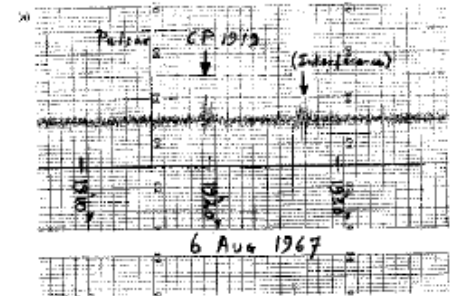
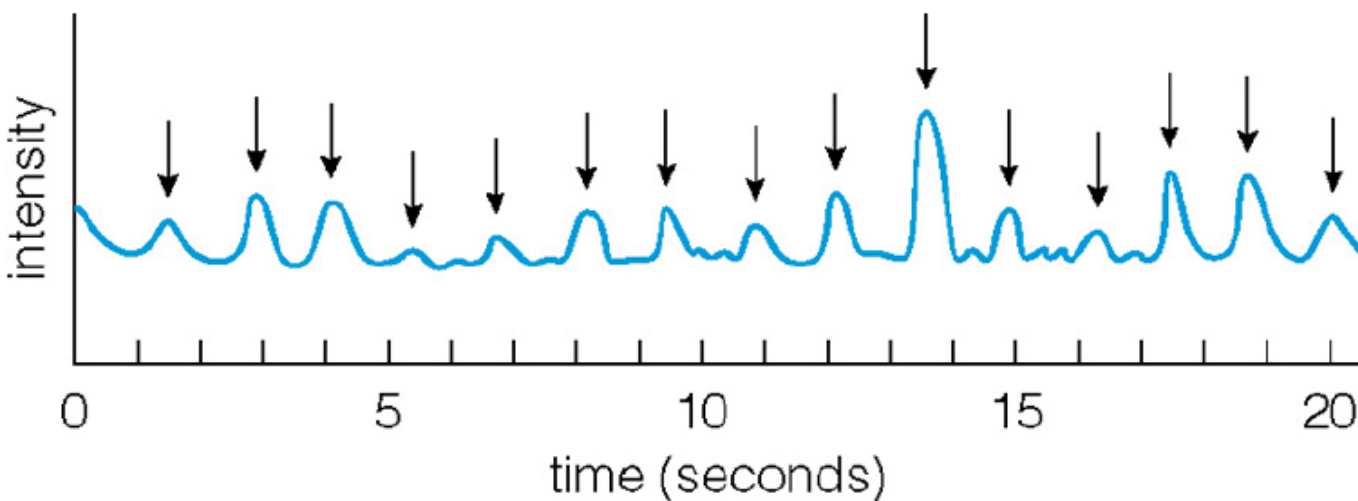


- In 1967, graduate student Jocelyn Bell and her advisor Anthony Hewish accidentally discovered a radio source in *Vulpecula* (**LGM1**).
- Sharp pulse recurred every 1.3 sec.
- Determined it was 300 pc away.
- They called it a “**pulsar**”, but what was it?

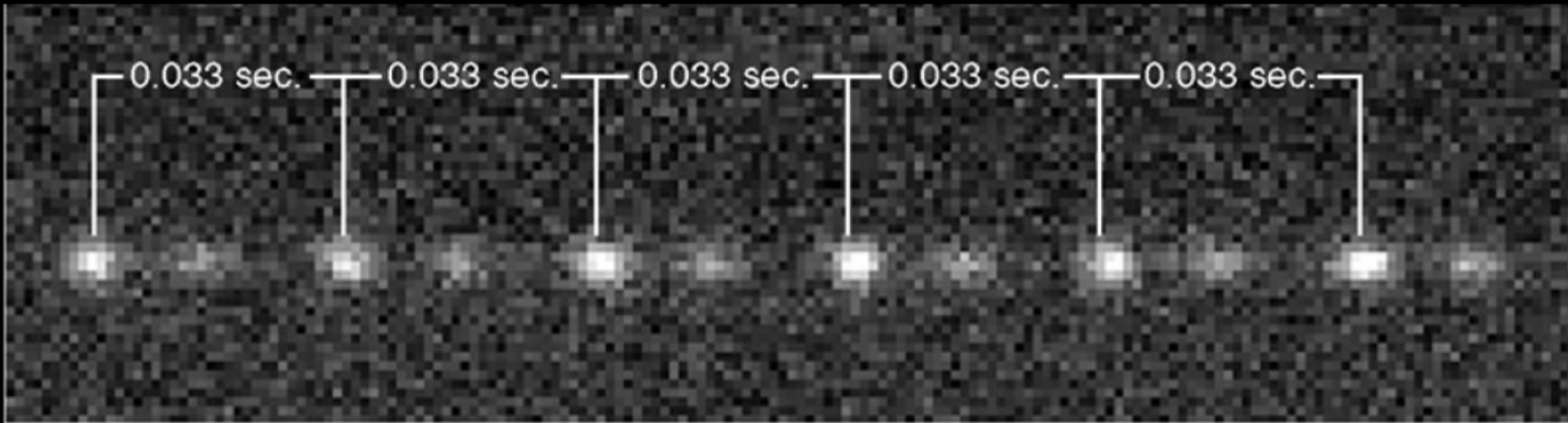


# The Crab Pulsar

The mystery was solved when a pulsar was discovered in the heart of the Crab Nebula.



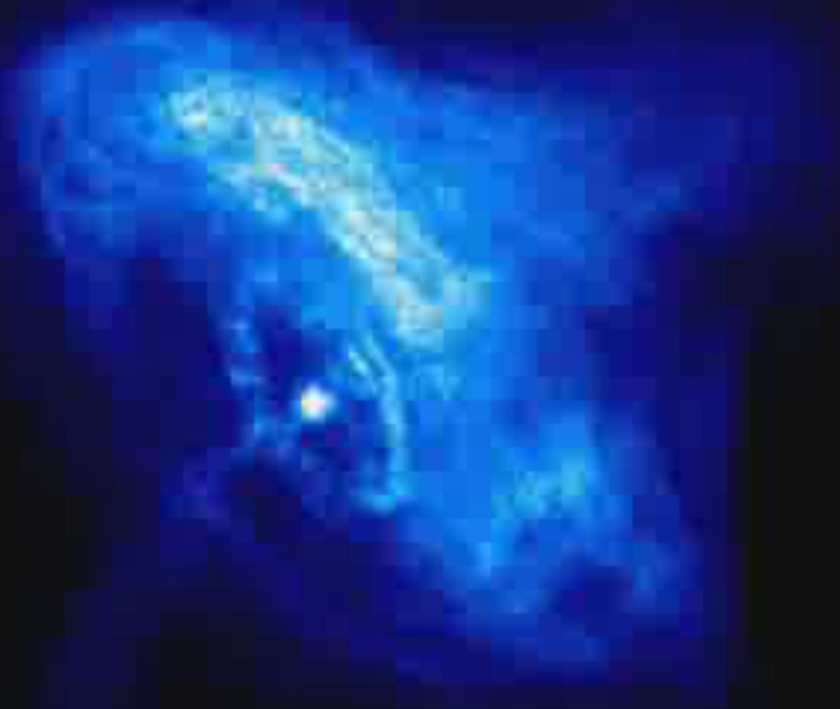
The Crab pulsar also pulses in visual light

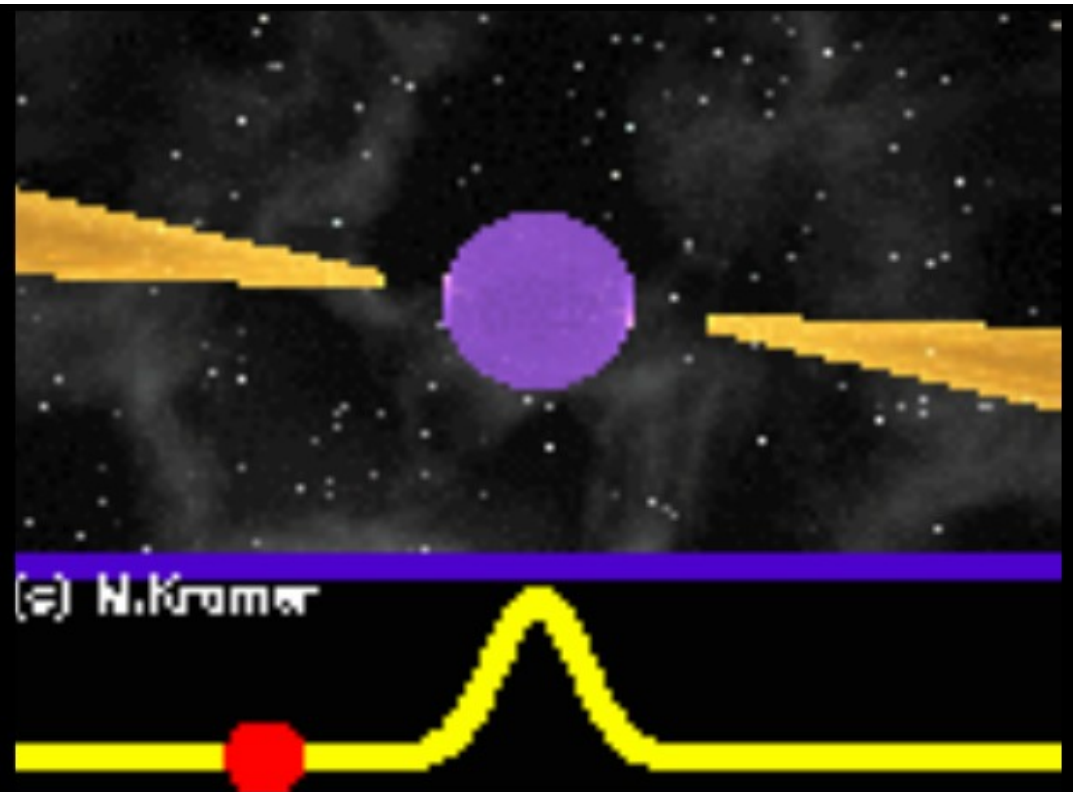


*X-rays*

Crab Nebula

*Infrared*





- PSR 0329+54 (714 ms)
- Vela Pulsar (89 ms)
- PSR 1937-21 (1.5 ms)



Centrifugal acceleration at equator < gravitational acceleration

$$\Omega^2 R < \frac{GM}{R^2} \Rightarrow \frac{4\pi^2}{P^2} < \frac{GM}{R^3} \Rightarrow P > 2\pi \sqrt{\frac{R^3}{GM}}$$

Minimum spin period for:

- Typical WD ( $R=10000$  km,  $M=0.5 M_{\odot}$ )  $P > 24$  s
- The fastest WD ( $R=3000$  km,  $M=1.3 M_{\odot}$ )  $P > 2.5$  s
- Typical NS ( $R=10$  km,  $M=1.4 M_{\odot}$ )  $P > 0.5$  ms

## Theory

Tiny

Mass  $\sim 1.5 M_{\odot}$

Supernova Corpse

Rotating Fast

High magnetic field

## Observations

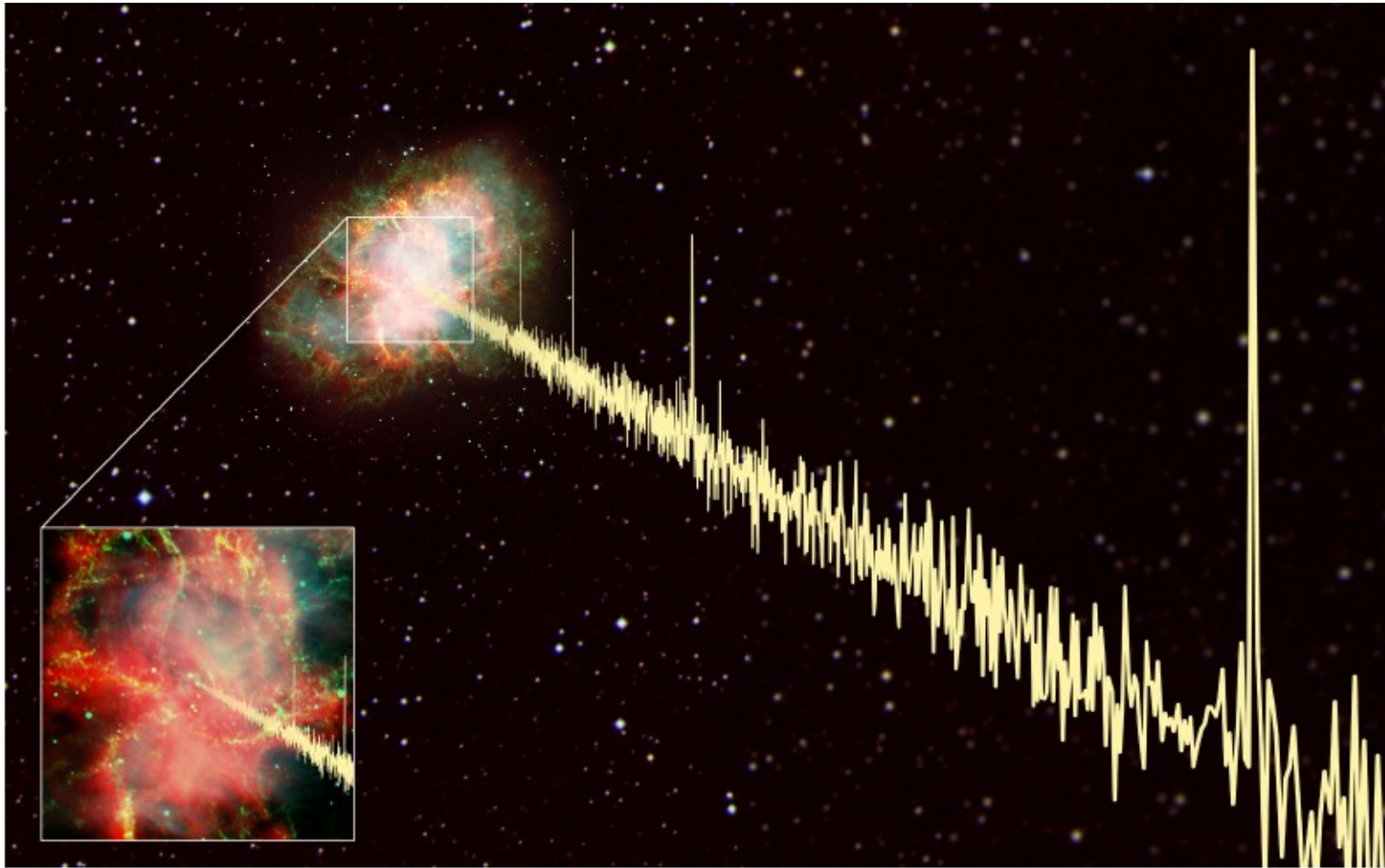
Small Pulse Width

Confirmed in binaries

Seen in SN Remnants

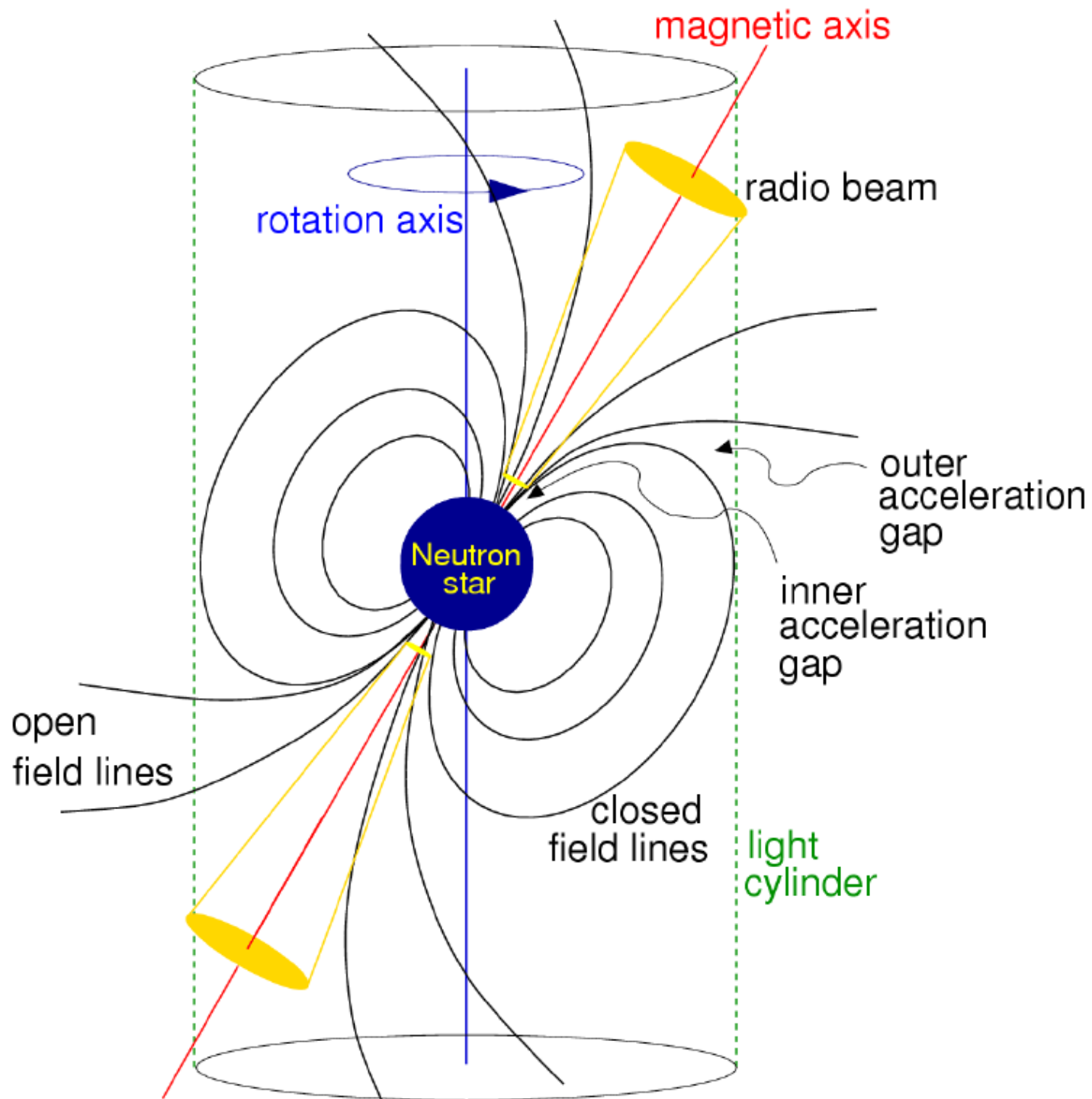
Short Pulse Period

Synchrotron nebula  
and spin-down rate



- Isolated NSs are born as **fast-spinning radio pulsars**
- Pulsars **spin down** because of dipole radiation

From **young, fast and energetic** to **old, slow and faint** pulsars





**Crab:  $P=33$  ms,  $\dot{P}=4.3 \times 10^{-13}$  s s<sup>-1</sup>**

Rotational energy loss:  $\dot{E}_{rot} = \frac{d}{dt} \left( \frac{1}{2} I \omega^2 \right) = I \omega \dot{\omega} = I \frac{4\pi^2}{P} \frac{d}{dt} \left( \frac{1}{P} \right) = -4\pi^2 I \dot{P} P^{-3}$   
 $\Rightarrow \dot{E}_{rot,Crab} \approx 5 \times 10^{38}$  erg s<sup>-1</sup>

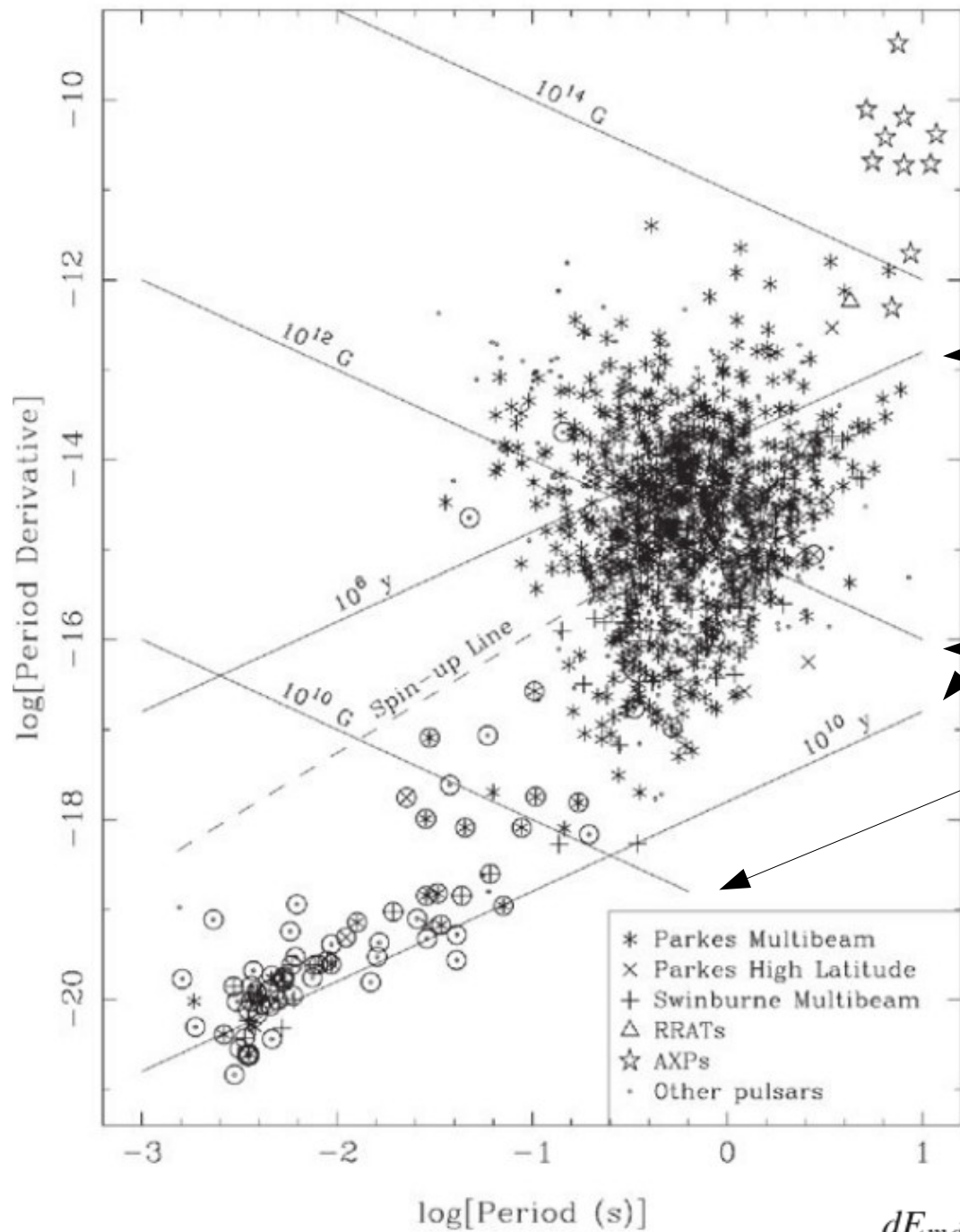
Rotating magnetic dipole in vacuum:  $\dot{E} = -(32\pi^4/3c^3) B_{\perp}^2 R^6 P^{-4}$

$$\Rightarrow B_{\perp} = \sqrt{\frac{3c^3 I P \dot{P}}{8\pi^2 R^6}} \approx 3.2 \times 10^{19} (P \dot{P})^{1/2} \text{ G}$$
$$\Rightarrow B_{Crab} \approx 4 \times 10^{12} \text{ G}$$

Characteristic age:  $\tau = P/2\dot{P}$

Assuming  $B = \text{const}$ :  $P\dot{P} = \text{const}$

$$P\dot{P} = P \frac{dP}{dt} \Rightarrow \int_0^{\tau} P dP = \int_0^{\tau} P \dot{P} dt \Rightarrow \frac{1}{2} (P^2 - P_0^2) = P \dot{P} \tau \Rightarrow \tau \approx \frac{P}{2\dot{P}} \text{ if } P_0 \ll P$$
$$\Rightarrow \tau_{Crab} \approx 1218 \text{ yrs} \approx 2014 - 1054 = 960 \text{ yrs}$$



$$\tau = P/2\dot{P},$$

$$B_{NS} \propto \sqrt{P\dot{P}}.$$

$$-\frac{dE_{rot}}{dt} = \frac{d}{dt} \left( \frac{1}{2} I \Omega^2 \right) = \frac{4\pi^2}{P^3} I \dot{P},$$

$$-\frac{dE_{md}}{dt} = \frac{B^2(R_{LC})}{8\pi} (4\pi R_{LC}^2 c) = \frac{1}{2} B_{NS}^2 \left( \frac{R_{NS}^6}{R_{LC}^4} \right) c \propto \frac{B_{NS}^2}{P^4}.$$

- **Rotating Radio Transients (RRaTs):** discovered in 2006 as isolated radio pulses. But pulse separations are not random: regularly slowing down periods  $\Rightarrow$  “intermittent” radio pulsars
- **Radio-quiet gamma-ray pulsars:** only one (*Geminga*) known before 2008. Tens discovered by *Fermi* gamma-ray satellite. Why not detected in radio?

Emission beam much broader in gamma than in radio

# Egret Pulsars

**Table 3**  $\gamma$ -ray fluxes of EGRET pulsars [17, 44, 70]

Pulsar	Period (ms) $P$	Age (kyr) $P/2\dot{P}$	EGRET $F_{-8}$	Pulsar catalog $F_{-8}$	2FGL $F(1-100\text{ GeV})^a$
0833-45, Vela	89.3	11.3	$834.3 \pm 11.2$	$1061 \pm 7.0$	$135.8 \pm 0.4$
J0633+1746, Geminga	237	340	$352.9 \pm 5.7$	$305.3 \pm 3.5$	$72.9 \pm 0.3$
0531+21, <sup>b</sup> Crab	33	1.25	$226.2 \pm 11.2$	$209 \pm 4$	$18.3 \pm 0.15$
1706-44	102	17.6	$111.2 \pm 6.2$	$149.8 \pm 4.1$	$19.1 \pm 1.7$
1055-52	197	540	$33.3 \pm 3.82$	$30.45 \pm 1.7$	$5.0 \pm 0.09$
1951+32 <sup>c</sup>	39.5	110	$16 \pm 2$	$17.6 \pm 1.9$	$2.1 \pm 0.07$
1509-58, <sup>c</sup> Circinus	88.9	150	–	$8.7 \pm 1.4$	$1.45 \pm 0.08$

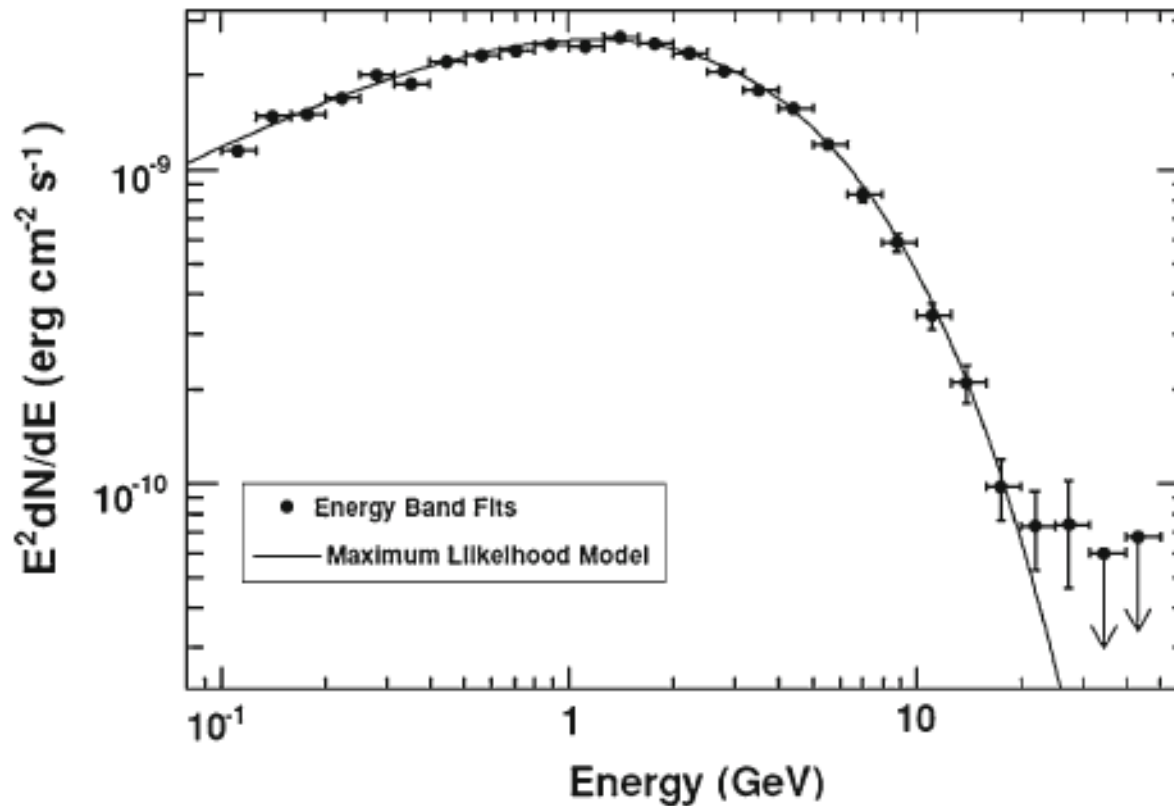
<sup>a</sup>Also in units of  $10^{-8} \text{ ph cm}^{-2} \text{ s}^{-1}$

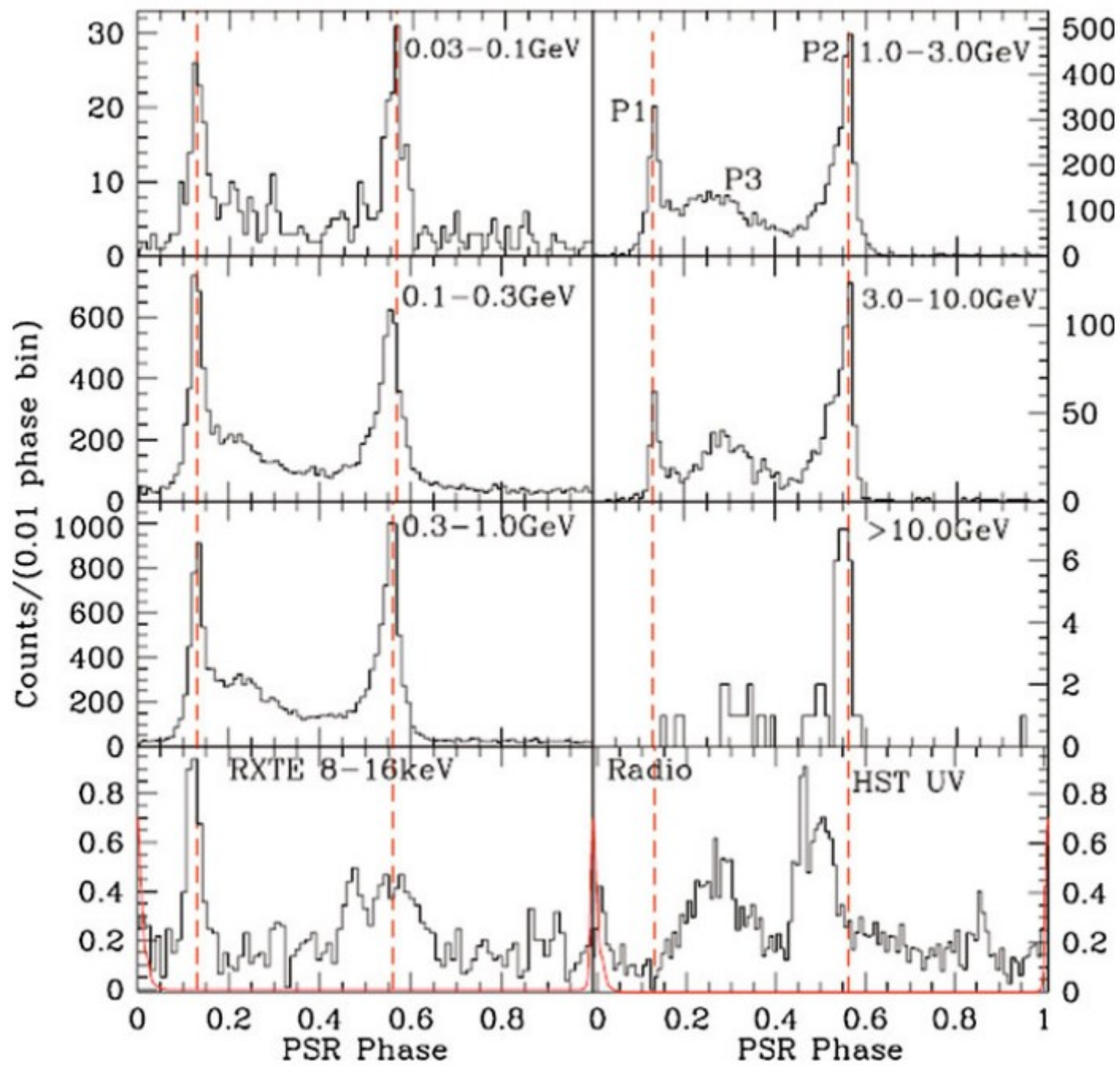
<sup>b</sup>Associated with SN 1054

<sup>c</sup>Pulsars not reported in the 3EG [71]

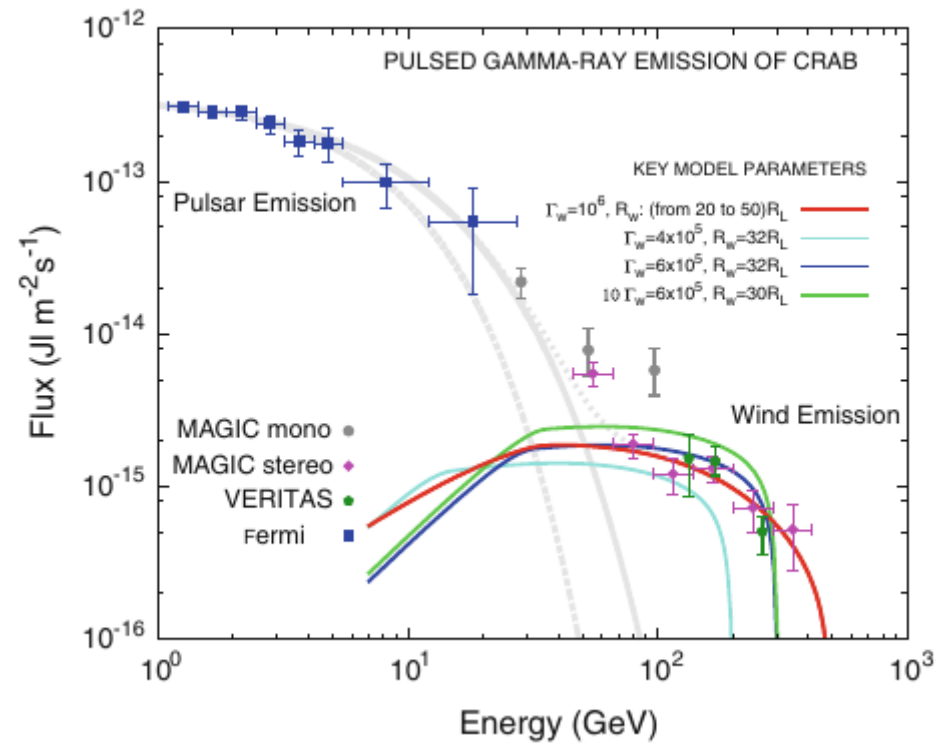
# Gamma-ray spectrum

$$N(E) \propto E^{-\Gamma_\gamma} \exp[-(E/E_c)^b],$$

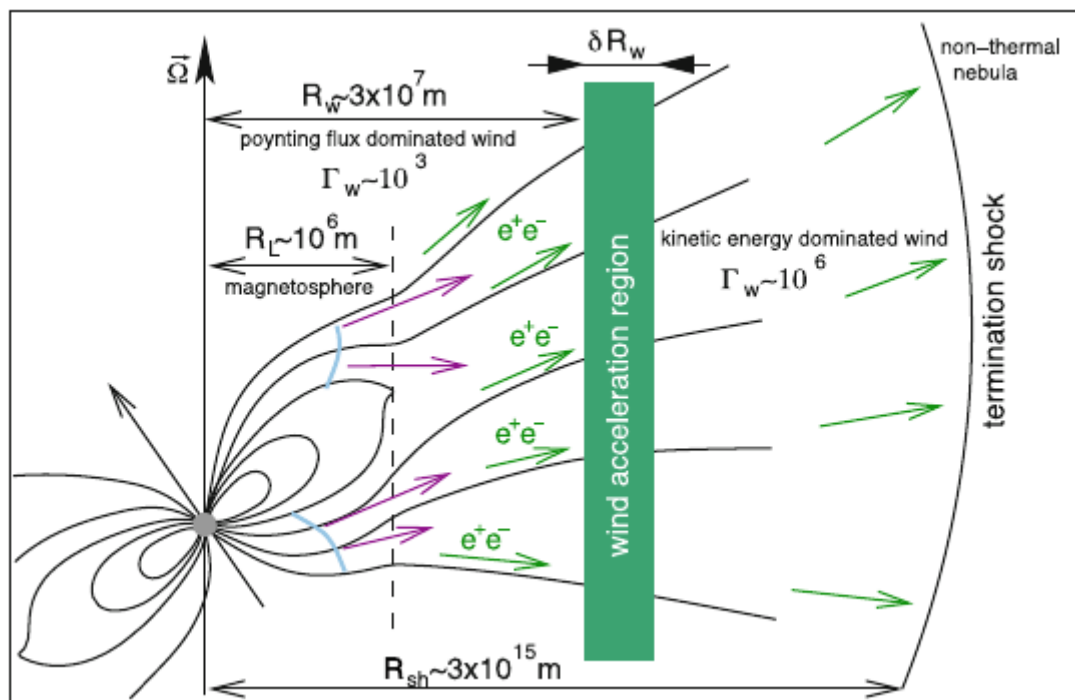




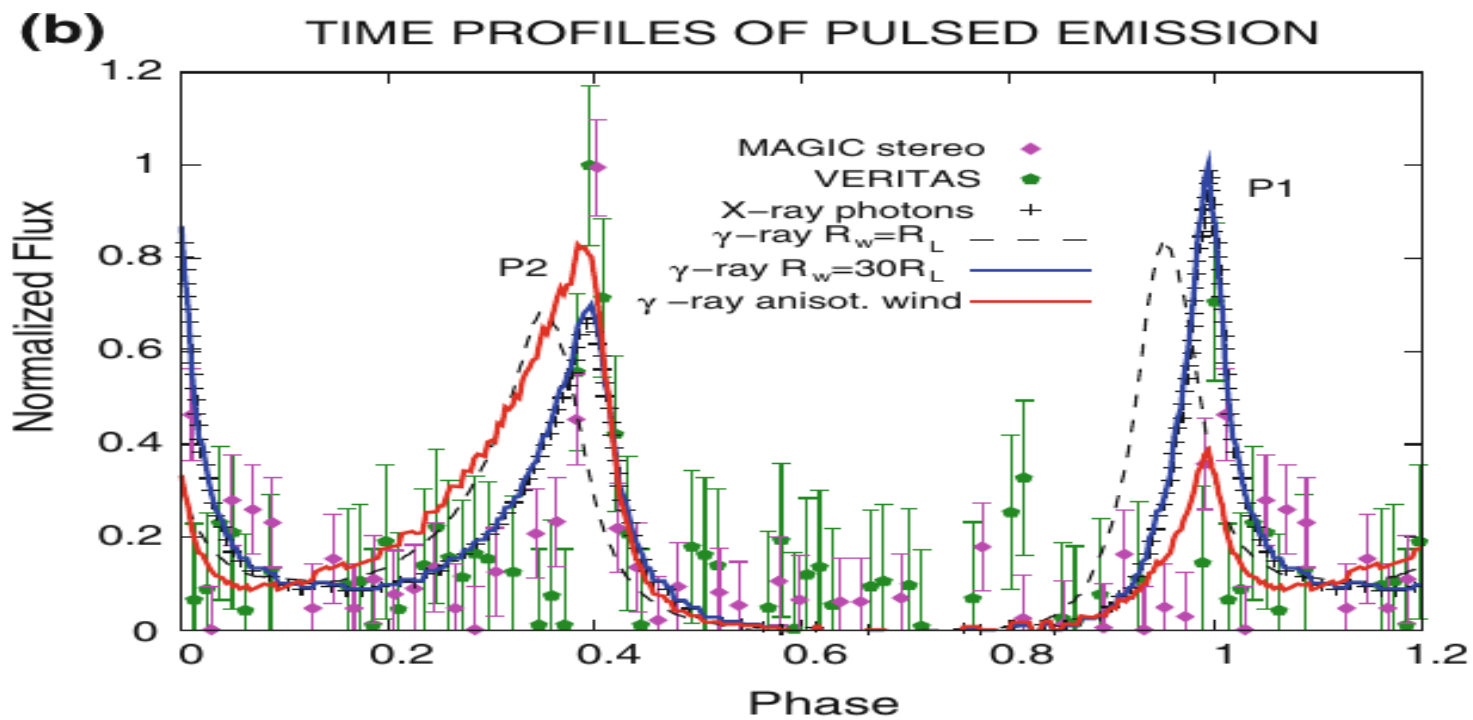
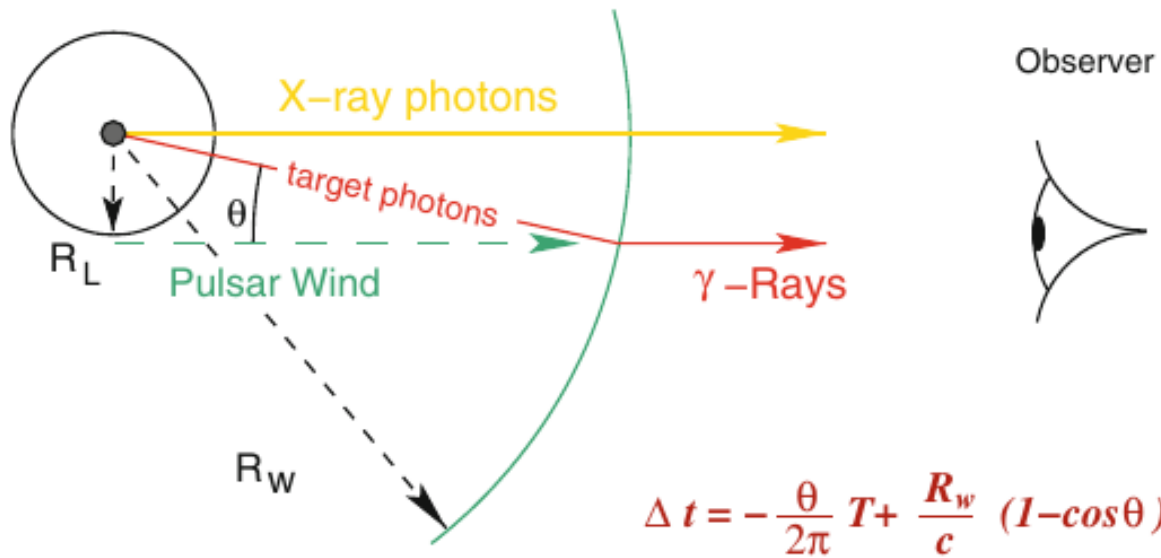
# Crab Pulsed SED



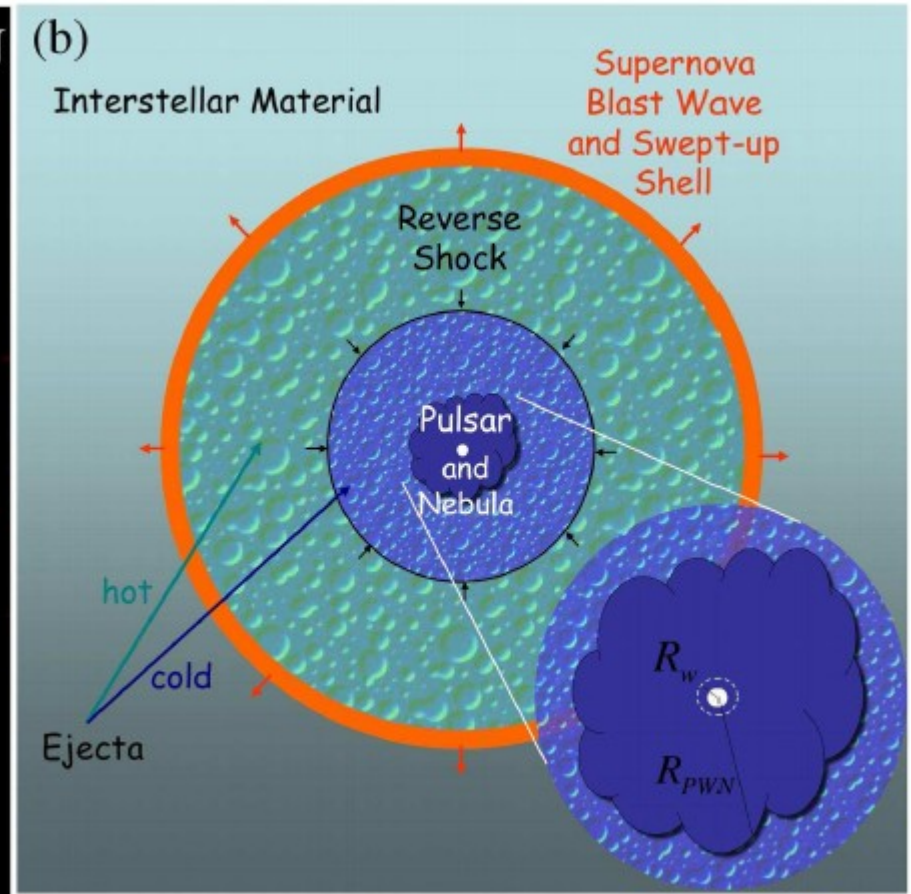
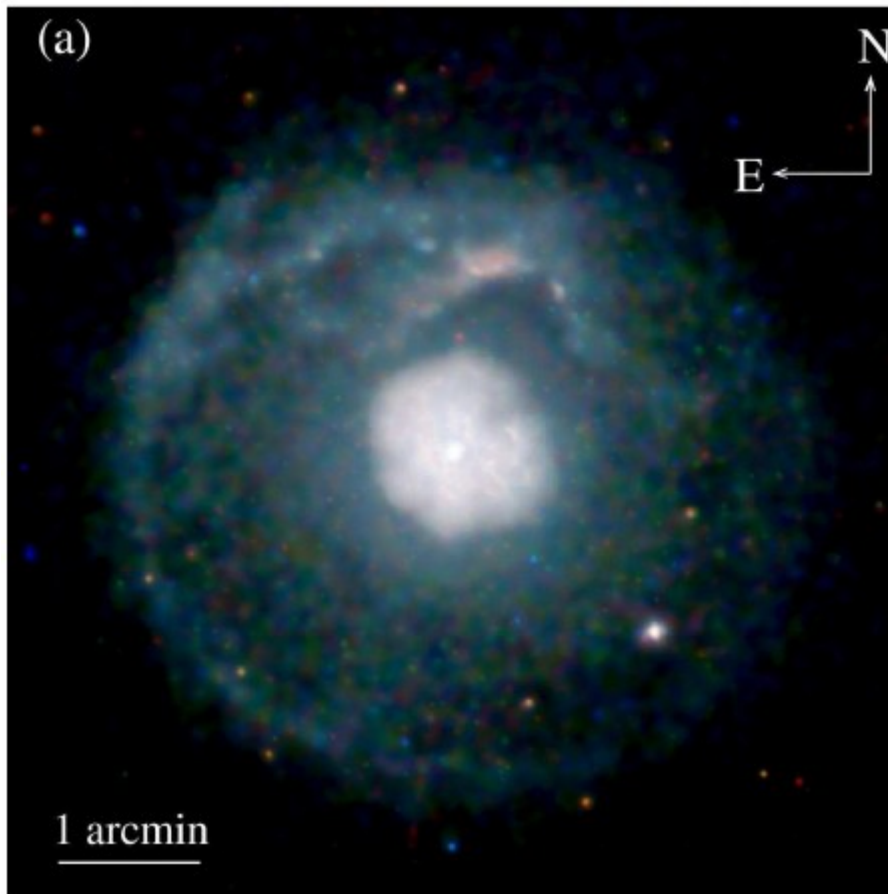
# Pulsar Wind

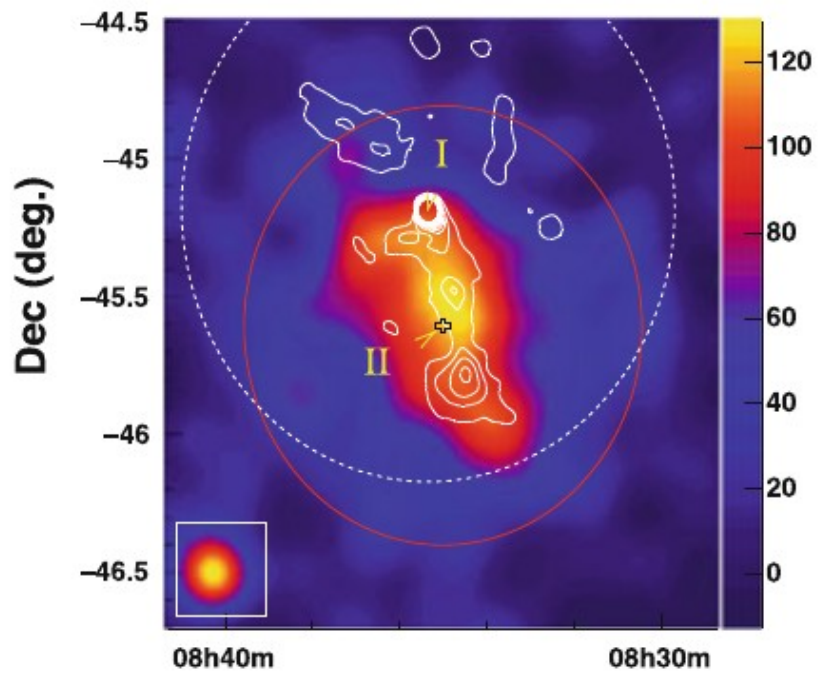




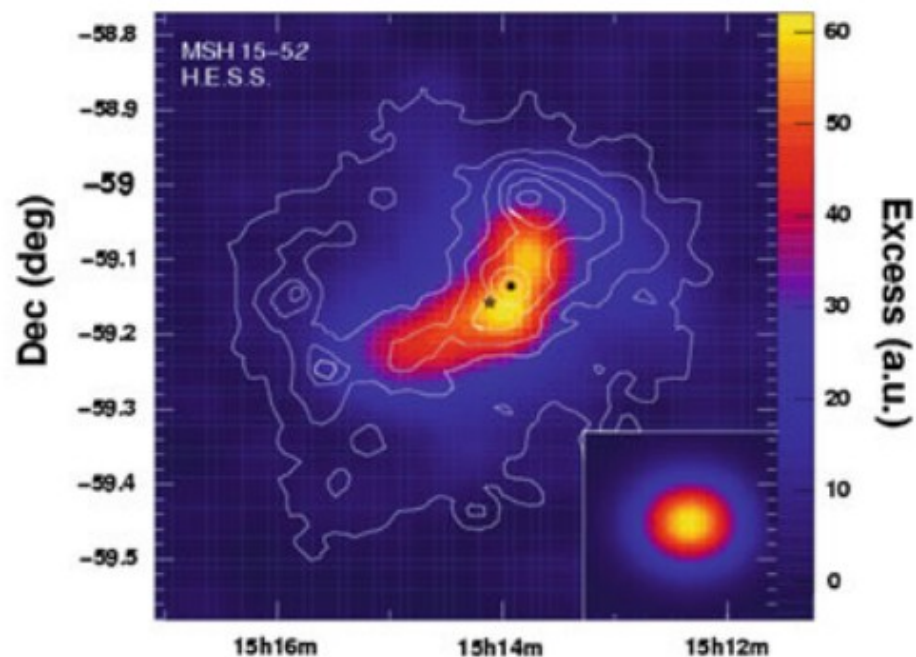


# Pulsar Wind Nebulae

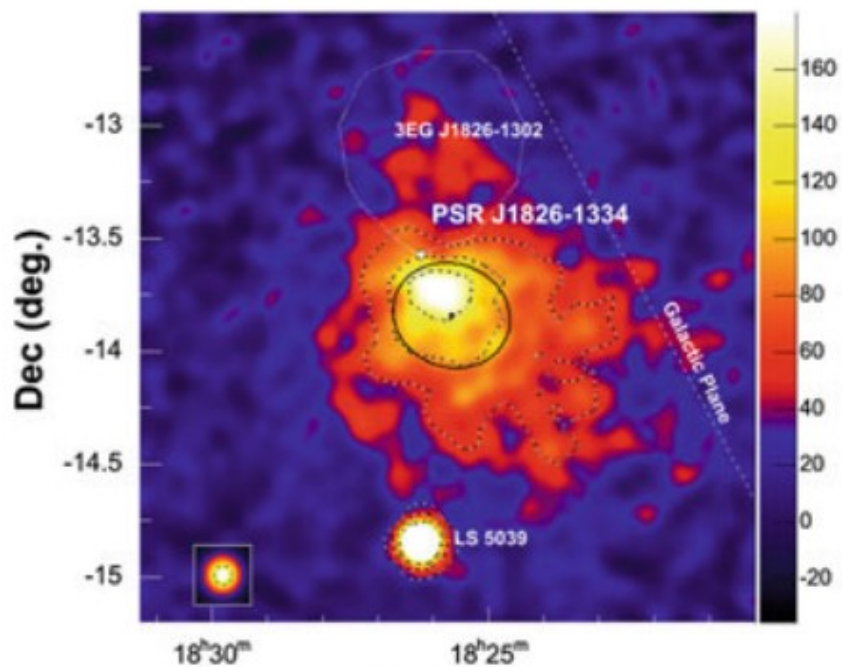




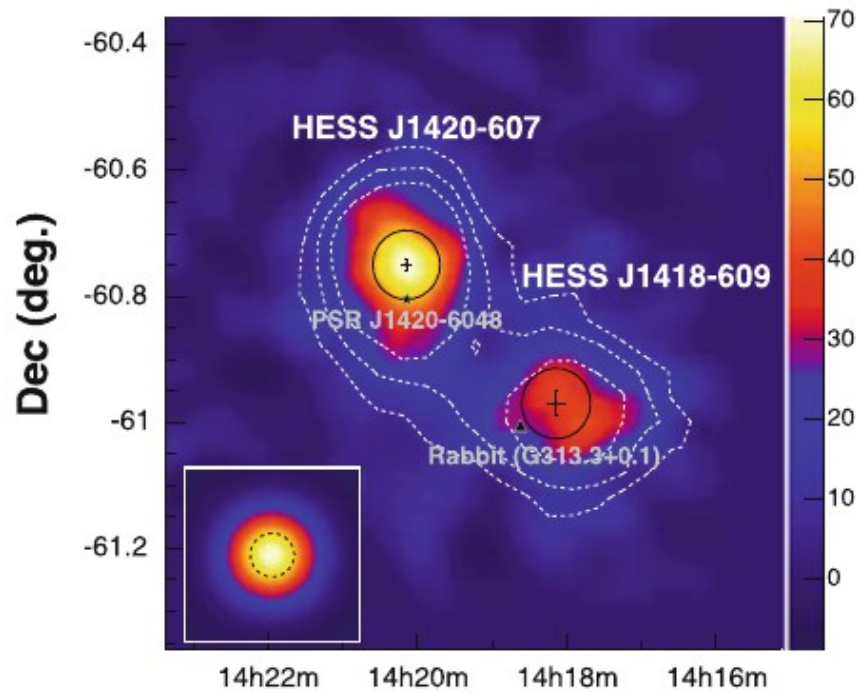
RA (hours)



RA (hours)

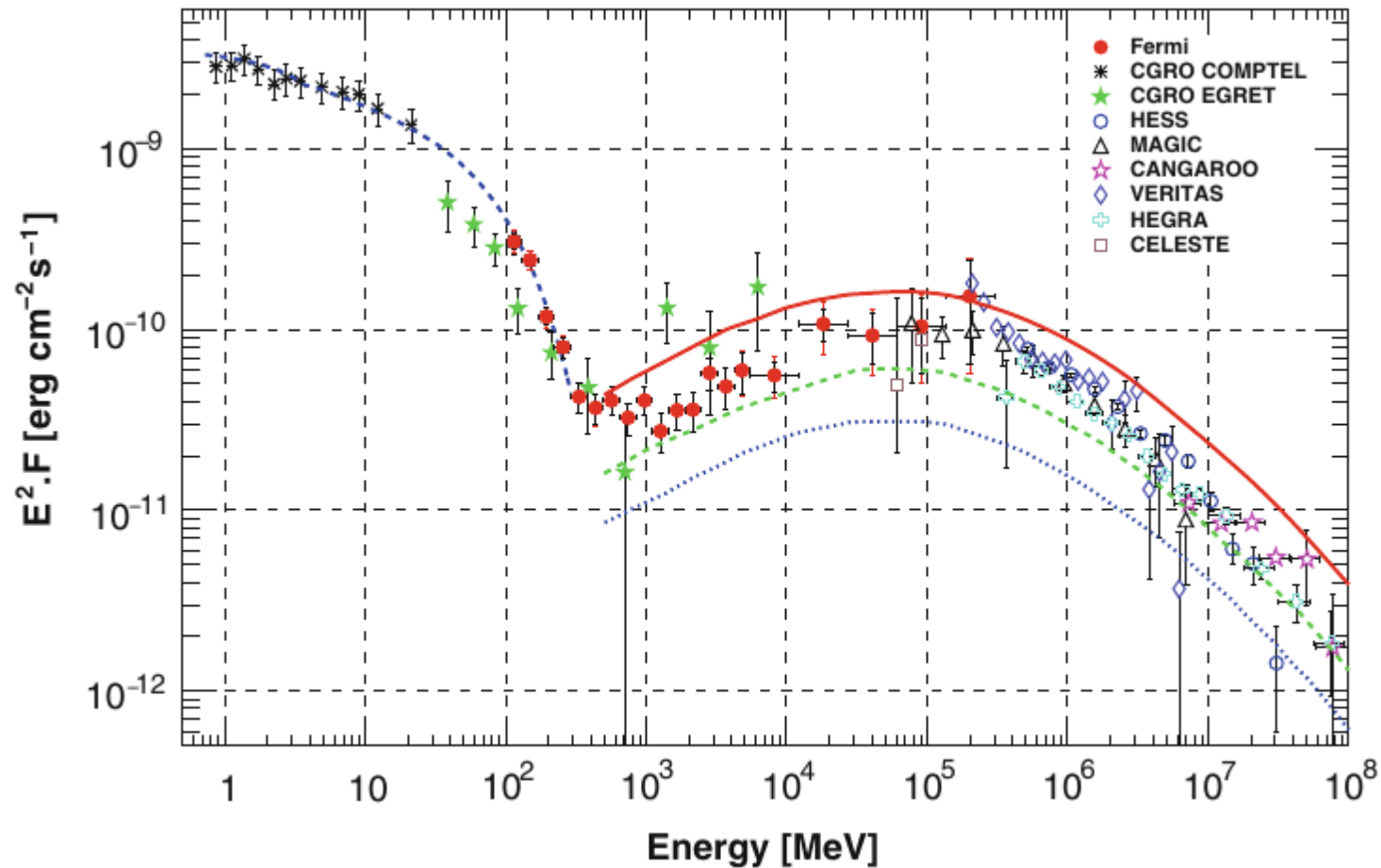


RA J2000 (hours)

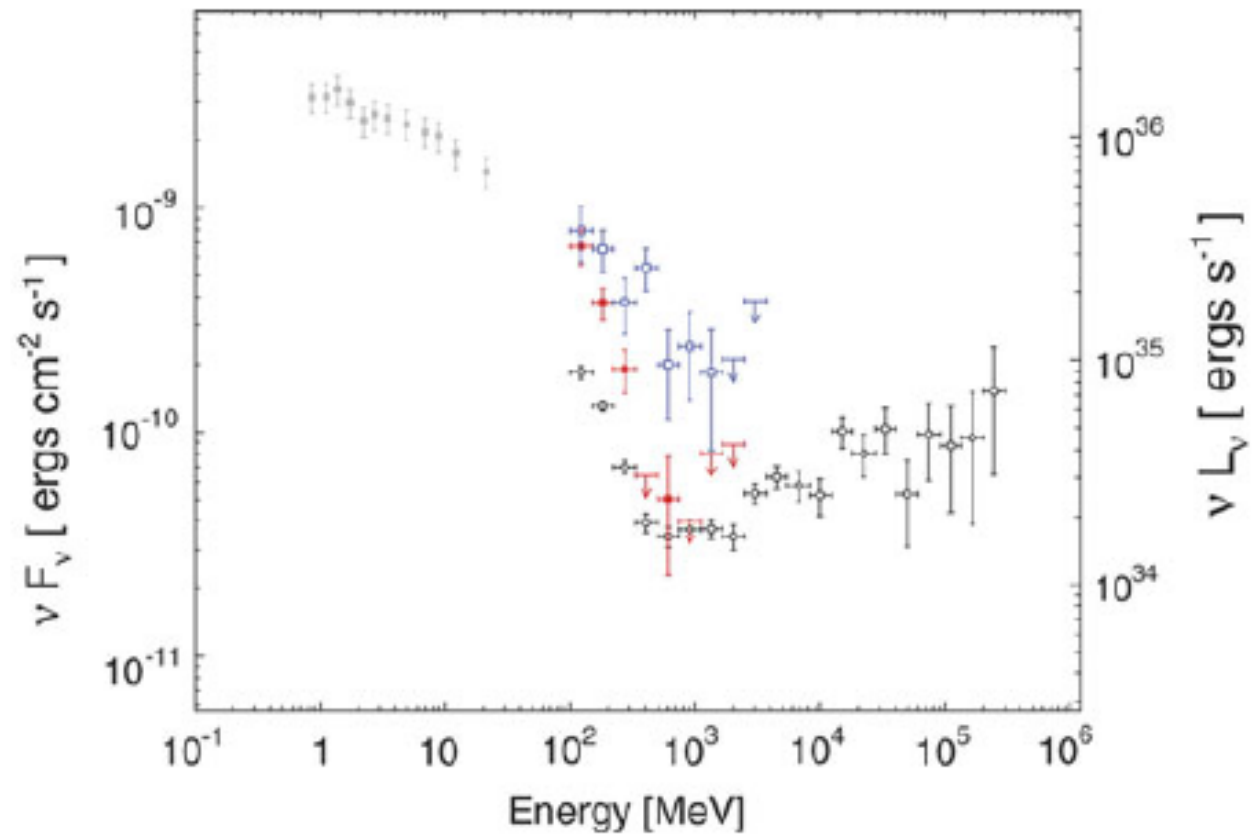


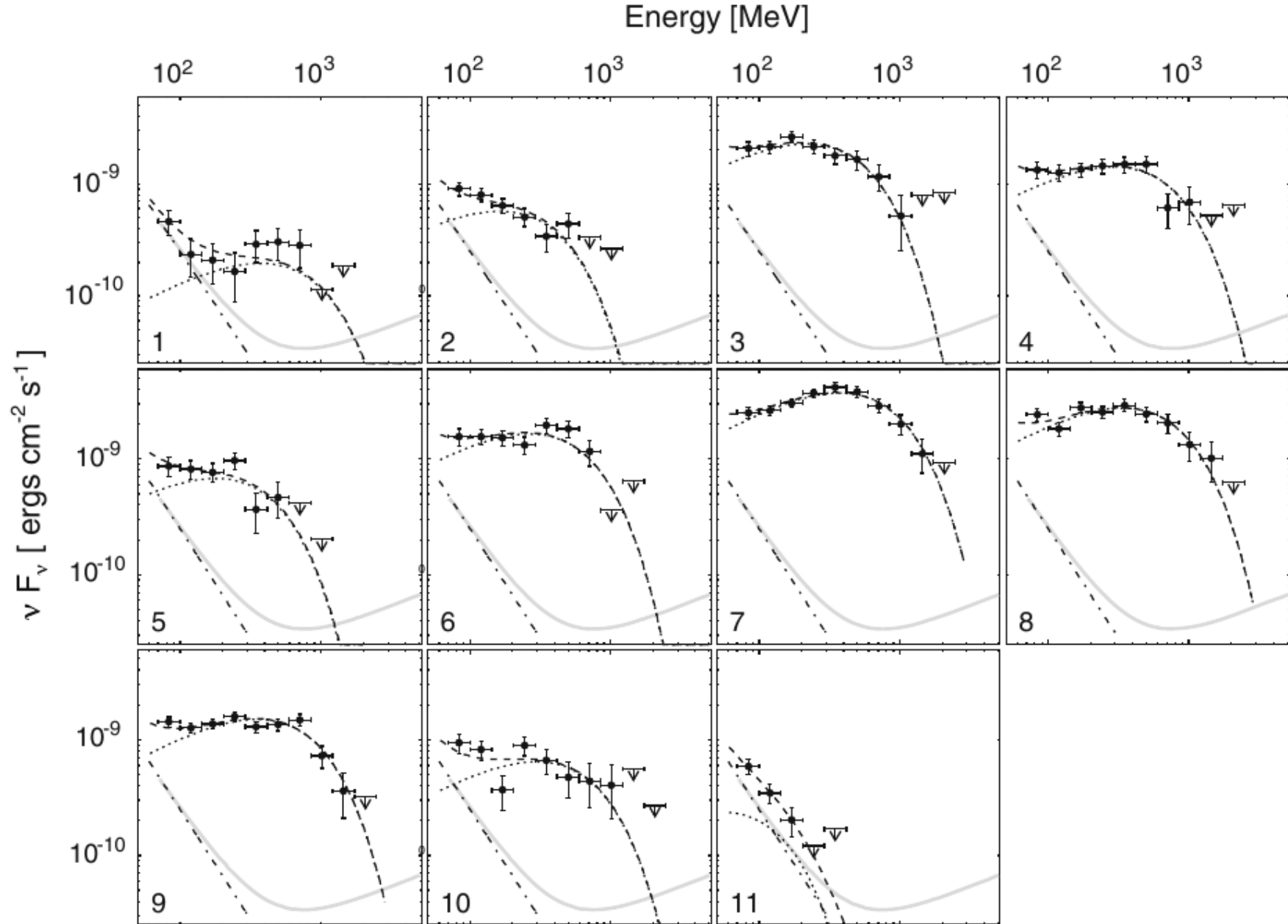
RA (hours)

# Crab PWN SED

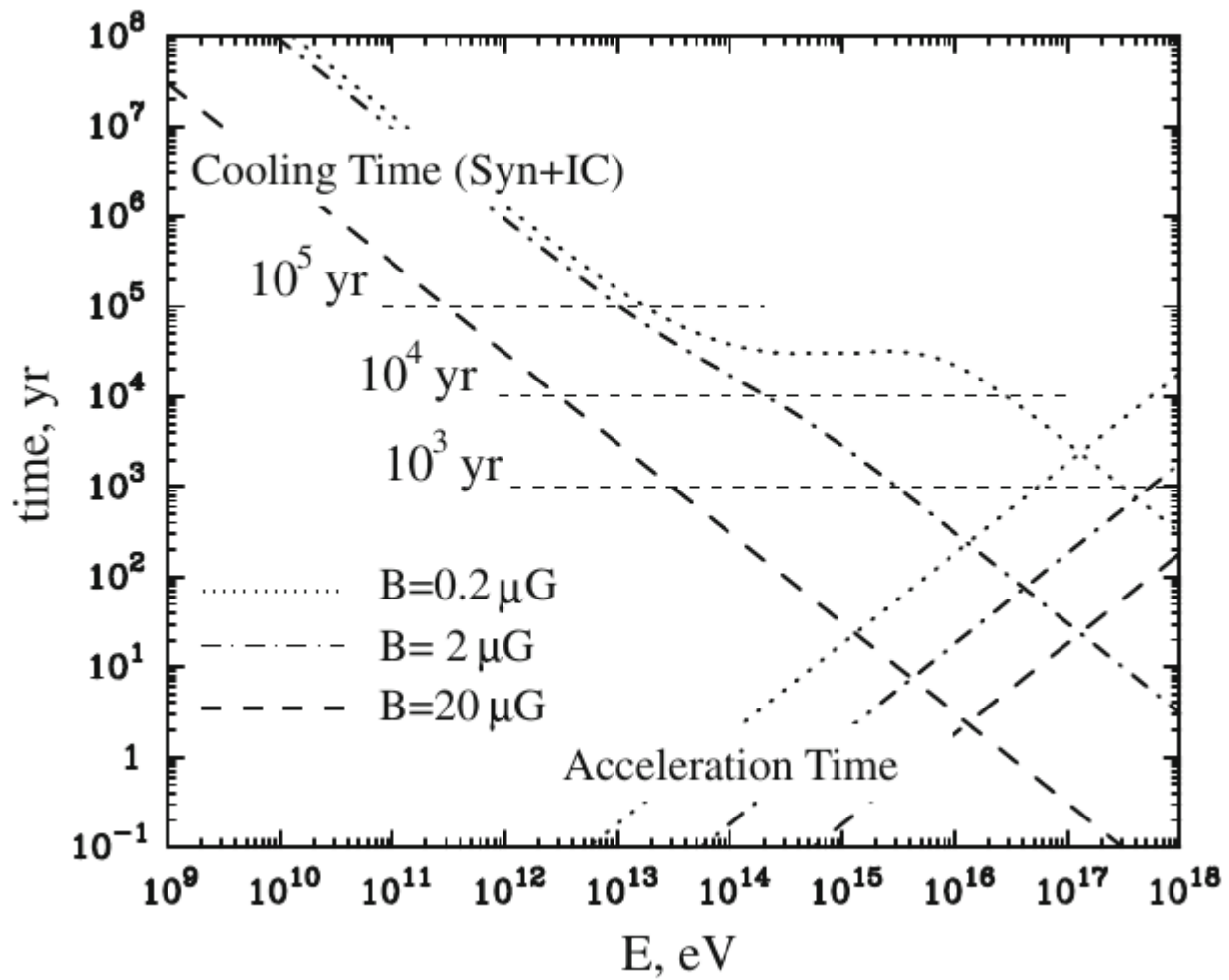


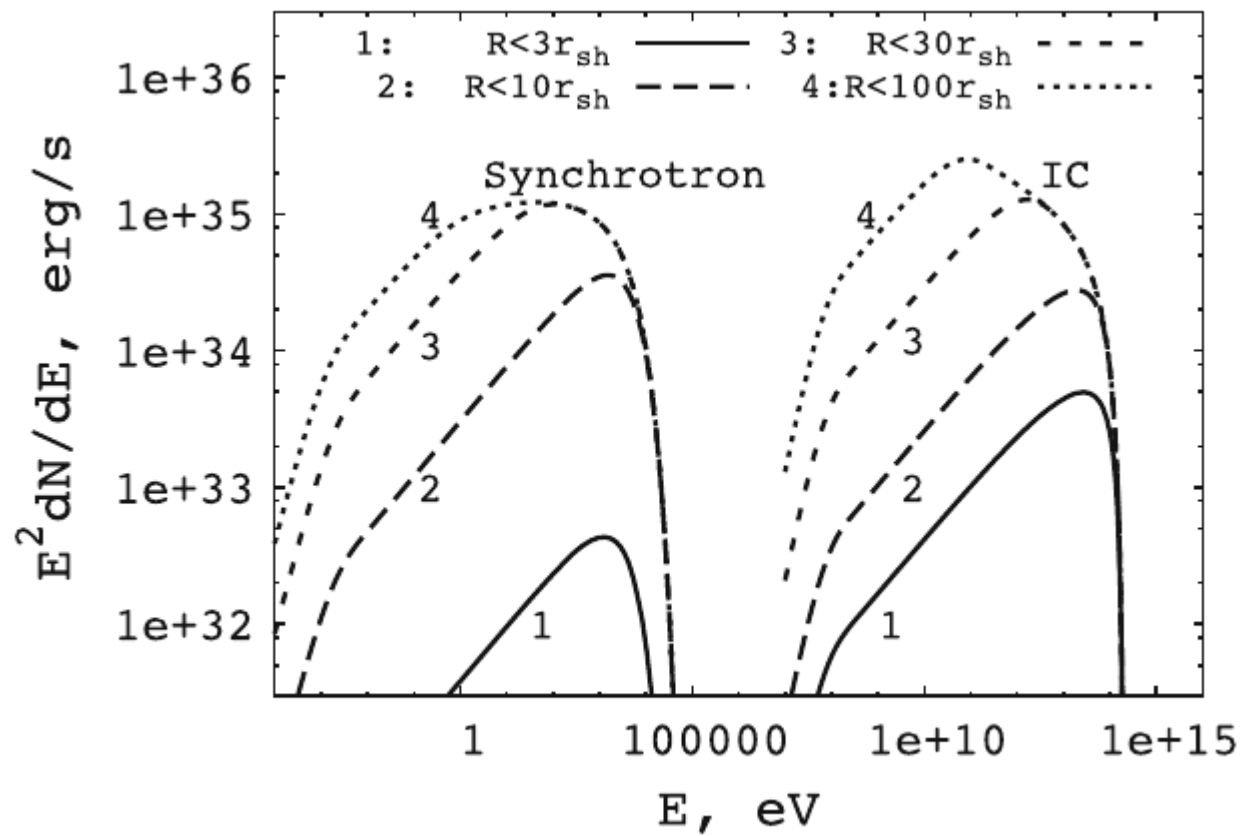
# Crab Flares



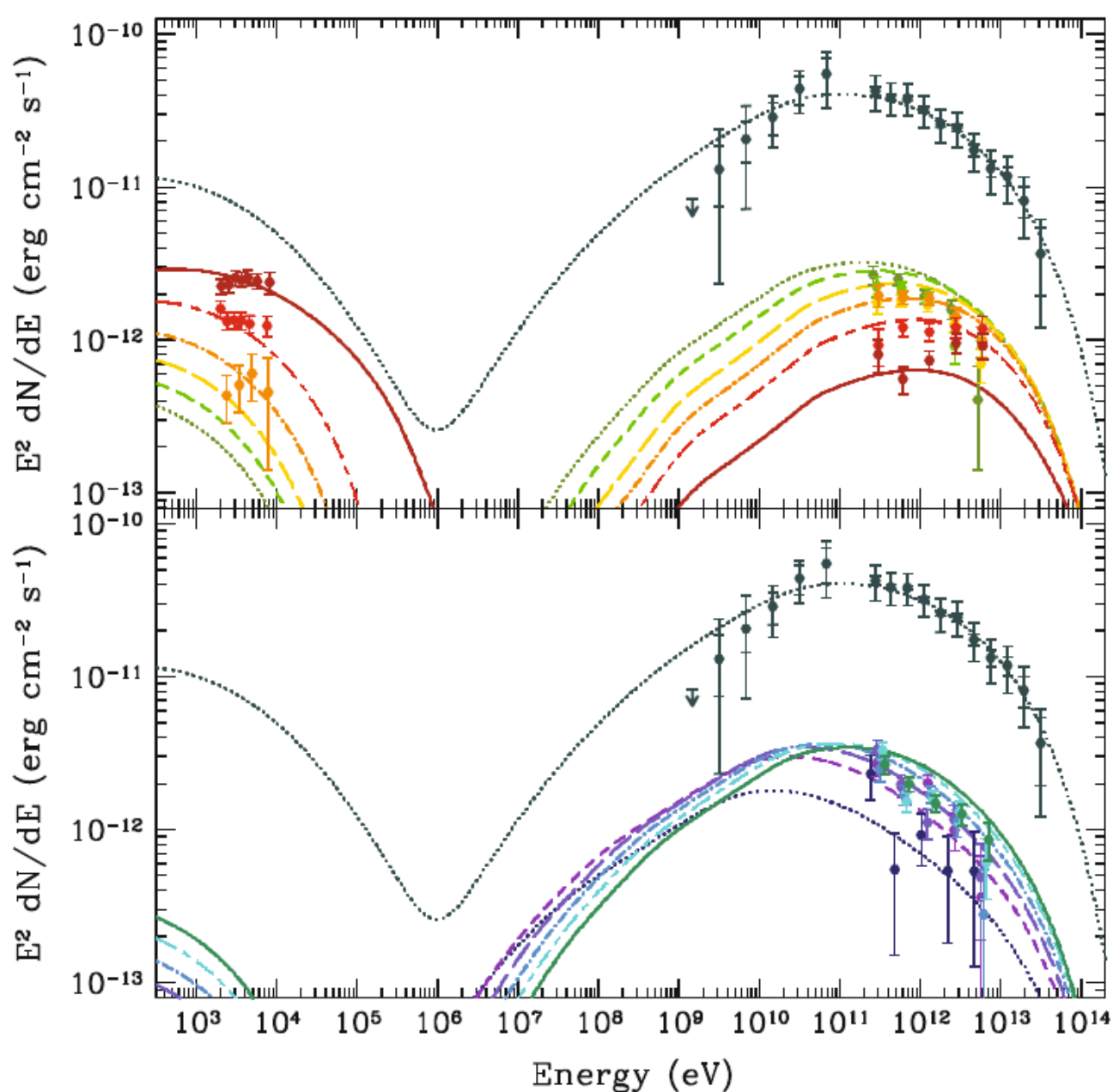


**Fig. 41** Time evolution of the Crab SED during the April 2011 flare. The flare duration of approximately 9 days has been divided in 11 time windows of approximately constant flux. The *dot-dashed line* indicates the assumed constant background from the synchrotron nebula. The *dotted lines* show the flaring component, and the *dashed lines* are the sums of the background and flaring components (from Ref. [110])









**Fig. 48** SED of broad-band IC gamma-ray emission of the pulsar wind nebula HESS J1825-137 calculated for 12 zones with a constant 6 arcmin width of the zones:  $0' - 6'$ ,  $6' - 12'$ , ...  $66' - 72'$ . The *theoretical curves* are shown together with observational points obtained with the *Suzaku* (the inner 6 zones), *Fermi LAT* (the entire nebula), and HESS (all 12 zones) telescopes [242]