins normalized at 10 keV

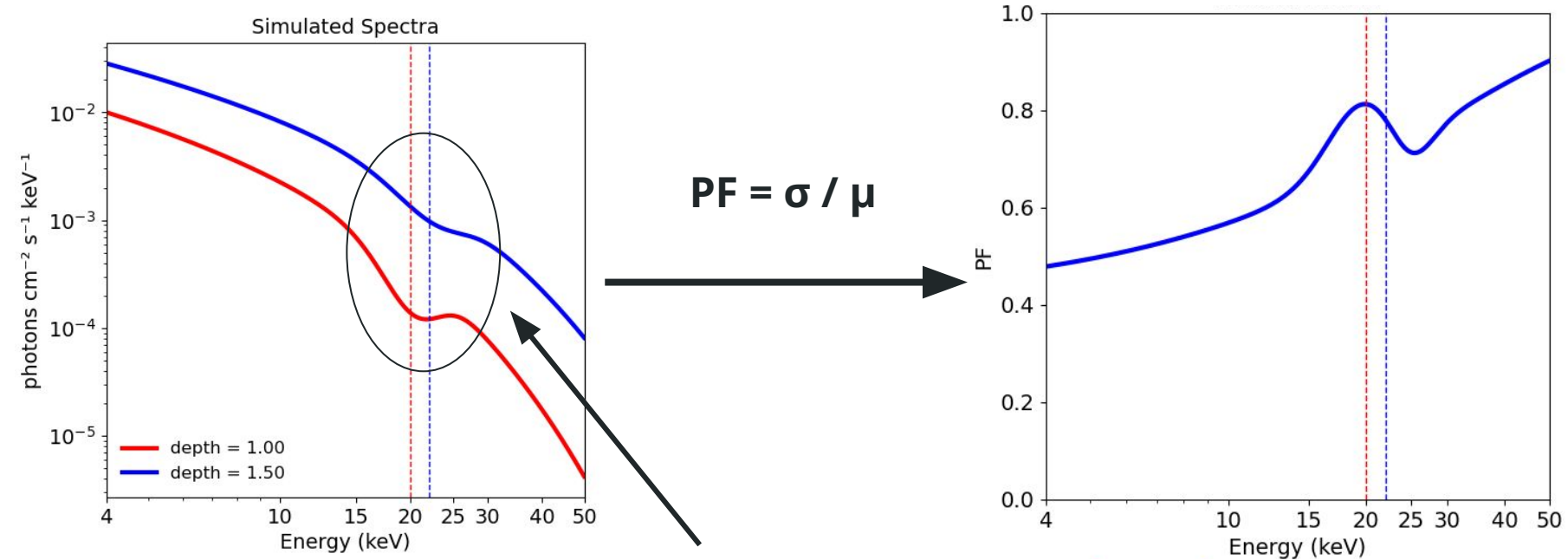


Cyclotron line parameters variation



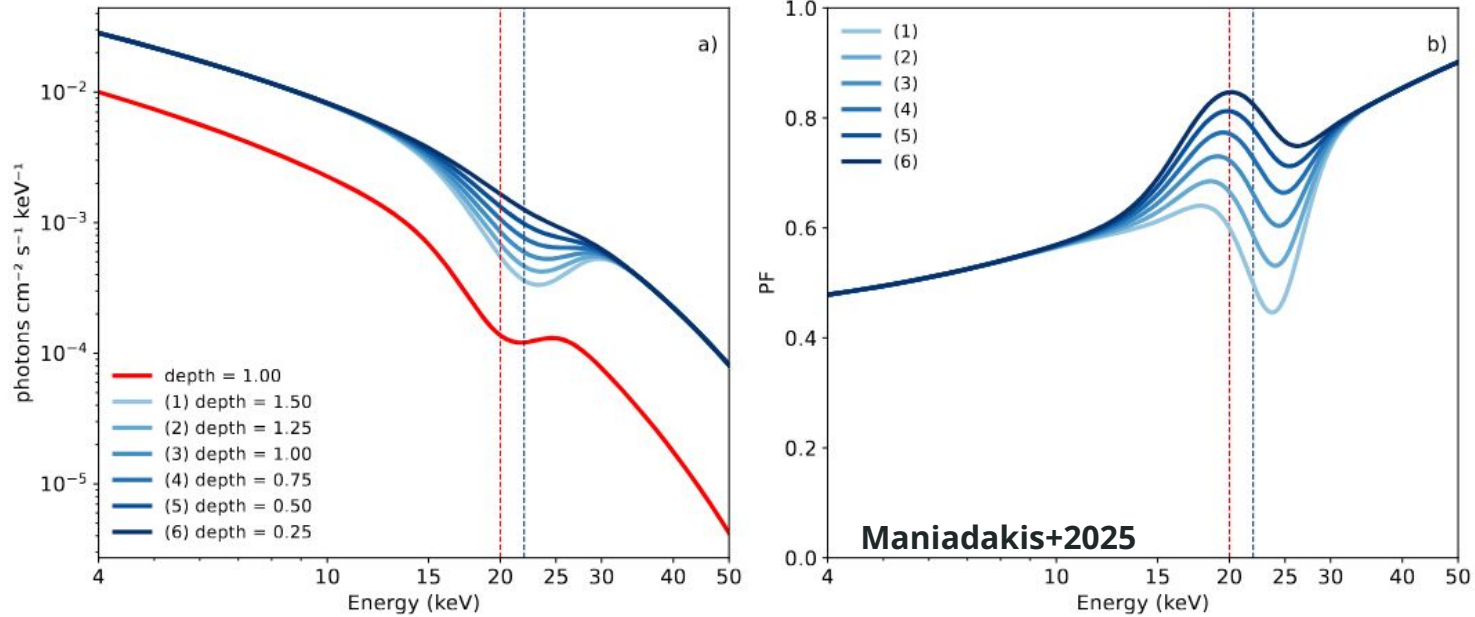
1. **CRSF deeper** at **secondary** peak
2. **CRSF shallower** at **primary** peak

# Reproducing the PF features



Simply said: the PF spectra track the **spectral spin variability of the Cyclotron line**

# CRSF depth vs spin-dependent flux



Increasing **depth** of the CRSF of the primary peak spectrum

**Bump becomes smaller and smaller**  $\longrightarrow$  **Dip becomes deeper and deeper**

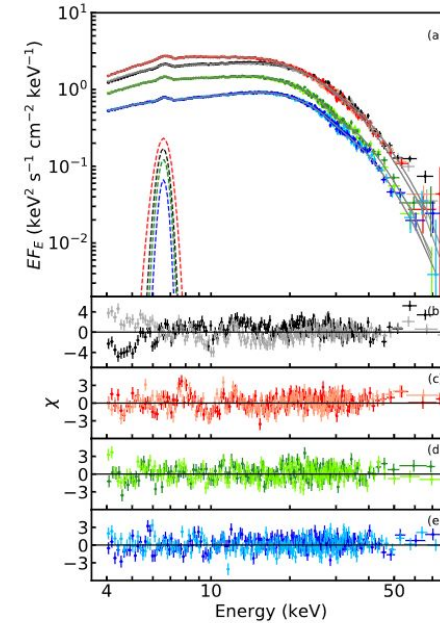
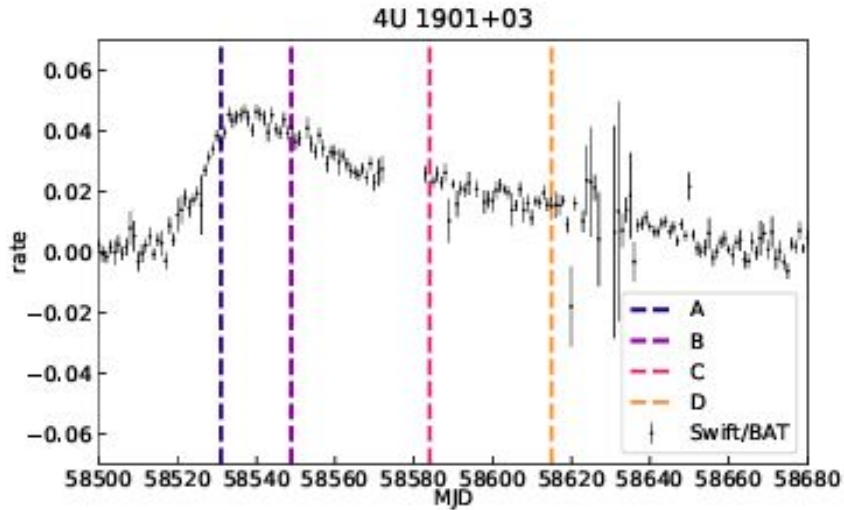
Feature has a more **complicated shape**: the energy does not coincide with the spectral value

Uncovering  
state-dependent  
cyclotron lines

# 4U 1901+03 Spectra Modelling

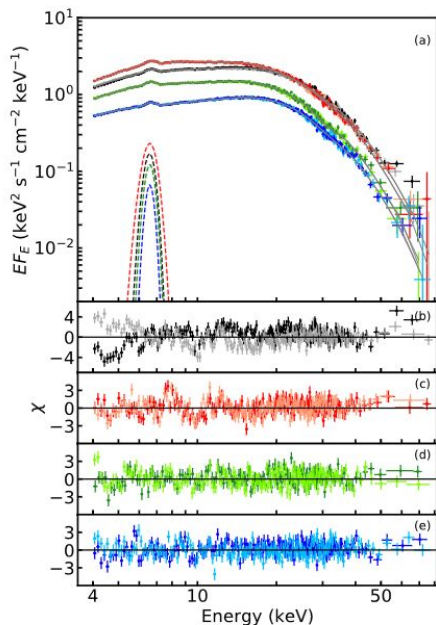
## Spectral evolution of X-ray pulsar 4U 1901+03 during the 2019 outburst based on Insight-HXMT and *NuSTAR* observations

Armin Nabizadeh<sup>1</sup>, Sergey S. Tsygankov<sup>1,2</sup>, Long Ji<sup>3</sup>, Victor Doroshenko<sup>3,2</sup>, Sergey V. Molkov<sup>2</sup>, Youli Tuo<sup>4</sup>, Shuang-Nan Zhang<sup>4</sup>, Fan-Jun Lu<sup>4</sup>, Shu Zhang<sup>4</sup>, and Juri Poutanen<sup>1,2,5</sup>



**Fig. 6.** Same as Fig. 2, but only for the *NuSTAR* observations together with the best-fit model (TBABS  $\times$  (GAU+COMPTT  $\times$  GABS  $\times$  GABS)). Lighter colours represent the data obtained from the *NuSTAR*/FPMB module.

# 4U 1901+03 Energy Spectra Modelling



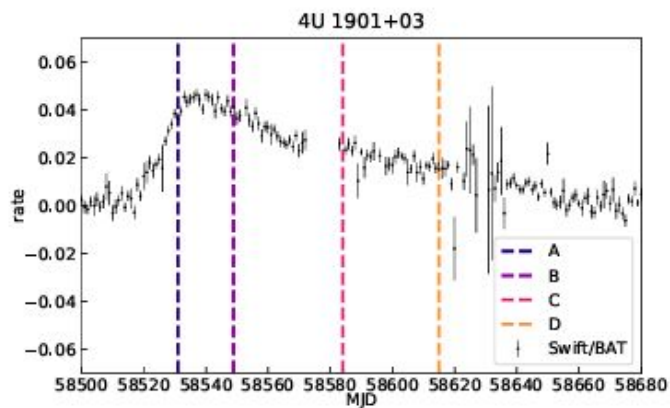
**Table 3.** Best-fit parameters for the model  $\text{TBABS} \times (\text{GAU} + \text{COMPTT} \times \text{GABS} \times \text{GABS})$  for the four data sets of pulse-averaged spectra during the 2019 outburst.

| Model                                 | Parameters             | Units  | NuObs1                    | NuObs2                    | NuObs3<br>+P0211006008    | NuObs4<br>+P0211006022    |
|---------------------------------------|------------------------|--|---------------------------|---------------------------|---------------------------|---------------------------|
| CONSTANT <sup>(a)</sup>               | FPMB/FPMA              |  | $0.996^{+0.001}_{-0.001}$ | $1.026^{+0.001}_{-0.001}$ | $1.028^{+0.001}_{-0.001}$ | $1.017^{+0.001}_{-0.001}$ |
| CONSTANT <sup>(b)</sup>               | LE/FPMA                |  |                           |                           | $0.995^{+0.004}_{-0.004}$ | $0.935^{+0.003}_{-0.003}$ |
| CONSTANT <sup>(c)</sup>               | ME/FPMA                |  |                           |                           | $1.004^{+0.003}_{-0.003}$ | $0.983^{+0.002}_{-0.002}$ |
| TBABS                                 | $N_{\text{H}}$         | $10^{22} \text{ cm}^{-2}$                    | $0.9^{+0.2}_{-0.2}$       | $0.3^{+0.2}_{-0.2}$       | $1.17^{+0.05}_{-0.05}$    | $1.42^{+0.05}_{-0.05}$    |
| COMPTT                                | $T_0$                  | keV  | $1.08^{+0.01}_{-0.01}$    | $1.24^{+0.02}_{-0.02}$    | $1.01^{+0.01}_{-0.01}$    | $0.88^{+0.02}_{-0.01}$    |
|                                       | $kT$                   | keV  | $5.64^{+0.06}_{-0.06}$    | $5.25^{+0.08}_{-0.09}$    | $4.88^{+0.06}_{-0.05}$    | $4.91^{+0.04}_{-0.04}$    |
|                                       | $\tau_p$               |  | $4.592^{+0.04}_{-0.04}$   | $4.55^{+0.04}_{-0.05}$    | $5.04^{+0.05}_{-0.05}$    | $5.29^{+0.08}_{-0.1}$     |
|                                       | $A_{\text{comptt}}$    |  | $0.148^{+0.002}_{-0.002}$ | $0.186^{+0.002}_{-0.003}$ | $0.122^{+0.002}_{-0.002}$ | $0.080^{+0.004}_{-0.002}$ |
| GABS                                  | $E_{\text{abs1}}$      | keV  | $10.6^{+0.1}_{-0.1}$      | $10.8^{+0.2}_{-0.2}$      | $10.5^{+0.1}_{-0.1}$      | $9.0^{+0.4}_{-0.8}$       |
|                                       | $\sigma_{\text{abs1}}$ | keV  | $1.1^{+0.2}_{-0.2}$       | $1.7^{+0.2}_{-0.3}$       | $2.1^{+0.2}_{-0.2}$       | $4.4^{+0.8}_{-0.5}$       |
|                                       | $\tau_{\text{abs1}}$   |  | $0.03^{+0.01}_{-0.01}$    | $0.05^{+0.01}_{-0.01}$    | $0.06^{+0.01}_{-0.01}$    | $0.14^{+0.1}_{-0.05}$     |
|                                       | GABS                   | $E_{\text{abs2}}$                            | keV                       | $39.2^{+0.4}_{-0.4}$      | $35.3^{+0.4}_{-1.4}$      | $32.2^{+0.6}_{-0.6}$      |
|                                       | $\sigma_{\text{abs2}}$ | keV  | $10.0^{+3.4}_{-0.5}$      | $9.9^{+2.0}_{-1.5}$       | $5.8^{+0.6}_{-0.5}$       | $5.5^{+0.8}_{-0.6}$       |
|                                       | $\tau_{\text{abs2}}$   |  | $0.46^{+0.19}_{-0.06}$    | $0.37^{+0.2}_{-0.2}$      | $0.30^{+0.09}_{-0.08}$    | $0.21^{+0.09}_{-0.06}$    |
| GAUSSIAN                              | $E_{\text{Fe}}$        | keV  | $6.34^{+0.01}_{-0.01}$    | $6.33^{+0.01}_{-0.01}$    | $6.37^{+0.01}_{-0.01}$    | $6.38^{+0.01}_{-0.01}$    |
|                                       | $\sigma_{\text{Fe}}$   | keV  | $0.30^{+0.02}_{-0.02}$    | $0.31^{+0.02}_{-0.02}$    | $0.28^{+0.02}_{-0.02}$    | $0.23^{+0.02}_{-0.02}$    |
|                                       | $A_{\text{Fe}}$        | $10^{-3} \text{ ph s}^{-1} \text{ cm}^{-2}$  | $3.4^{+0.2}_{-0.2}$       | $5.0^{+0.3}_{-0.3}$       | $2.2^{+0.1}_{-0.1}$       | $0.96^{+0.05}_{-0.05}$    |
| $F_{1-79 \text{ keV}}$ <sup>(d)</sup> |                        | $10^{-9} \text{ erg s}^{-1} \text{ cm}^{-2}$ | $7.49^{+0.03}_{-0.04}$    | $8.51^{+0.05}_{-0.04}$    | $4.95^{+0.01}_{-0.01}$    | $3.082^{+0.009}_{-0.009}$ |
| $F_{4-79 \text{ keV}}$ <sup>(d)</sup> |                        | $10^{-9} \text{ erg s}^{-1} \text{ cm}^{-2}$ | $6.47^{+0.02}_{-0.02}$    | $7.43^{+0.03}_{-0.03}$    | $4.183^{+0.006}_{-0.006}$ | $2.561^{+0.003}_{-0.003}$ |
| $\chi^2(\text{d.o.f.})$               |                        |  | 2085 (1665)               | 1615 (1564)               | 2963 (2949)               | 3417 (3087)               |

**Fig. 6.** Same as Fig. 2, but only for the *NuSTAR* observations together with the best-fit model ( $\text{TBABS} \times (\text{GAU} + \text{COMPTT} \times \text{GABS} \times \text{GABS})$ ). Lighter colours represent the data obtained from the *NuSTAR*/FPMB module.

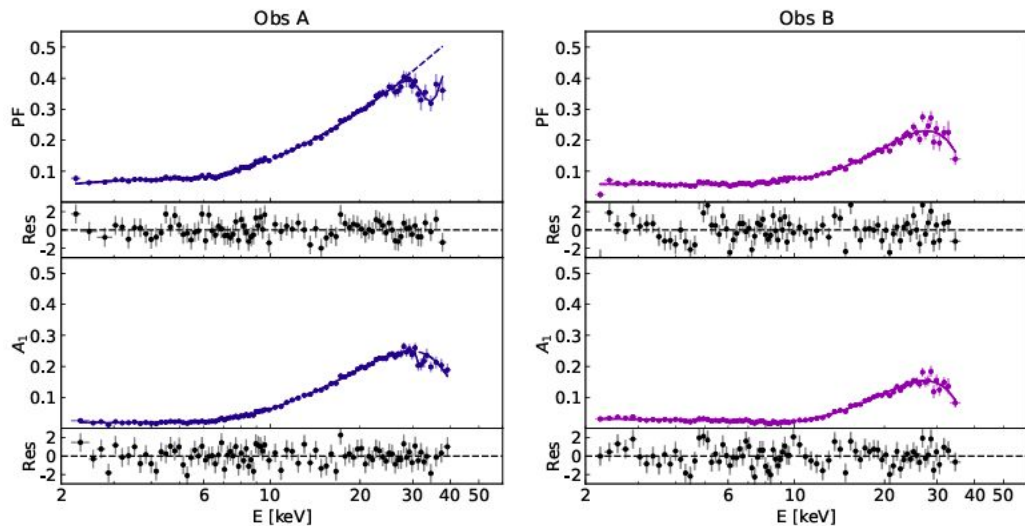
**Notes.** <sup>(a)</sup>Cross-normalisation constant between FPMB and FPMA instruments on board *NuSTAR*. <sup>(b)</sup>Cross-normalisation constant between Insight-HXMT/LE and *NuSTAR*/FPMA instruments. <sup>(c)</sup>Cross-normalisation constant between Insight-HXMT/ME and *NuSTAR*/FPMA instruments. <sup>(d)</sup>Unabsorbed X-ray flux.

# Luminosity-dependence of the PFS features



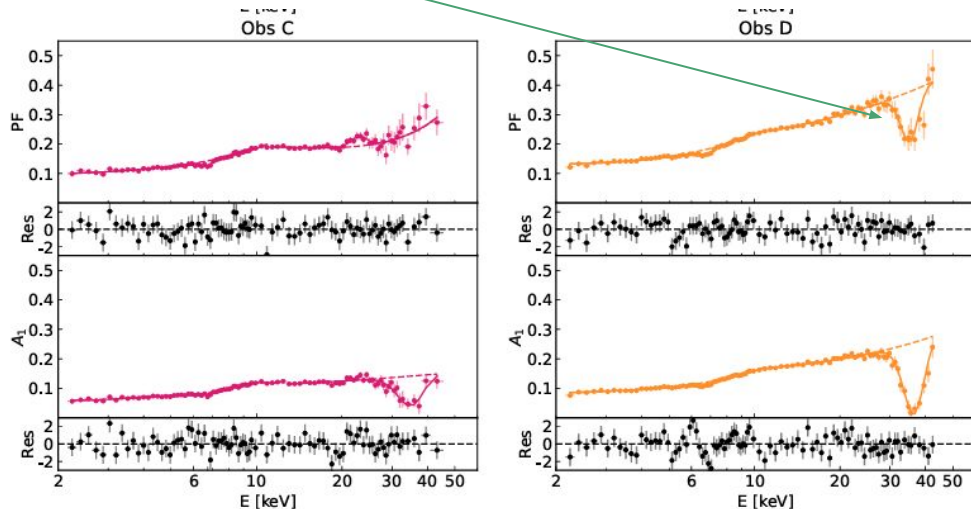
[Ambrosi, D'Ai et al, 2026, A&A](#)

Almost featureless PFS at high Lum



# Luminosity-dependence of the PFS features

A clear hint to a feature at low Lum



**Table 4.** Posterior parameter estimates for the cyclotron resonance model.

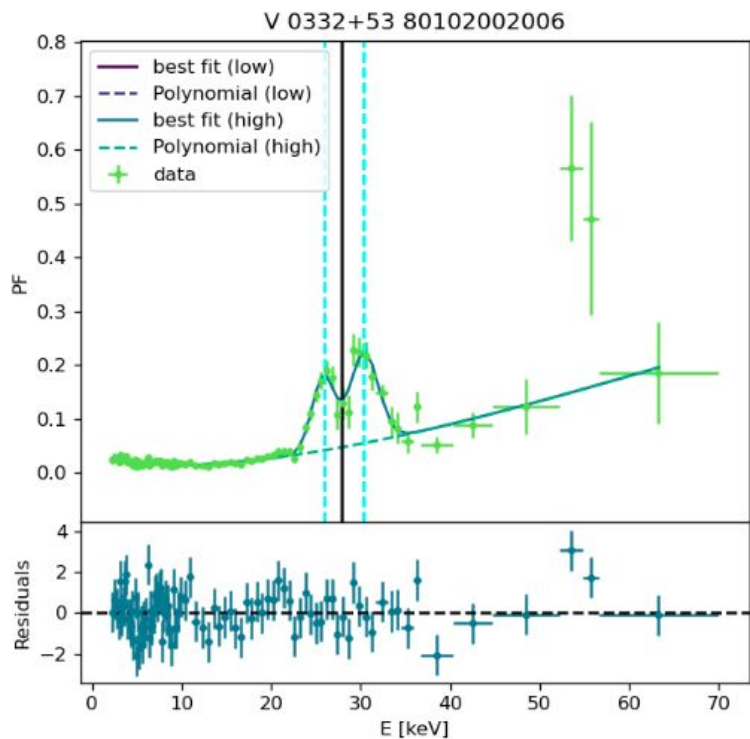
| Parameter                    | A                       | B                   | C                   | D                   |
|------------------------------|-------------------------|---------------------|---------------------|---------------------|
| $C_{\text{FPMB}}$            | $0.938 \pm 0.003$       | $0.988 \pm 0.004$   | $0.985 \pm 0.004$   | $0.969 \pm 0.003$   |
| $\Gamma$                     | $-0.27^{+0.07}_{-0.08}$ | $0.2 \pm 0.1$       | $-0.1 \pm 0.1$      | $-0.8 \pm 0.1$      |
| $E_{\text{cut}}$ [keV]       | $6.2 \pm 0.1$           | $6.7 \pm 0.2$       | $6.1 \pm 0.2$       | $5.4 \pm 0.1$       |
| Norm                         | $0.057 \pm 0.009$       | $0.20 \pm 0.06$     | $0.06 \pm 0.01$     | $0.007 \pm 0.002$   |
| $E_{\text{cyc}}$ [keV]       | $32.1^{+1.2}_{-0.8}$    | $32.2 \pm 1.3$      | $32.1 \pm 0.8$      | $31.7 \pm 0.6$      |
| $\sigma_{\text{CRSF}}$ [keV] | $4.5^{+1.4}_{-1.3}$     | $6.0^{+0.7}_{-1.0}$ | $5.2^{+0.9}_{-0.8}$ | $5.8 \pm 0.7$       |
| Depth <sub>CRSF</sub> [keV]  | $0.8^{+0.5}_{-0.3}$     | $1.6^{+0.6}_{-0.5}$ | $3.0^{+1.1}_{-0.8}$ | $2.7^{+0.8}_{-0.6}$ |
| $\log_{10}\text{BF}$         | 0.98                    | 5.1                 | 25.0                | 23.8                |

**Notes.** We report the median and 68% credible intervals (16th and 84th percentiles) for each parameter. The final row provides the log-evidence ( $\log_{10}\text{BF}$ ) compared to a null model.

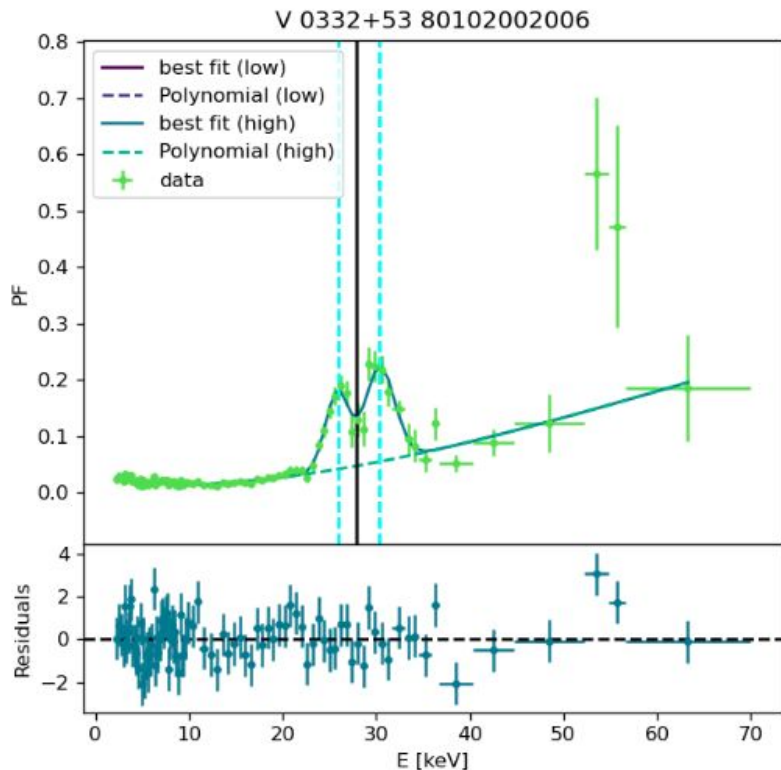
[Ambrosi, D'Ai et al, 2026, A&A](#)

Cyclotron line wings

# The PFS of V 0332+53



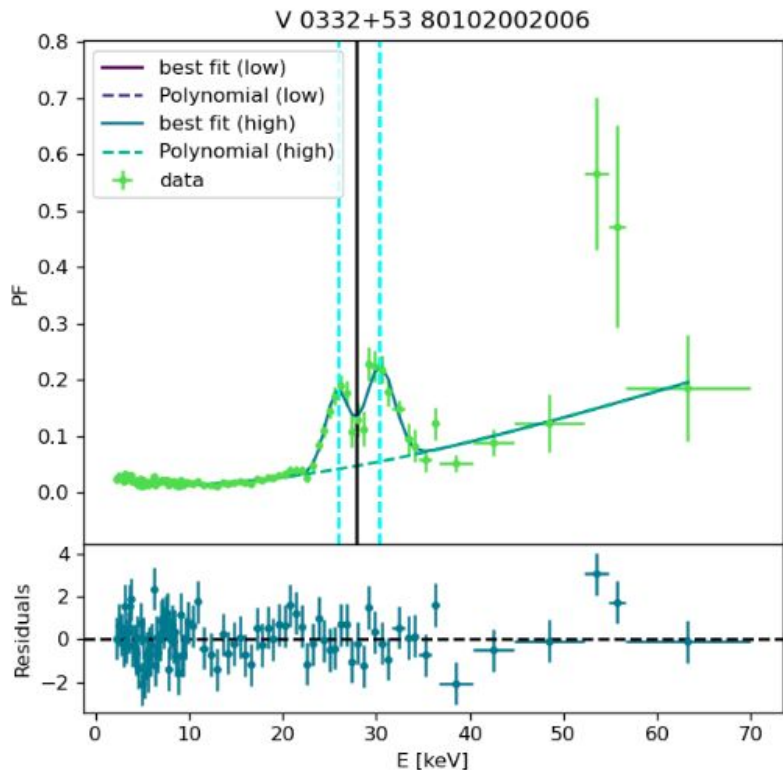
# The PF spectra of V0332 from Nustar observations



[D'Ai et al., A&A, 2025](#)

|  | 806              |                   |                        |                   |
|--|------------------|-------------------|------------------------|-------------------|
| $\chi^2_{\text{red,lo}}/\text{d.o.f.}$ | 1.0/43           | 1.2/43            | 0.9/45                 | —                 |
| $\chi^2_{\text{red,hi}}/\text{d.o.f.}$ | 1.2/36           | 1.9/36            | 1.3/33                 | —                 |
| $n_{\text{pol}}^{(\text{hi})}$         | 3                | 3                 | 3                      | —                 |
| $n_{\text{pol}}^{(\text{lo})}$         | 1                | 1                 | 2                      | —                 |
| $E_{\text{split}}$ (keV)               | 10.01            | 10.01             | 12.08                  | —                 |
| $A_1$                                  | $0.38 \pm 0.02$  | $0.228 \pm 0.011$ | $0.28^{+0.06}_{-0.10}$ | 0.86              |
| $E_1$ (keV)                            | $25.78 \pm 0.08$ | $25.81 \pm 0.06$  | $27.4^{+0.3}_{-0.5}$   | 27.93             |
| $\sigma_1$ (keV)                       | $1.20 \pm 0.06$  | $1.12 \pm 0.05$   | $1.96^{+0.18}_{-0.22}$ | 8.47              |
| $A_2$                                  | $0.66 \pm 0.05$  | $0.340 \pm 0.019$ | $0.17^{+0.10}_{-0.05}$ | —                 |
| $E_2$ (keV)                            | $30.28 \pm 0.11$ | $30.56 \pm 0.07$  | $31^{+2}_{-2}$         | —                 |
| $\sigma_2$ (keV)                       | $1.68 \pm 0.14$  | $1.16 \pm 0.06$   | $2.0^{+0.5}_{-0.7}$    | —                 |
| $D_{\text{cyc}}$                       | —                | —                 | —                      | $0.862 \pm 0.002$ |
| $E_{\text{cyc}}$ (keV)                 | —                | —                 | —                      | $28.40 \pm 0.02$  |
| $\sigma_{\text{cyc}}$ (keV)            | —                | —                 | —                      | $7.59 \pm 0.08$   |

# The PF spectra of V0332 from Nustar observations

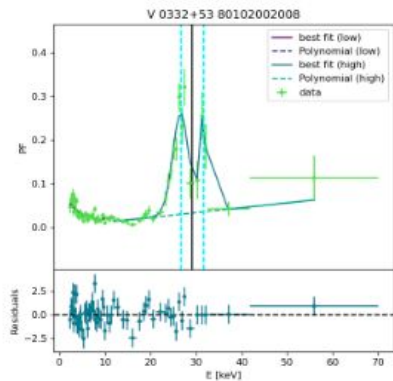
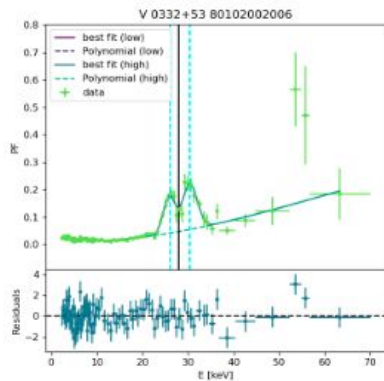
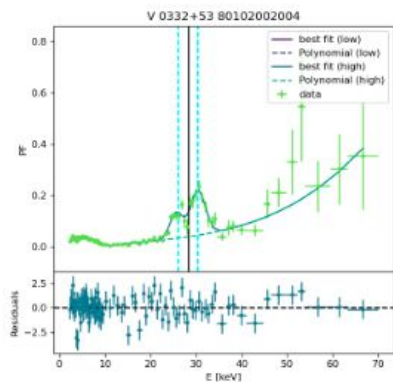
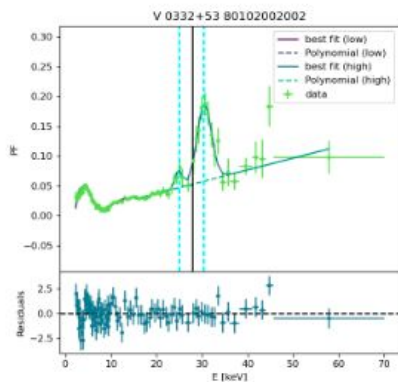


[D'Ai et al., A&A, 2025](#)

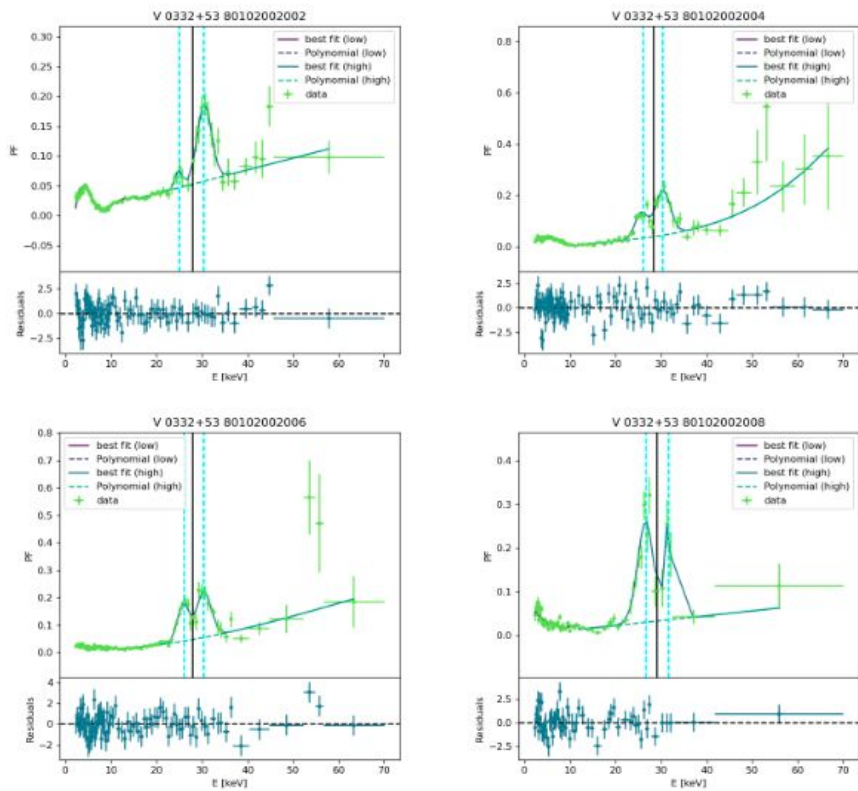
|  | 806              |                   |                        |                   |
|--|------------------|-------------------|------------------------|-------------------|
| $\chi^2_{\text{red,lo}}/\text{d.o.f.}$ | 1.0/43           | 1.2/43            | 0.9/45                 | —                 |
| $\chi^2_{\text{red,hi}}/\text{d.o.f.}$ | 1.2/36           | 1.9/36            | 1.3/33                 | —                 |
| $n_{\text{pol}}^{(\text{hi})}$         | 3                | 3                 | 3                      | —                 |
| $n_{\text{pol}}^{(\text{lo})}$         | 1                | 1                 | 2                      | —                 |
| $E_{\text{split}} \text{ (keV)}$       | 10.01            | 10.01             | 12.08                  | —                 |
| $A_1$                                  | $0.38 \pm 0.02$  | $0.228 \pm 0.011$ | $0.28^{+0.06}_{-0.10}$ | 0.86              |
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| $\sigma_2 \text{ (keV)}$               | $1.68 \pm 0.14$  | $1.16 \pm 0.06$   | $2.0^{+0.5}_{-0.7}$    | —                 |
| $D_{\text{cyc}}$                       | —                | —                 | —                      | $0.862 \pm 0.002$ |
| $E_{\text{cyc}} \text{ (keV)}$         | —                | —                 | —                      | $28.40 \pm 0.02$  |
| $\sigma_{\text{cyc}} \text{ (keV)}$    | —                | —                 | —                      | $7.59 \pm 0.08$   |

from the spectral analysis of [Doroshenko+17](#)

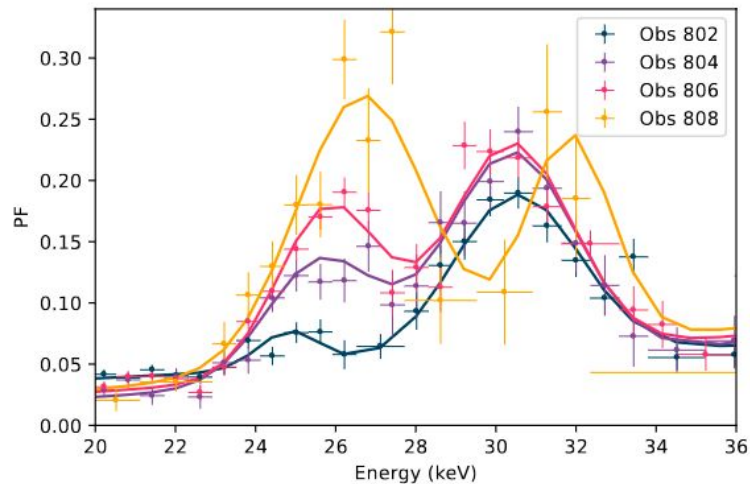
The overall picture: two peaks always at both side of  $E_{cyc}$



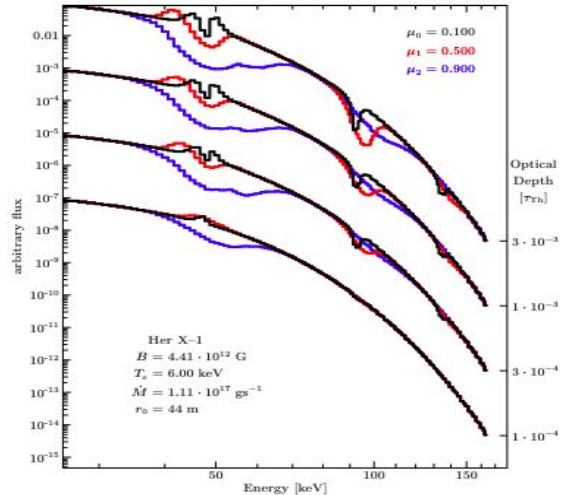
# The overall picture: two peaks always at both side of $E_{cyc}$



Data and best-fitting models from the first 4 obs.



# What is the origin of this variability?



**Fig. 5.** Continuum from Becker & Wolff (2007) with imprinted cyclotron lines for several angles  $\mu = \cos \theta$  to the magnetic field axis and optical depths  $\tau$ . The continuum parameters are the same as in the spectrum from Becker & Wolff (2007, Fig. 6 therein) for Her X-1. The different colors show three angles to the magnetic field axis. The optical depth is increasing from the bottom to the top as shown by the axis on the right-hand side.

Cyclotron lines are (theoretically) expected to be asymmetric with broad line wings depending on the observing angle, and physical and geometrical properties of the line forming region.

The appearance of these wings is strongly indicative of a face-on geometry, with a small angle between the rotation and magnetic axis.

# The low-energy landscape

# Building a broadband PFS

EPIC/pn and NuSTAR cross-calibration of pulse profiles from a simultaneous observation of Vela X-1

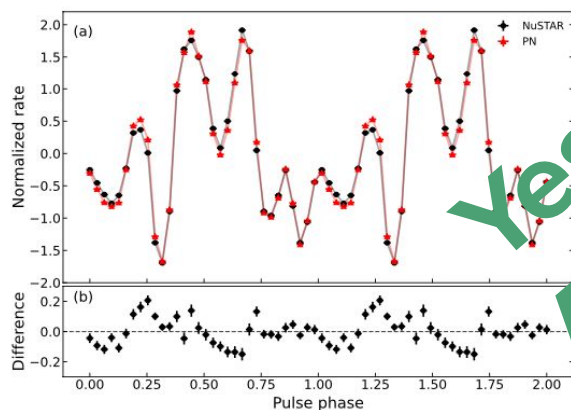
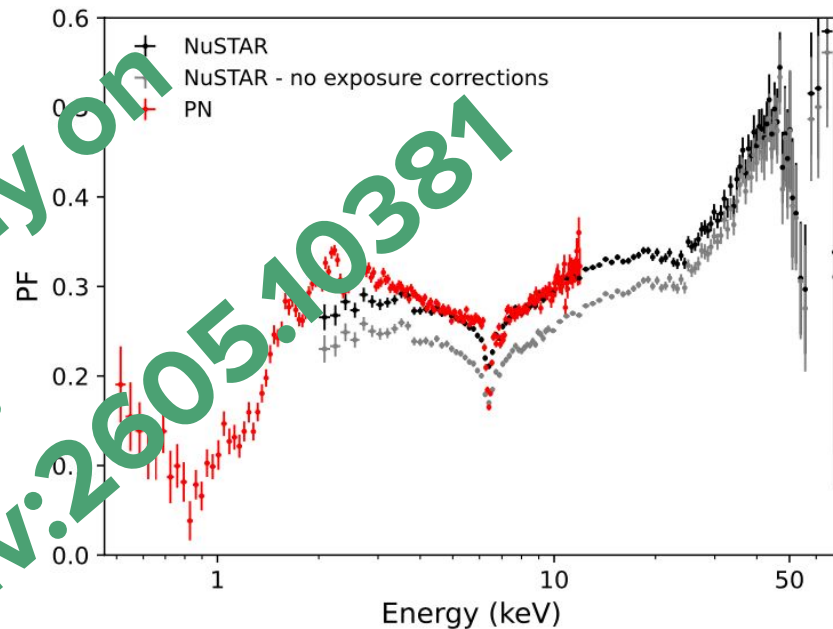


Fig. 5: (a) Pulse profiles of Vela X-1 in the 4–5 keV energy band extracted with *XMM-Newton*/EPIC-pn and *NuSTAR*, folded into 32 phase bins. (b) Phase-by-phase difference between the normalized pulse profiles derived from the two instruments.



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# Building a broadband PFS

EPIC/pn and NuSTAR cross-calibration of pulse profiles from a simultaneous observation of Vela X-1

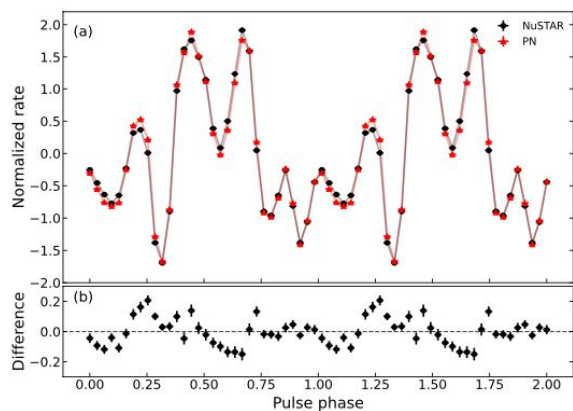
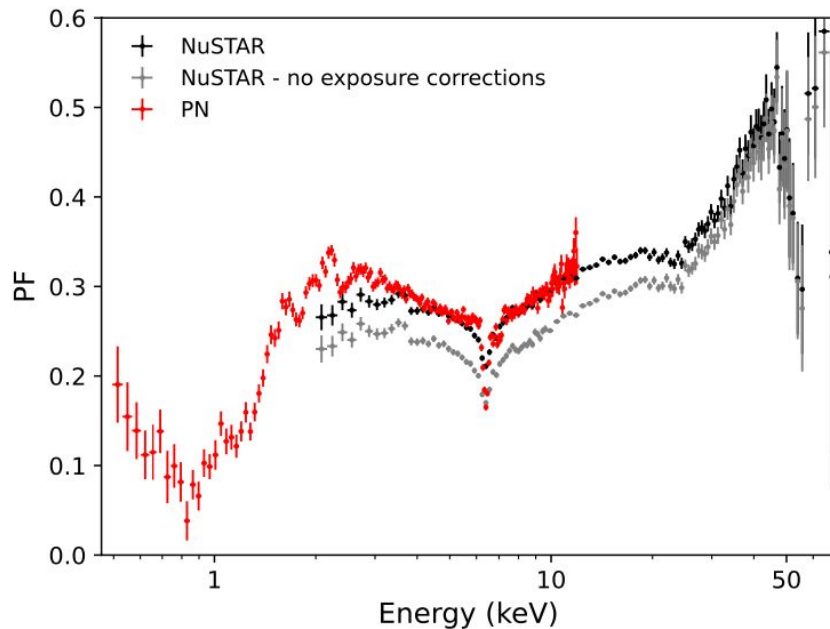
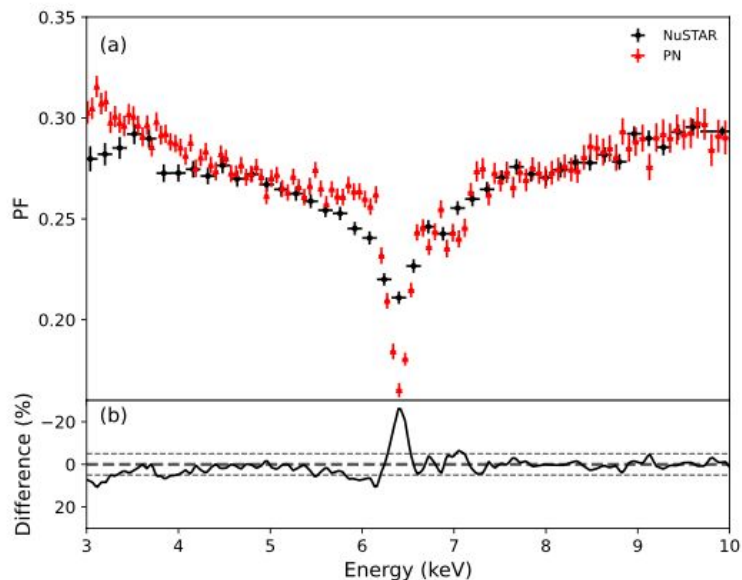


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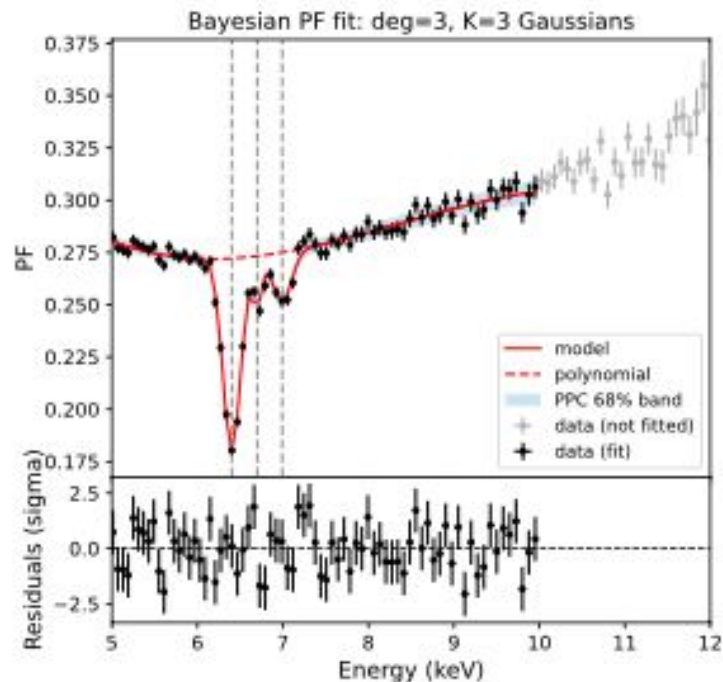


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# The iron range landscape

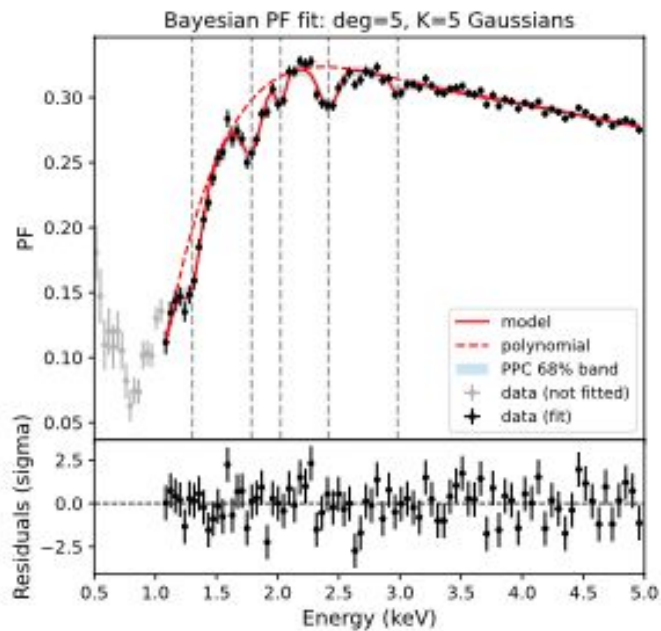


(a) Pulsed fraction spectra calculated with the rms method.



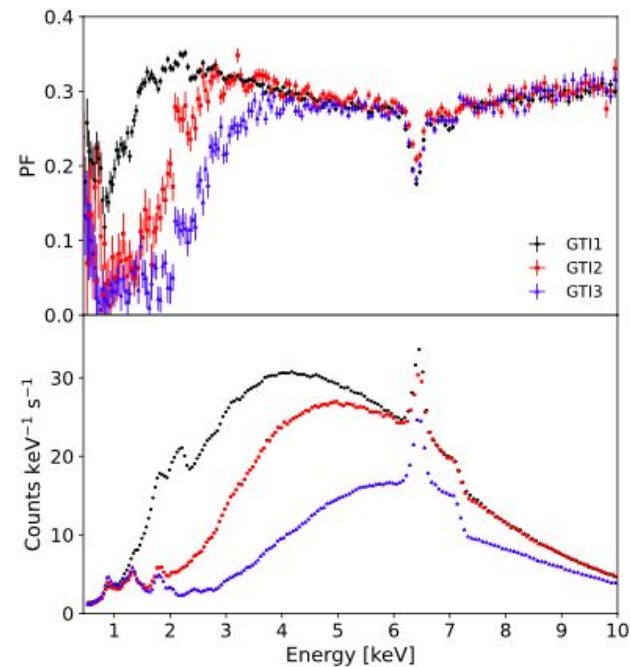
(b)

# The low-energy landscape of spectral features



(a)

## Time-dependent evolution of the PFS



Exploiting the high  
resolution of XRISM

# XRISM observation of Cen X-3

196 ks observation made on Feb. 12 2024, covering one complete orbit ( $P_{\text{orb}}=179.7$  ks)

THE ASTROPHYSICAL JOURNAL LETTERS, 977:L21 (8pp), 2024 December 10

<https://doi.org/10.3847/2041-8213/ad946d>

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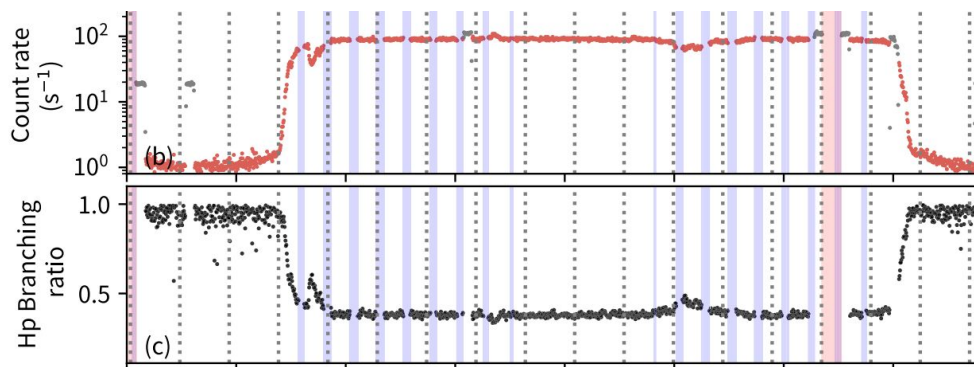
OPEN ACCESS



## Detection of the Orbital Modulation of Fe $K\alpha$ Fluorescence Emission in Centaurus X-3 Using the High-resolution Spectrometer Resolve on board XRISM

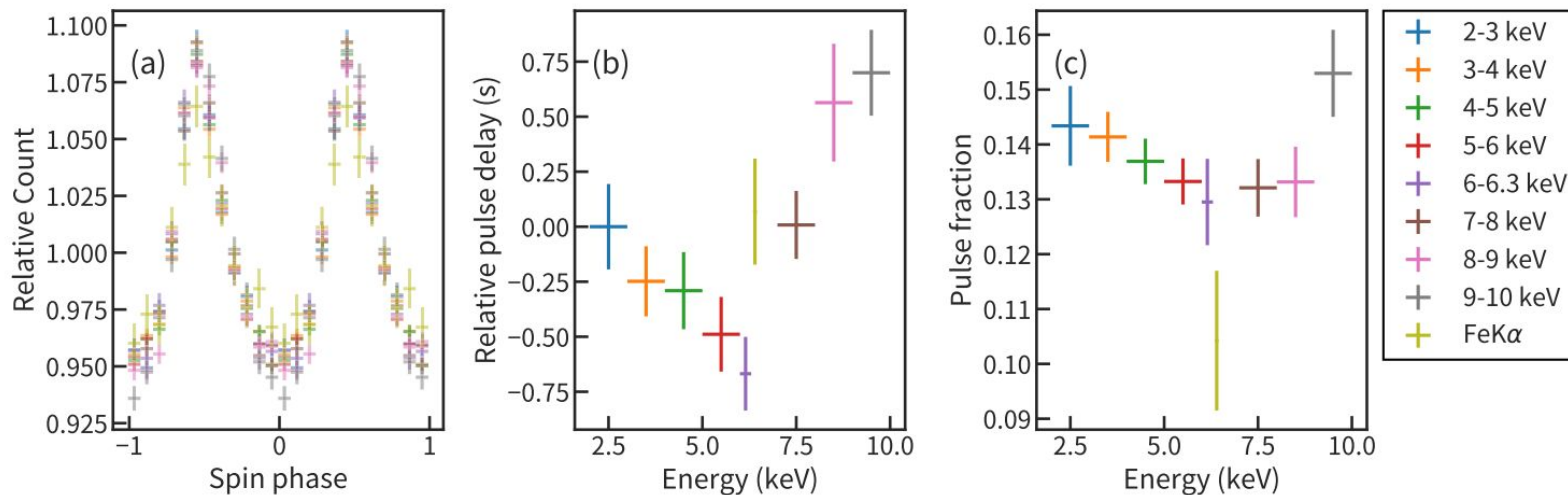
Yuto Mochizuki<sup>1,2</sup>, Masahiro Tsujimoto<sup>1</sup>, Richard L. Kelley<sup>3</sup>, Bert Vander Meulen<sup>4</sup>, Teruaki Enoto<sup>5</sup>, Yutaro Nagai<sup>5</sup>, Chris Done<sup>6</sup>, Pragati Pradhan<sup>7</sup>, Natalie Hell<sup>8</sup>, Katja Pottschmidt<sup>9,10</sup>, Ken Ebisawa<sup>1,2</sup>, and Ehud Behar<sup>11</sup>

9.3e6 of clean events (3.6e6 of Hp)



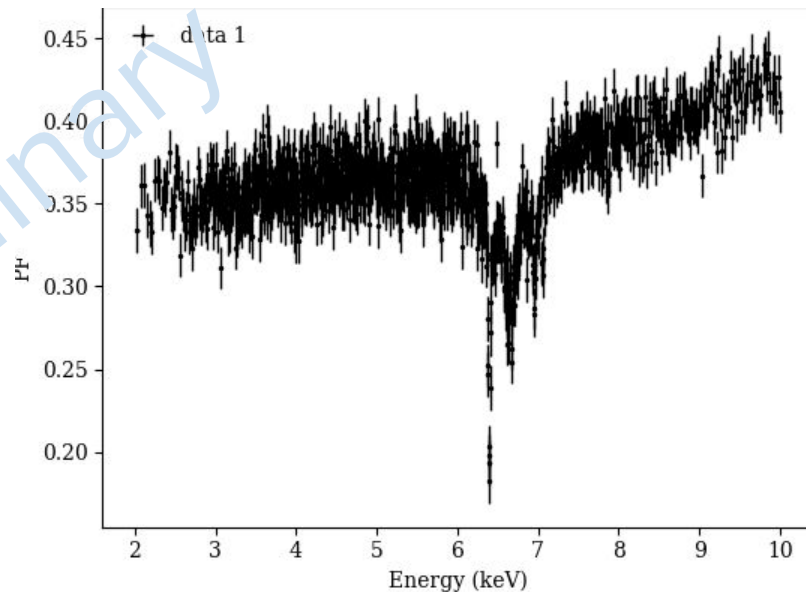
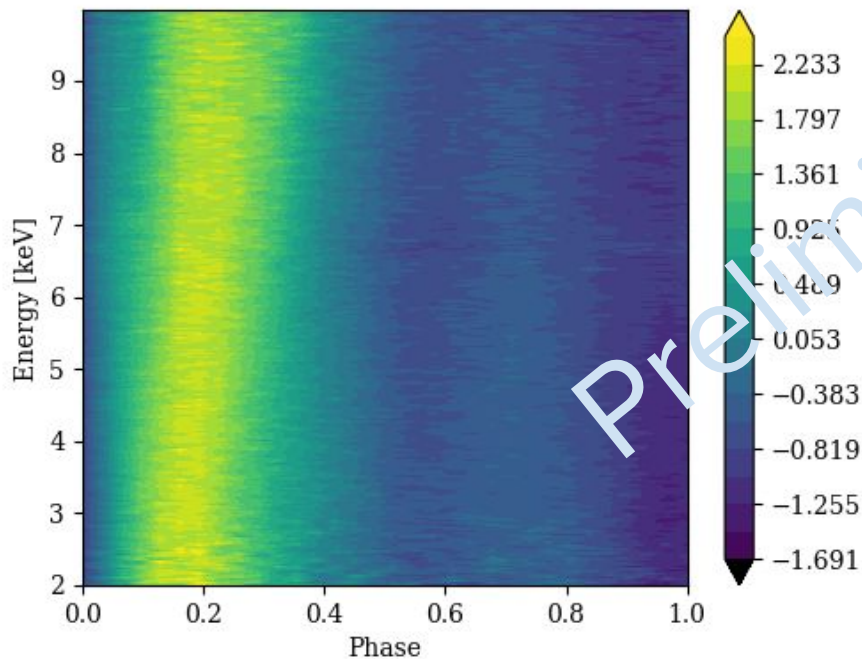
# NS timing & energy resolved profiles

Mochizuki+24



**Figure 4.** (a) Pulse shape folded by  $P_{\text{spin}}$ , (b) phase delay relative to the lowest energy band as a function of energy, and (c) pulse fraction as a function of energy. The Fe K $\alpha$  count rate is from 6.35 to 6.45 keV.

# The 2-12 keV Resolve energy phase matrix and PFS



# Conclusions

- Tested methodology for a large variety of cases
- Introduced flexibility for ingesting different types of detectors
- Configurable parameters for the perfect fine-tuning (choice of GTI, best signal-to-noise ratio, fit modelling and so on)
- Working on a spectral-timing approach to improve determination of spectral and timing parameters

Do you have a particular source you want to analyse? Want to join?

Contact me **[antonino.dai@inaf.it](mailto:antonino.dai@inaf.it)**

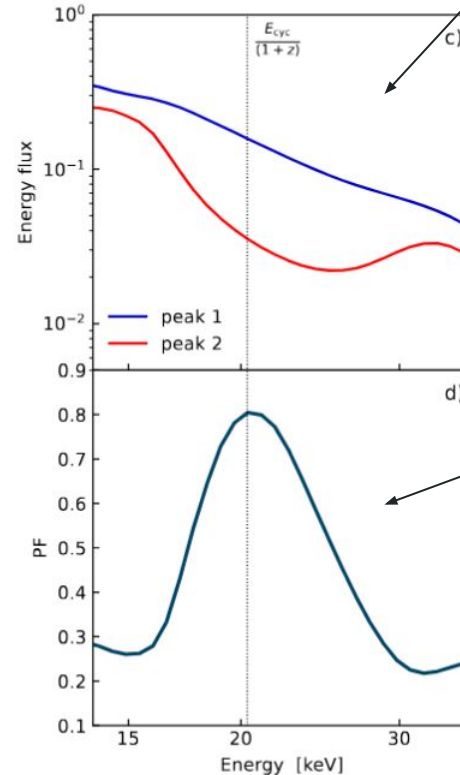
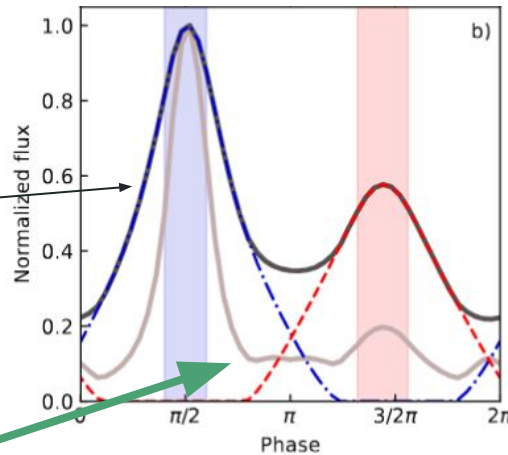
Back-up material

# Physical modeling simulations using the **FINRAD** code (Sokolova-Iapa+2021,2023)

We **reproduce the observables**, using the **FINRAD** code (Radiative Transfer Equation for two hotspots in NS)

**Simulated total pulse profile**

**Energy resolved pulse profile around the CRSF energy**



**Simulated Primary and secondary peak spectra**

**Reproducing the bump at the PF spectrum**

Maniadakis+ 2025

# Resulting Geometry of 4U 1538

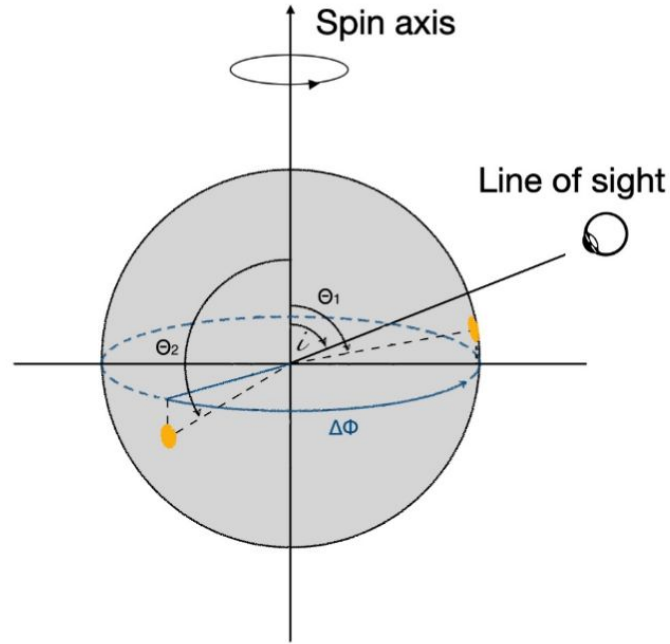


Fig. 14: Geometry adopted for 4U 1538-52, showing the neutron star, magnetic poles at  $\Theta_1 = 80^\circ$  and  $\Theta_2 = 105^\circ$ , azimuthal separation  $\Delta\Phi = 168^\circ$ , and inclination to the observer's line of sight  $i = 67^\circ$ .

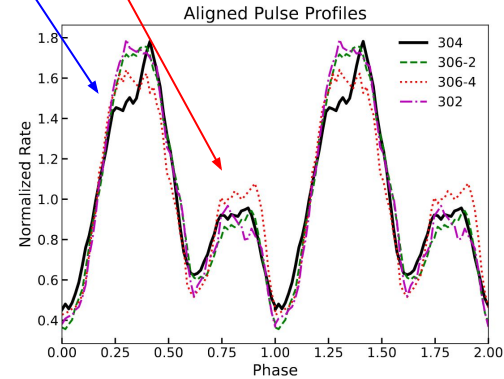
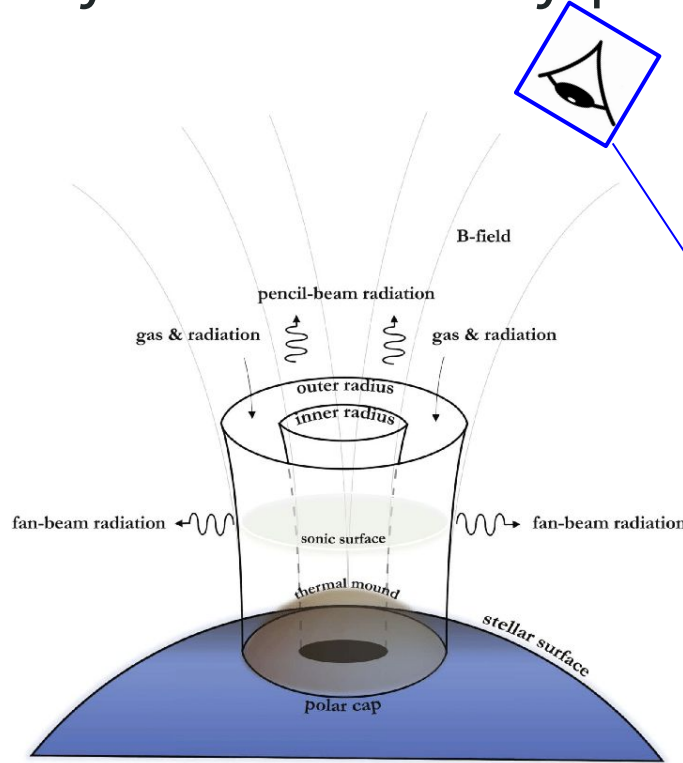
# Primary vs Secondary peak

## Primary peak:

- Higher flux
- **Smaller** cyclotron cross section

## Secondary peak:

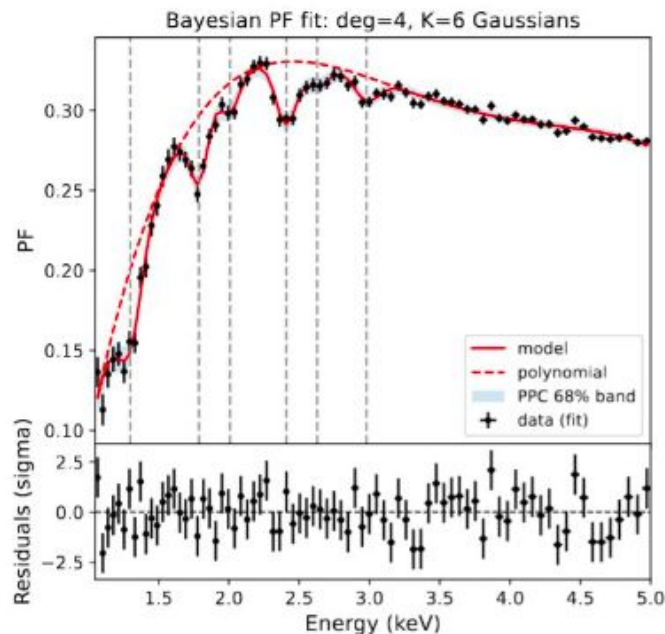
- Lower flux
- **Higher** cyclotron cross section



# Energy range: 1 - 5 keV: EPIC-pn data / Bayesian fitting

Gaussian priors:

- centroid energies
  - widths of lines: energy resolution
- 
- Mg XI (f,i,r):  $E_{\text{ref}} = 1.338 \text{ keV} \rightarrow E_{\text{pf}} = 1.30 \pm 0.01 \text{ keV}$
  - Si XIII (f,i,r):  $E_{\text{ref}} = 1.823 \text{ keV} \rightarrow E_{\text{pf}} = 1.79 \pm 0.01 \text{ keV}$
  - Si XIV Ly $\alpha$ :  $E_{\text{ref}} = 2.0049 \text{ keV} \rightarrow E_{\text{pf}} = 2.01 \pm 0.02 \text{ keV}$
  - S XV (f,i,r):  $E_{\text{ref}} = 2.439 \text{ keV} \rightarrow E_{\text{pf}} = 2.41 \pm 0.01 \text{ keV}$
  - S XVI Ly $\alpha$ :  $E_{\text{ref}} = 2.6207 \text{ keV} \rightarrow E_{\text{pf}} = 2.63 \pm 0.03 \text{ keV}$
  - Ar VI-IX:  $E_{\text{ref}} = 2.9661 \text{ keV} \rightarrow E_{\text{pf}} = 2.98 \pm 0.02 \text{ keV}$

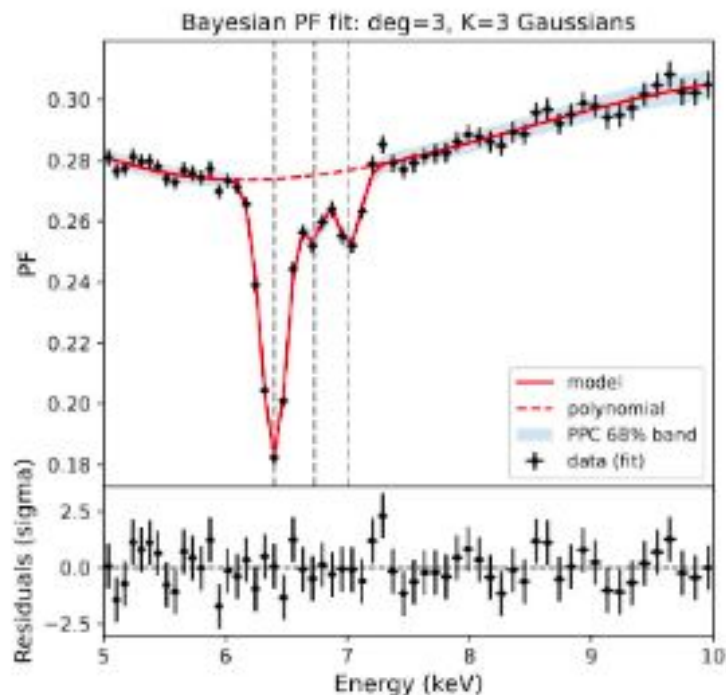


# Energy range: 5 - 10 keV: EPIC-pn data / Bayesian fitting

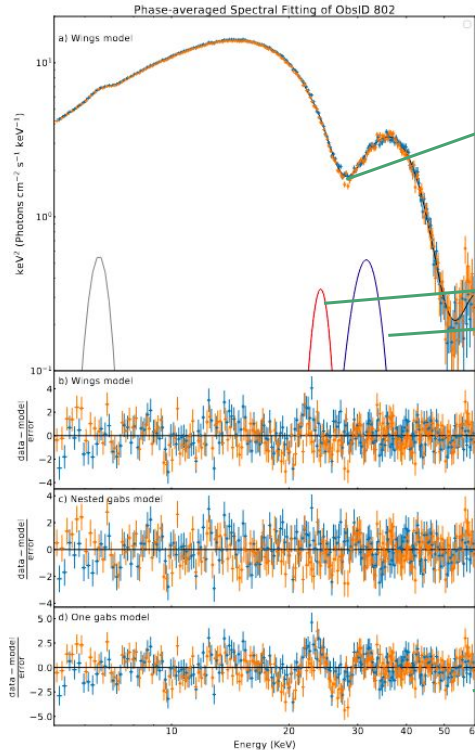
We use all exposure this time...

There are indications in previous works for the Fe XXV triplet at  $\sim 6.7$  keV (Amato+2021, Diez+2025).

- Fe  $K\alpha$ :  $E_{\text{ref}} = 6.4$  keV  $\rightarrow E_{\text{pf}} = 6.399 \pm 0.005$  keV
- Fe XXV:  $E_{\text{ref}} = 6.7$  keV  $\rightarrow E_{\text{pf}} = 6.73 \pm 0.03$  keV
- Fe  $K\beta$ :  $E_{\text{ref}} = 7.06$  keV  $\rightarrow E_{\text{pf}} = 7.01 \pm 0.02$  keV



# Looking for spectral counterparts



A single broad absorption feature dominates the residuals at the  $E_{\text{cyc}}$

Two emission components at both sides of the cyclotron line

equivalent to a “nested” model of two abs. features of different widths

but significantly better than a single Gaussian in absorption

# What if the line lags behind the continuum?

