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Supervised and unsupervised machine learning for astronomy: some concrete examples from my research

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ML: what is it?



Finding segregated subsystems of stellar-mass black holes in globular clusters



A few BHs in globular clusters were spotted observationally: M22 (Strader et al. 2012); M62 (Chomiuk et al. 2013); 47 Tuc (Miller-Jones et al. 2015; Bahramian et al. 2017) M10 (Shishkovsky et al. 2018); NGC 3201 Giesers et al. (2018)

Globular clusters produce thousands of BH: how many are retained?

They have **dynamical effects** and may merge and produce gravitational waves

Classification problem with

numeric features

- Half-Light Radius
- Central Surface Brightness
- Central Velocity
 Dispersion
- Total Luminosity
- Relaxation Time
- Core Radius

Low-dimensional feature space, observed in actual globular clusters (e.g. Harris 1996), easy to extract from simulations



~ 2000 state-ofthe-art dynamical simulations from MOCCA Survey I (Askar et al. 2017)



Askar, Askar, Pasquato, Giersz 2018 MNRAS 485, 5345

Classification problem



Metrics: precision (orange fishes caught / total caught fishes);

recall (orange fishes caught / total orange fishes); F-score harmonic mean of precision and recall

Simple tree models perform well



Figure 4. Comparison of each classifiers' f-score with 15-fold stratified CV testing. An f-score of 1.0 is the best possible, 0.0 is the worst. The score is affected by how well the classifier can find all the BH subsystems and whether the identifications are false-positives.

Decision tree model

Final prediction (leaf) based on proportion of BH subsystem hosts

Branch split on one structural parameter e.g. core radius > 1.15 pc

More splits on other parameters



Physical interpretation



First few branches of the learned tree

First split is on core radius: black hole subsystem hosts have large cores due to dynamical heating

Second split on total luminosity: big clusters produce more black holes, have higher retention due to higher escape velocity

Comparison with real GCs

NGC 6362*

Table 4. Predictions from the Harris (1996, updated 2010) and Baumgardt & Hilker (2018) datasets using the gradient boosted decision tree classifier. Entires where BHS presence was classified positively are shown. The BHS column represents the classifier trained on all simulation data whereas Fallback represents training on models where mass fallback was enabled and BH natal kicks were lower.

Cluster Name	BHS	Fallback	BHS Fallback	
	(Harris)	(Harris)	(B&H)	(B&H)
IC 4499*	1	1	1	1
NGC 288 *	1	1	1	1
NGC 3201 *	1	1	×	1
NGC 4372 *†	1	1	1	1
NGC 4590 (M68)	×	1	×	×
NGC 4833 *†	×	1	1	1
NGC 5139 (ω Cen)	1	1	×	1
NGC 5272 (M3)*	×	1	1	1
NGC 5286	×	1	×	1
NGC 5466*	×	1	×	×
NGC 5897 *†	1	1	×	1
NGC 5904 (M5)	×	1	1	1
NGC 5927	×	×	1	1
NGC 5986 *†	1	1	×	1
NGC 6101 *†	1	1	×	×
NGC 6139 †	1	1	×	×
NGC 6144 *†	×	1	1	1
NGC 6205 (M13)*	×	1	1	1
NGC 6218 (M12)	1	1	×	×
NGC 6254 (M10)	1	1	1	1
NGC 6266 (M62)	×	×	1	×
NGC 6273 (M19) †	×	1	1	1
NGC 6287 †	1	1	×	×
NGC 6304 †	×	1	1	1
NGC 6316 †	1	1	×	×
NGC 6333 (M9) †	1	1	×	×
NGC 6356 †	×	1	×	1

Green row = predicted BH subsystem host by all models e.g. NGC 288, M10

Results compare well with other methods (Askar et al. 2019 marked with *)

NGC 6380 ⁺
NGC 6288
NGC 0388
NGC 6401 *
NGC 6402 (M14) †
NGC $6426*^{\dagger}$
NGC 6440 †
NGC 6496 *†
NGC 6517 †
NGC 6539 (GCL 85)
NGC 6553
NGC $6569 * \dagger$
NGC 6584 *†
NGC 6656 (M22) *
NGC 6712*
NGC 6723 *†
NGC 6760 †
NGC 6779 (M56)*
NGC 6809 (M55)*
NGC 6934*
NGC 6981 (M72)*
NGC 7078 (M15)
NGC7089 (M2)
Pal11 *†
Terzan5 †

C	•	<i>c</i>	•
1	1	X	×
X	×	1	×
1	1	X	×
1	1	1	1
X	1	X	×
1	1	X	×
X	1	X	×
X	1	X	×
1	1	X	×
1	1	X	×
1	1	1	1
1	1	X	×
1	1	1	1
X	1	1	1
1	1	1	1
1	1	X	×
X	1	1	1
X	1	X	1
1	1	X	×
X	1	X	×
X	×	1	1
X	1	X	1
1	1	1	1
X	1	X	X

Now some unsupervised ML



Points in some highdimensional space

Clustering

Dimensionality reduction

What can we do without labels

- Reduce data-points to fewer representative data-points (finding groups in data; clustering)
 – does k-means ring a bell?
- Reduce coordinates/dimensions to fewer representative coordinates (dimensionality reduction)
 - You all know PCA, right? nonlinear version of it

reduce rows VS reduce columns

Example: chemical tagging

- Field stars may come from disrupted open clusters
- If each OC had distinctive chemistry, we can use abundances as a fingerprint of the parent cluster



Parallel coordinate display of 12 abundances of 330 main sequence stars from GAIA-ESO (Gilmore et al. 2012). Stars selected in real open cluster fields (courtesy A. Bragaglia), parent open cluster color-coded; can we recover them?

12D -> 2D

- If we could represent this 12D space on a plane...
- PCA and keep the first two components? Nah...



- If we could represent this 12D space on a plane...
- PCA and keep the first two components? Nah...



t-SNE

- Local (short) distances matter more than long distances
- Place points in the plane to minimize a loss function that keeps nearby points nearby

$$p_{j|i} = \frac{\exp(-\|\mathbf{x}_i - \mathbf{x}_j\|^2 / 2\sigma_i^2)}{\sum_{k \neq i} \exp(-\|\mathbf{x}_i - \mathbf{x}_k\|^2 / 2\sigma_i^2)} \quad p_{ij} = \frac{p_{j|i} + p_{i|j}}{2N} \quad \text{Similarity in high dimension}$$

$$p_{ij} \quad p_{ij} \quad q_{ij} = \frac{(1 + \|\mathbf{y}_i - \mathbf{y}_j\|^2)^{-1}}{\sum_{k \neq l} (1 + \|\mathbf{y}_k - \mathbf{y}_l\|^2)^{-1}} \quad \text{Similarity in low dimension}$$

$$KL(P\|Q) = \sum_{i \neq j} p_{ij} \log \frac{p_{ij}}{q_{ij}} \quad \text{Small } p_{ij} \quad \text{(faraway points)} \quad \text{do not affect the loss}$$

Dimensionality reduction



12 dimensional space represented on the plane with t-SNE

Learning the spectral index of turbulence of simulated molecular clouds from projected density maps

- Turbulence in molecular clouds modulates star formation, physics still not fully understood (Elmegreen & Scalo 2004, Hennebelle & Falgarone 2012)
- Velocity power spectrum of turbulence can be measured directly through e.g. line-of-sight velocity (Koch 2019)

Question

- Can we measure the turbulence index of simulated turbulent gas from density maps?
- In particular discriminate between Kolmogorov $P_v(k) = k^{-11/3}$ and Burgers $P_v(k) = k^{-4}$ spectra



Simulations

- 1000 simulations of turbulent gas with RAMSES2 [Teyssier 2002] AMR code
- 10x10x10 pc box, initially uniform density gas (6.77×10⁻²²g/cm³), total mass of 10⁴M_{sun}.
- Gas kept isothermal at temperature T=10K
- Injected a divergence free, turbulent, supersonic (Mach 1.41) velocity field with spectrum index n=11/3 or 4
- Evolved for 0.5 Myr, solving Euler's equation with a Lax-Friedrichs Riemann Solver, periodic boundaries without self-gravity and magnetic fields

Train/test/holdout split

- 500 sims w. Kolmogorov index, 500 w. Burgers
- 400+400 build the train set -> 3 projections (x,y,z)
 X 4 flip/flop X 4-way cut = 38400 training images
- 50+50 in the test set = 4800 test images
- 50+50 never looked at (holdout set) = 4800 images



Images

- 250x250 pixels, grayscale; each image corresponds to ¼ of the box, seen in projection along an axis (x,y,z)
- Luminosity encodes log column density





Kolmogorov

Burgers

Deep learning setup

- Keras on top of Tensorflow on workstation with a Titan V GPU
- Four convolutional layers (with max pooling) + three dense layers, RELU act.
- Dropout regularization



Performance on holdout set

	Predicted Kolmogorov	Predicted Burgers	
Kolmogorov	2113	287	
Burgers	812	1588	



Testing on different indices



We ran 1000 more simulations with turbulence index that ranges continously from 3 (left) to 4.5 (right). What will the net predict?

Predictions



Turbulence index



Back to classification: expensive labels

• Human-labeled data + training → classification



Example: galaxy zoo / zooniverse:

morphological classification of galaxies

Other example: finding jellyfish galaxies in TNG Yun et al. 2019, Yun et al in prep.

Few labels, costly to label data

- Active learning: the program chooses which data to learn from
- So you need less hand-labeled data
- Data is labeled where most needed



An active learning toy example

- A particle moves in a 1-D potential + noise
- Initial conditions x₀, x₀', evolved for time t
- Train a ML model to predict x = x(x₀, x₀', t)



The model learns `physics'

• The model is trained only on couples

 (x_0, x_0', t) ; x and never gets any direct information on the potential

- Why do this? We already have enough students to teach physics to...
- The point is: which model will learn faster (i.e. require less training data):
 - one that picks its own samples (active learner)
 - one that trains on random samples (passive learner)

Active learning VS passive learning



Number of simulations run

a couple (x_0, x_0', t) ; x is one 'simulation'

passive learner receives 1000 couples with (x_0, x_0', t) chosen at random and x calculated

active learner chooses the initial conditions (x_0, x_0', t) on which it has more doubts, calculates x

ACTIVE LEARNER REACHES THE SAME ERROR (MSE) AS A PASSIVE LEARNER WITH HALF AS MANY SIMULATIONS

Active learners run informative simulations



How much do you learn about the dynamics by placing a particle at rest at the bottom of the potential well?

Not much...

So the active learner undersamples this region (hole in the donut)

Active learners do not waste labelling effort on uninformative regions of parameter space

How to accomplish this?

How to pick what to study

Two students prepare for an exam together by solving practice tests. They do not know the actual solutions, but they know whether their two solutions match. They study again the topics where the solutions do not match.

- First something at random (e.g. 10 (x₀, x₀', t); x couples)
- On this, train two different models
- Generate a few candidate (x₀, x₀', t) at random
- Predict x_1 and x_2 with the two models
- Query the (x₀, x₀', t) for which the two predictions differ most strongly
- 'Query by committee' there are other schemes as well

Questions?



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