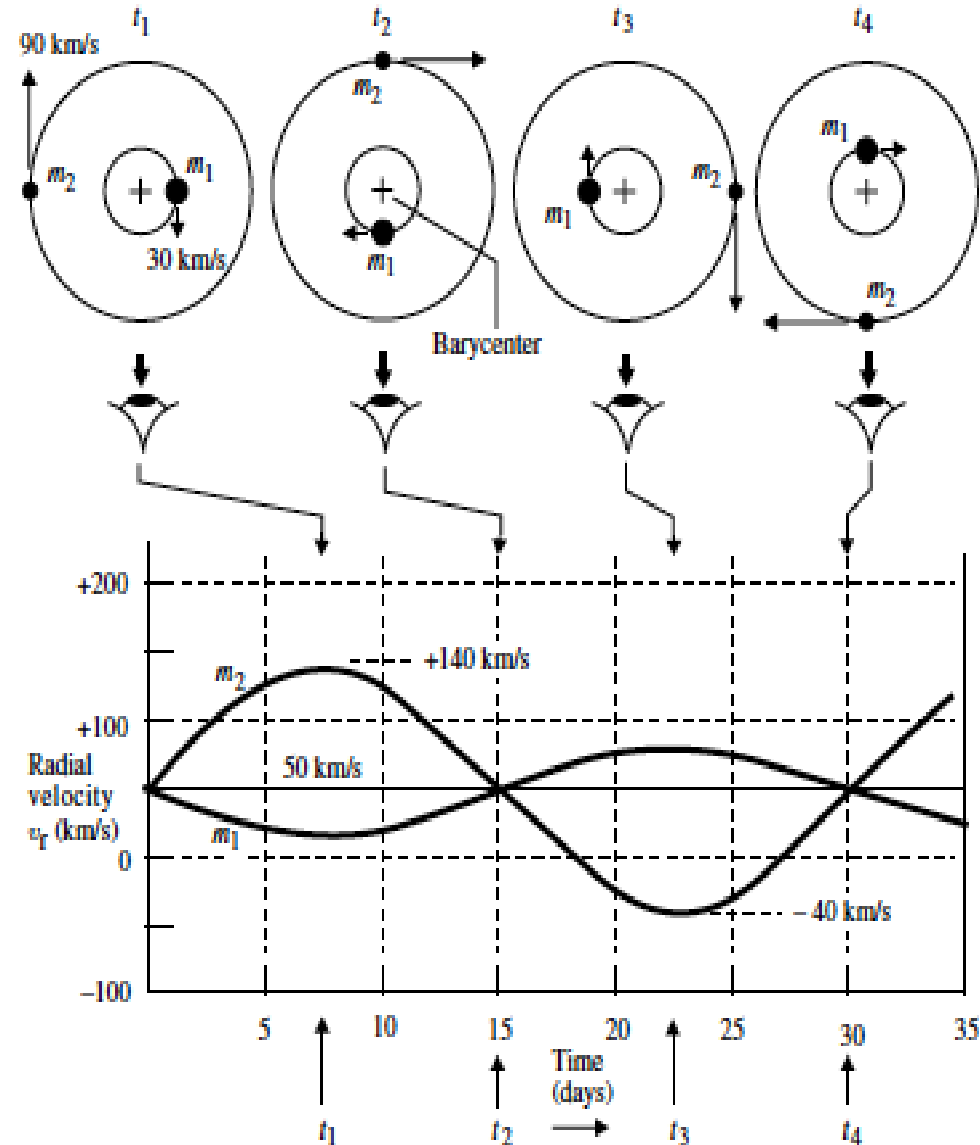


# The mass function

$$a_* = a \frac{M_o}{M_* + M_o}$$

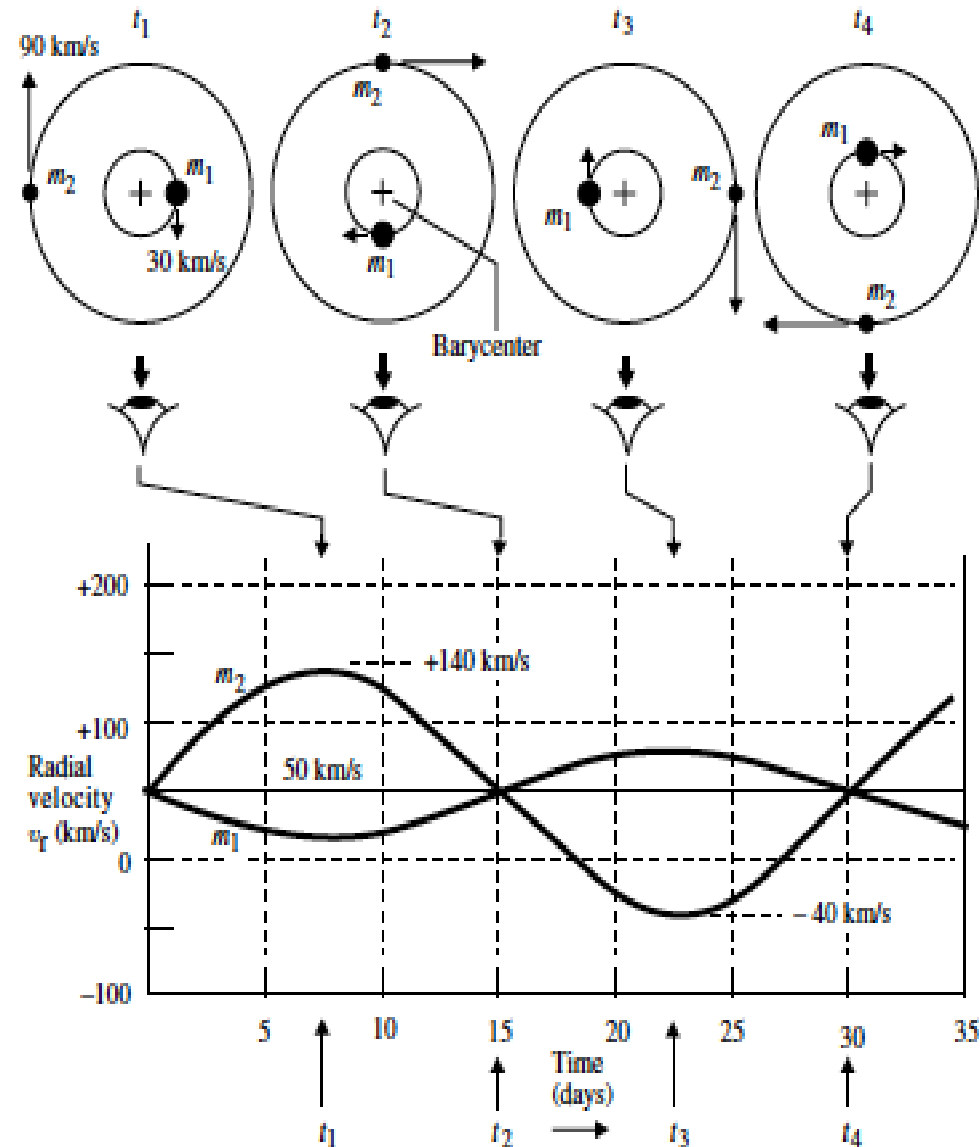


# The mass function

$$a_* = a \frac{M_o}{M_* + M_o}$$

Kepler's 3<sup>rd</sup> law becomes:

$$\omega^2 = G \frac{M_* + M_o}{a^3}$$



# The mass function

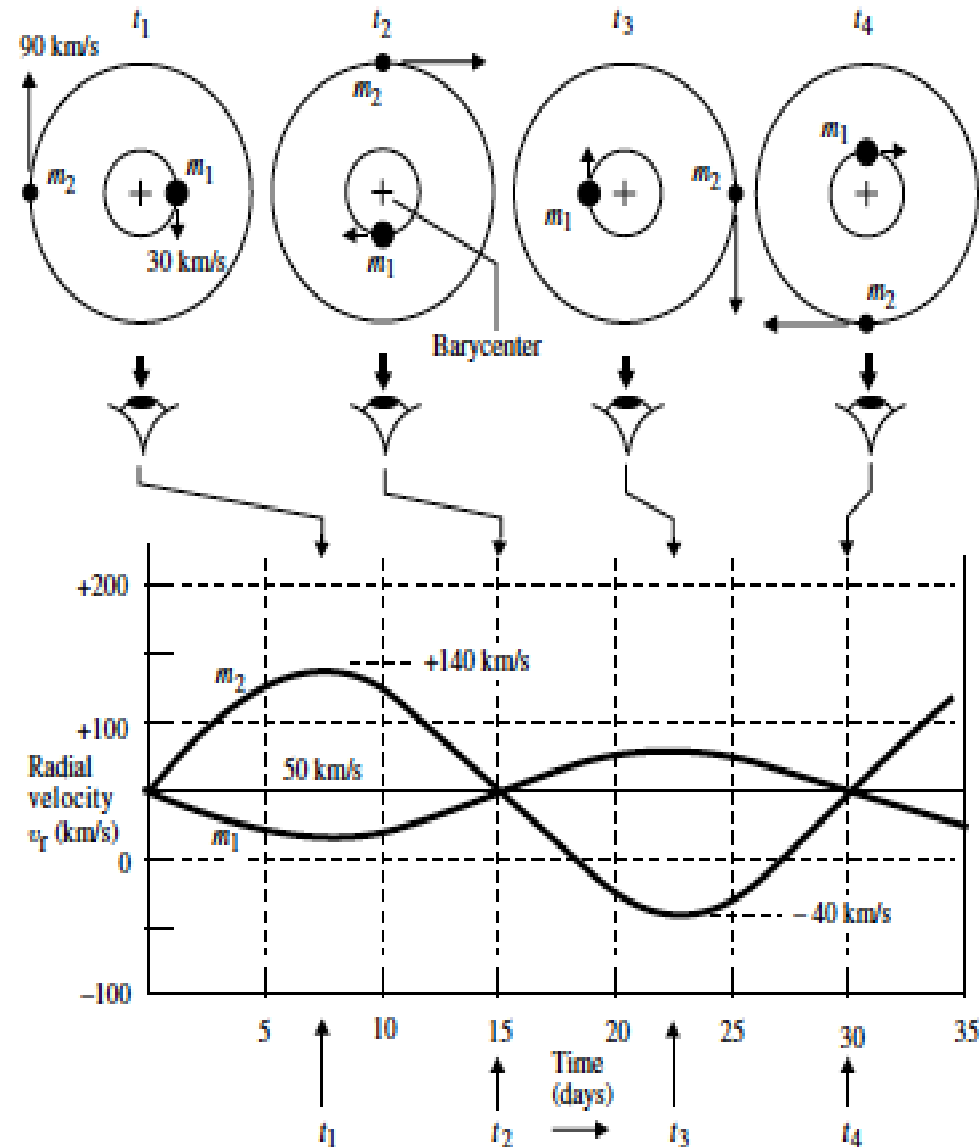
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We can also measure :

$$v_{max} = \omega a_* \sin(i)$$



# The mass function

$$a_* = a \frac{M_o}{M_* + M_o}$$

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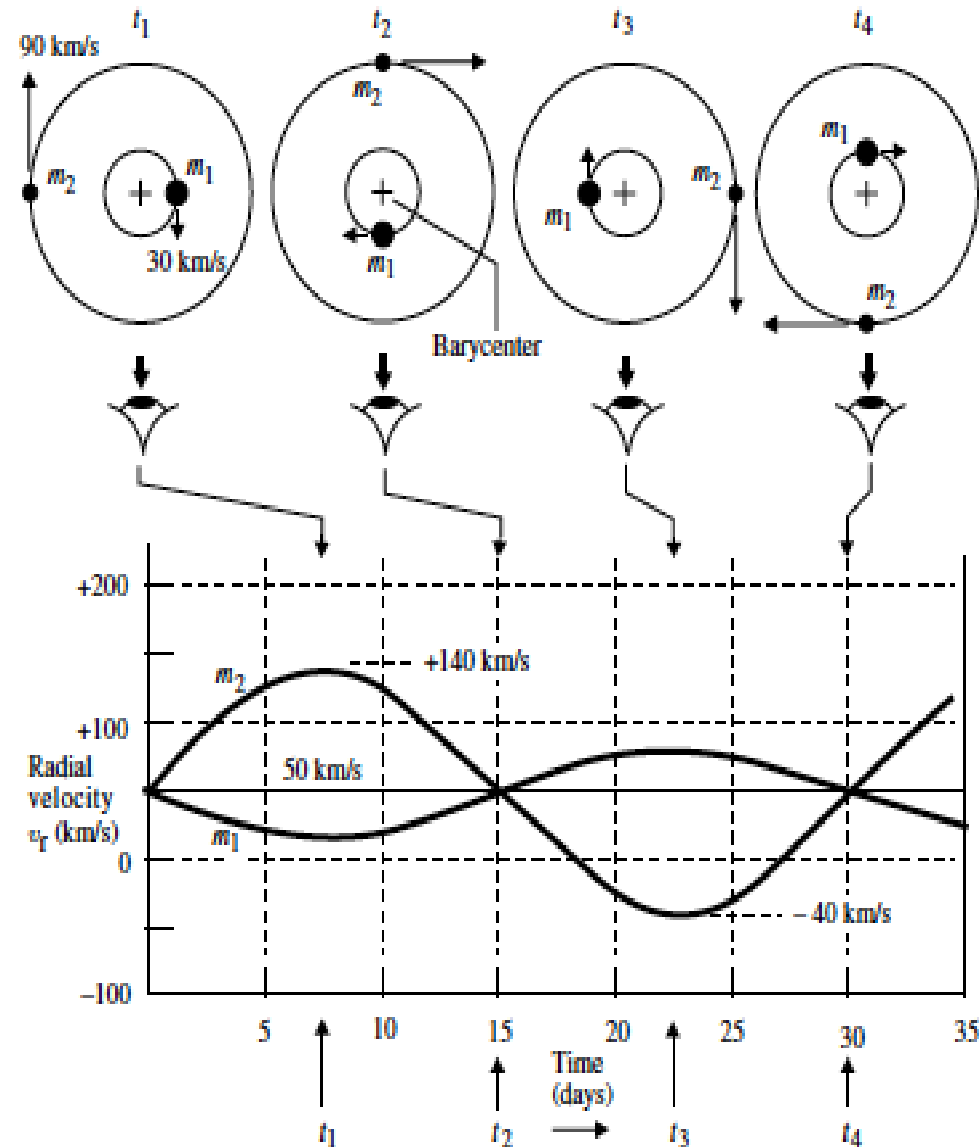
$$\omega^2 = G \frac{M_* + M_o}{a^3}$$

We can also measure :

$$v_{max} = \omega a_* \sin(i)$$

We define **mass function** :

$$f = \frac{v_m^3}{\omega G} = \frac{M_o^3 \sin^3 i}{(M_* + M_o)^2}$$



# The mass function

$$f = \frac{v_m^3}{\omega G} = \frac{M_o^3 \sin^3 i}{(M_* + M_o)^2}$$

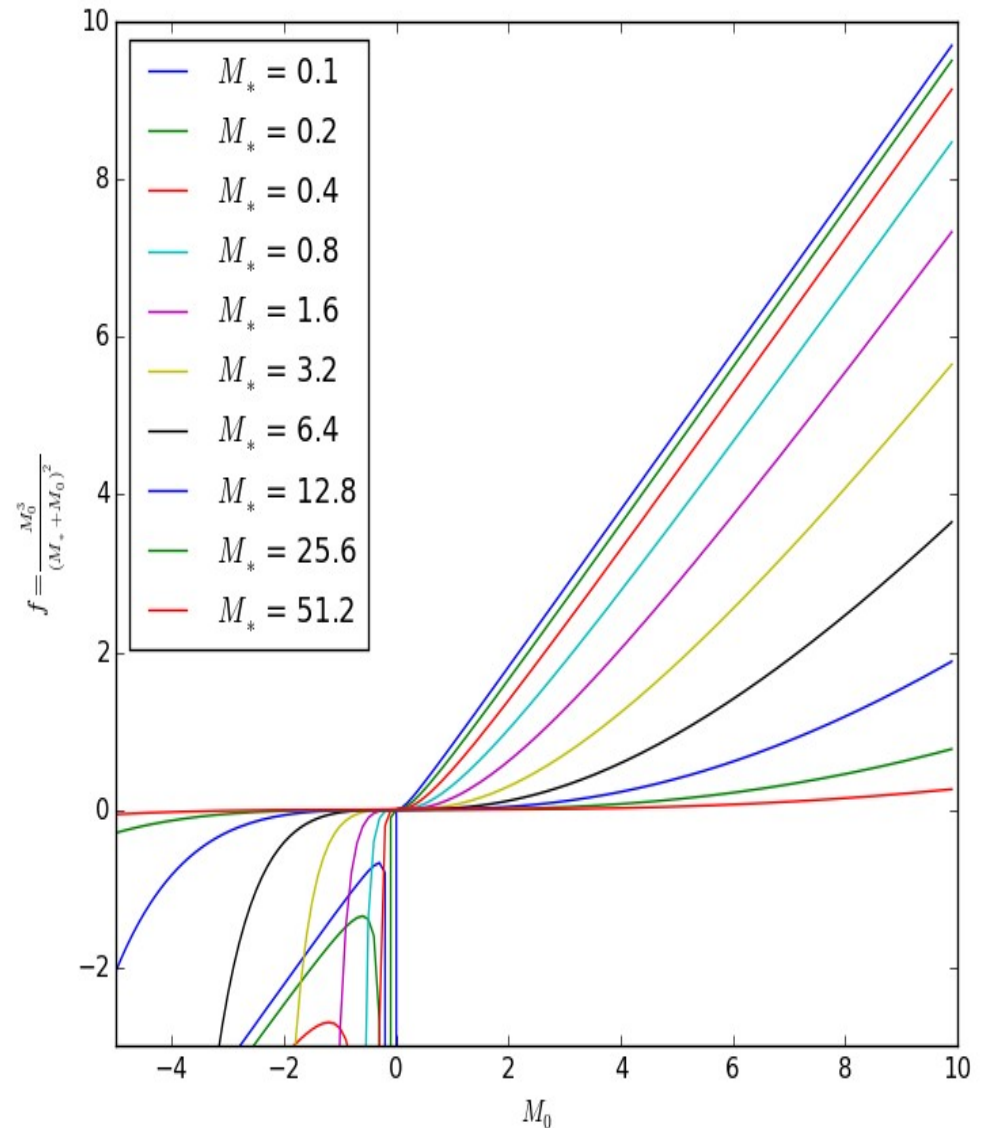
Mass function ( $f$ ): contains all measurable quantities

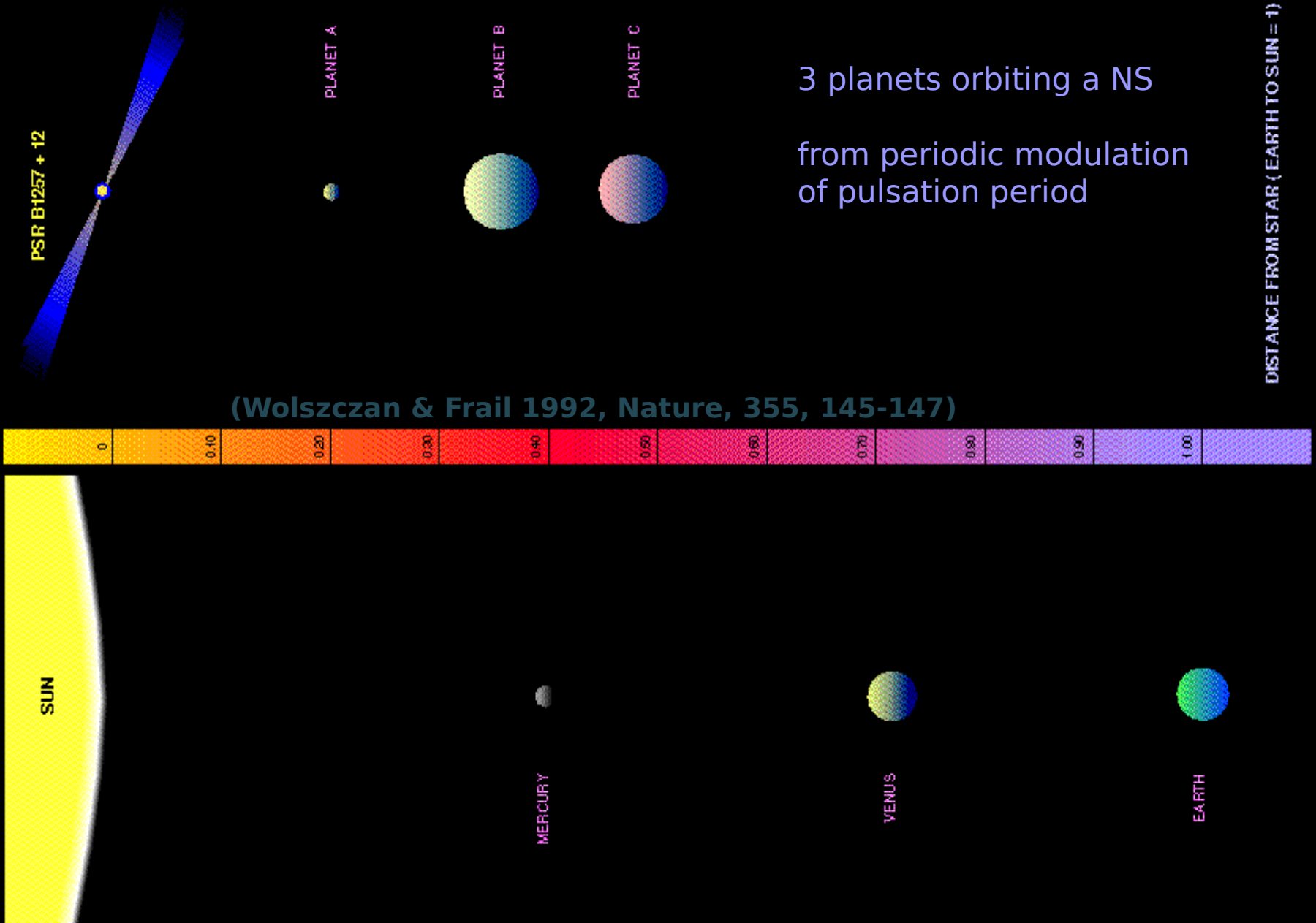
if stellar mass is known,

$f_*$  provides  $m_o \sin i$

with  $\sin i = 1$

lower limit on  $m_o$





# Exoplanets

# METHODS AND PRINCIPLES

---

Gravity causes star to “wobble”:

## 1) RADIAL VELOCITY

Radial Velocity: Motion toward and away detected by Doppler shifts in **stellar spectra**

## 2) ASTROMETRY

Astrometry: Motion in plane of sky detected in **images of stars** compared to background

---

Eclipses by planets (slightly!) dim the star light

## 3) TRANSIT

Detected by brightness decrease in **light curve**

---

## 4) MICROLENSING

Stars sometimes gravitationally lens background stars and the planet can contribute (very slightly)

Detection by small blip in lens **light curve**

---

## 5) IMAGING

Image of starlight reflected by planet.

Very Difficult: Requires **nulling** the star

---

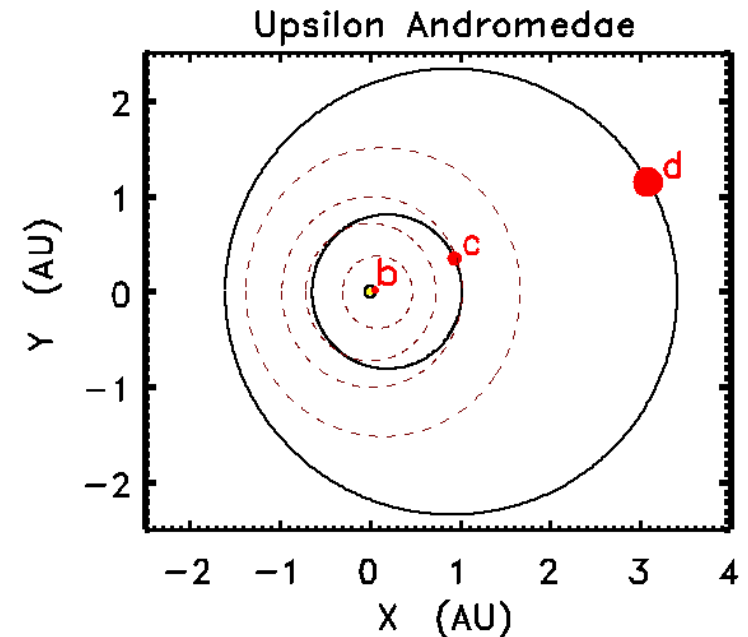
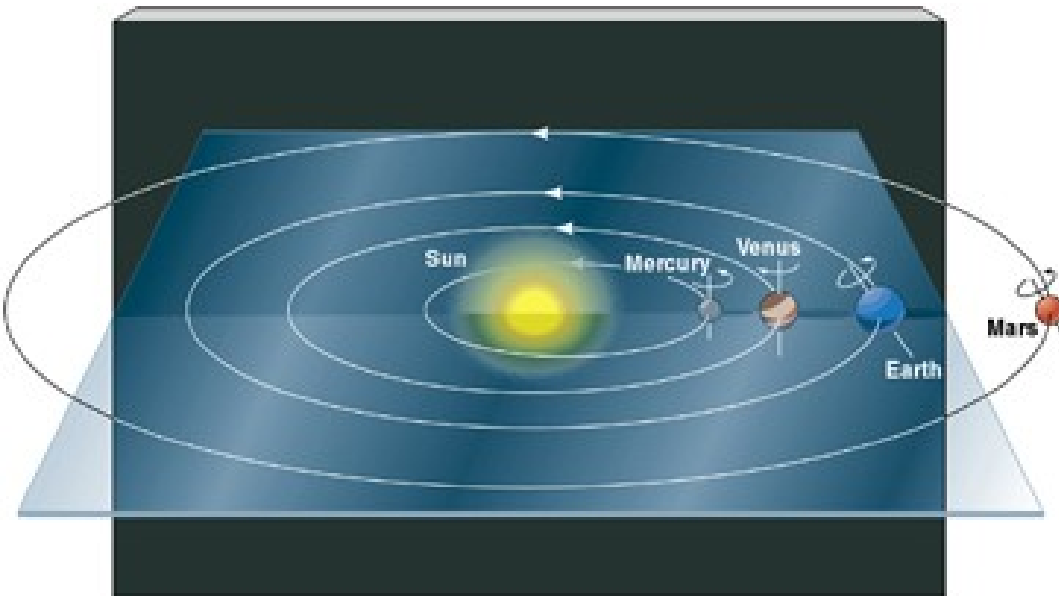


# PLANETARY SYSTEMS ALIGN IN A PLANE

The inclination of a planetary system can range from **edge on** to **face on**

**edge-on** = high inclination

**face-on** = low inclination

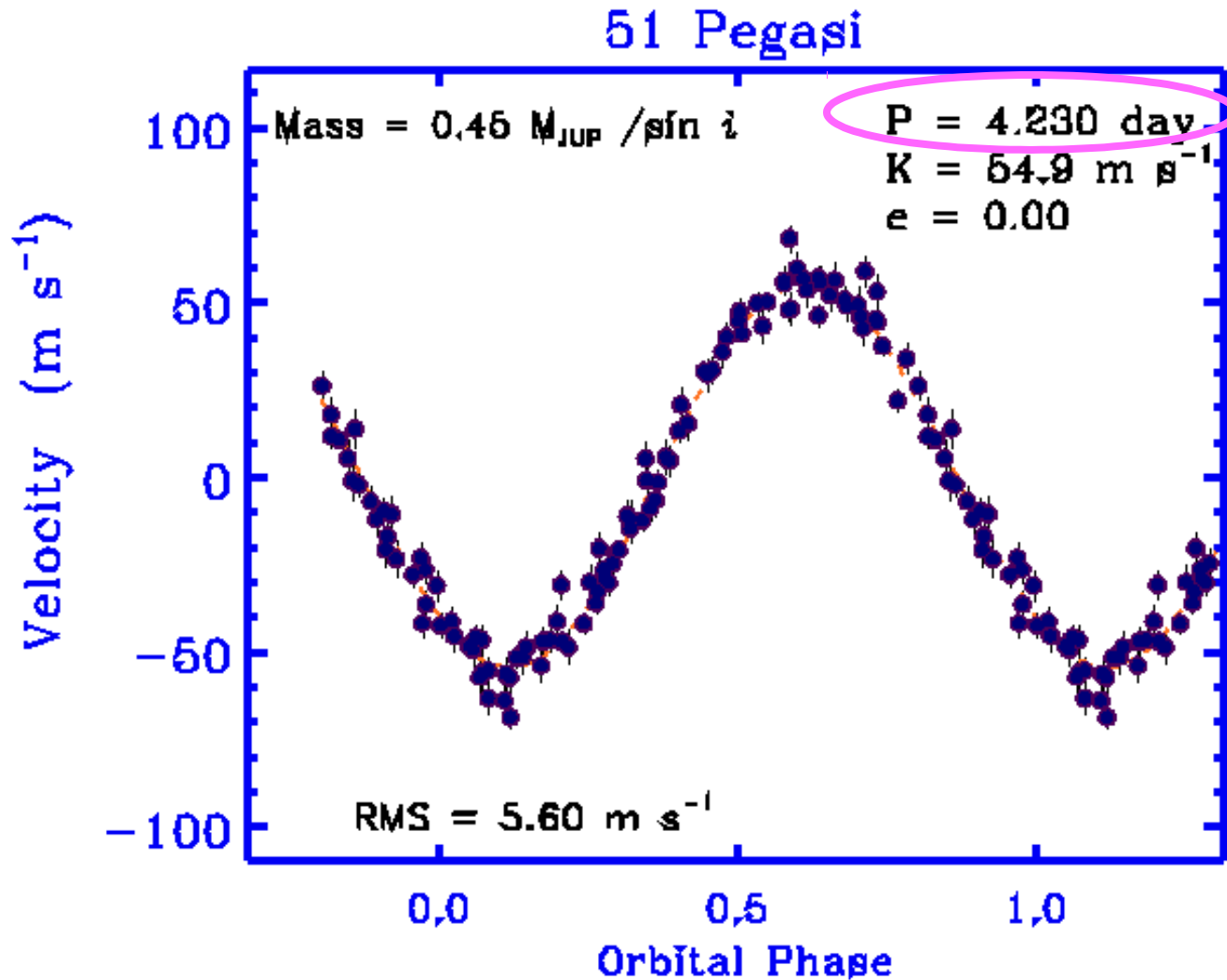


**Radial Velocity** and **Transit**  
methods

**Astrometry** and **imaging**  
methods

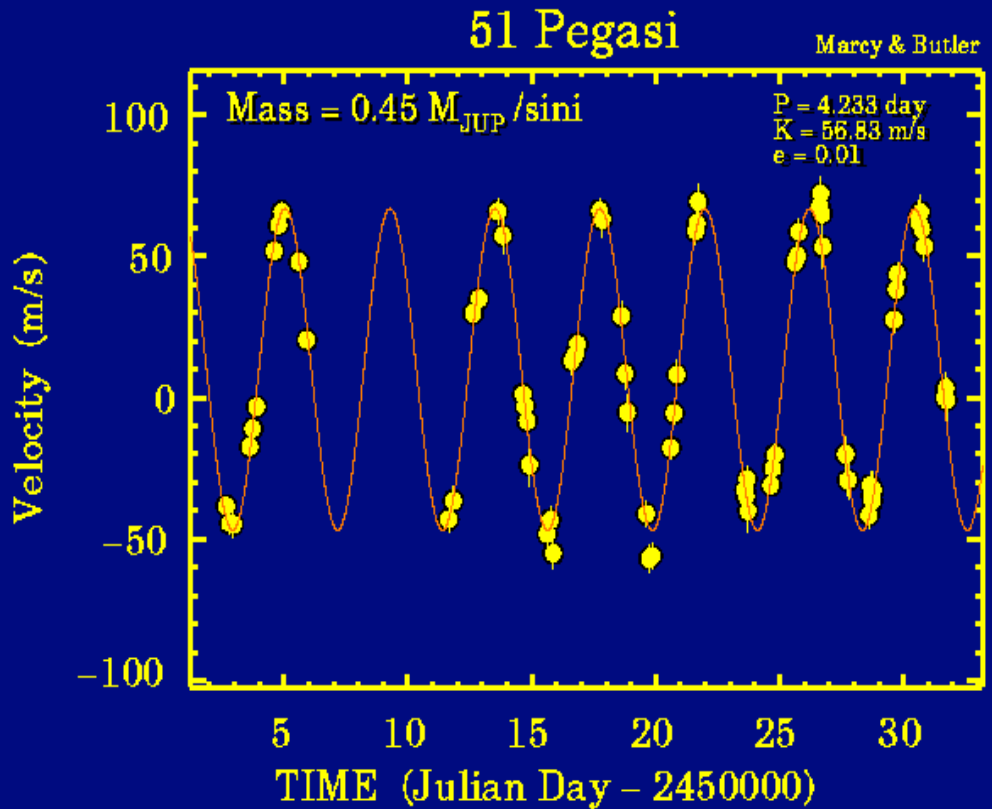
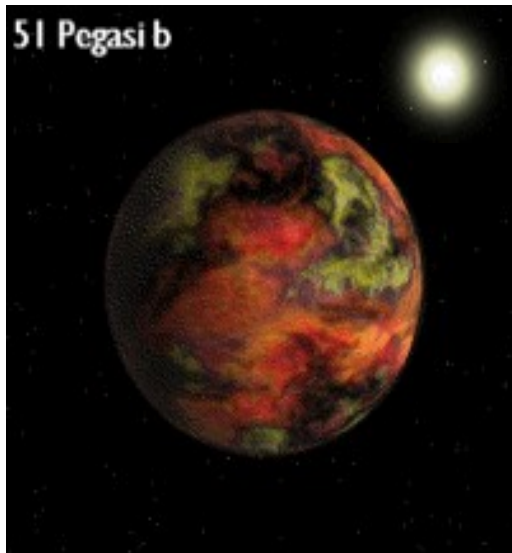
**Microlensing** method does not depend on orbital  
inclination

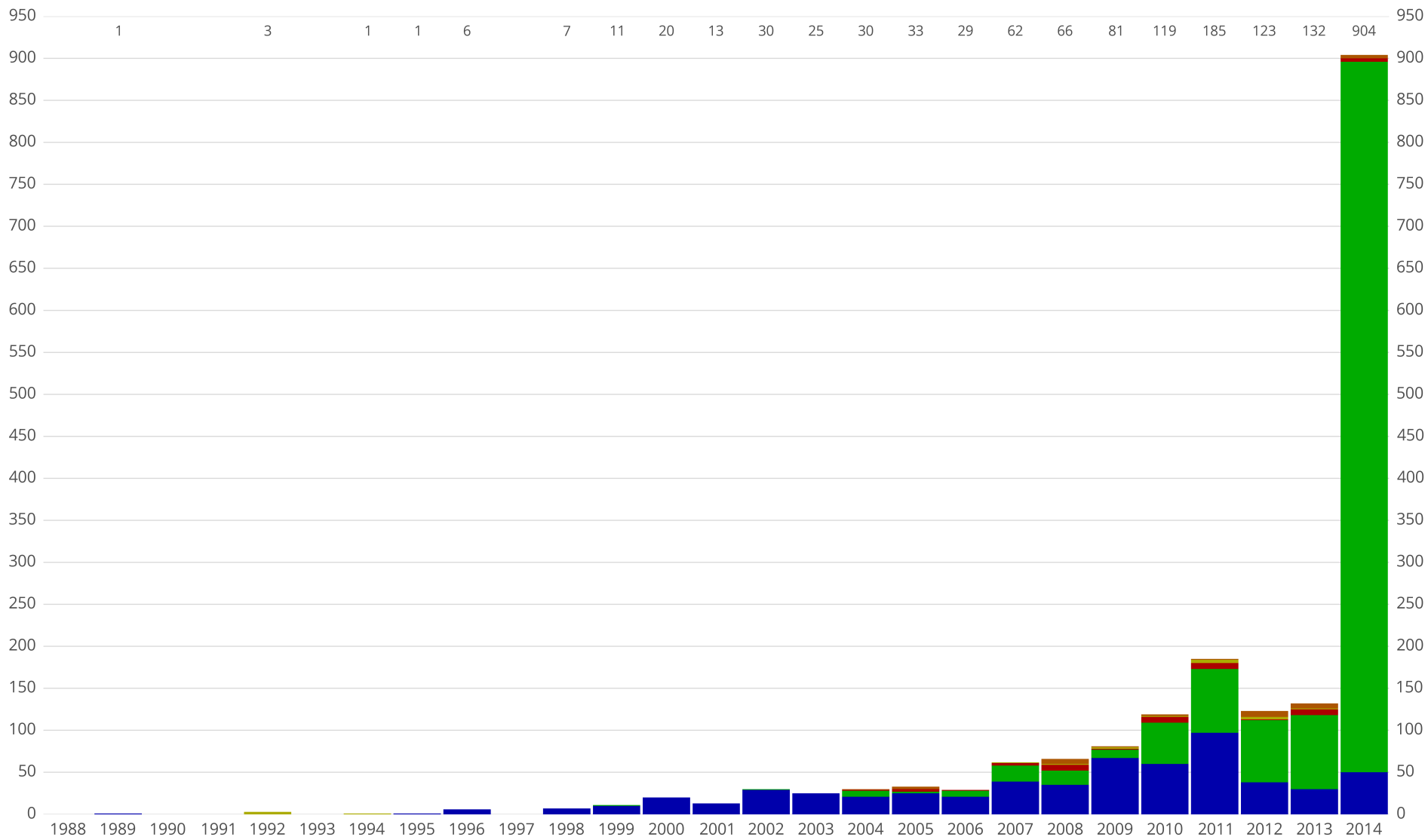
# The first confirmed exoplanet orbiting a MS star



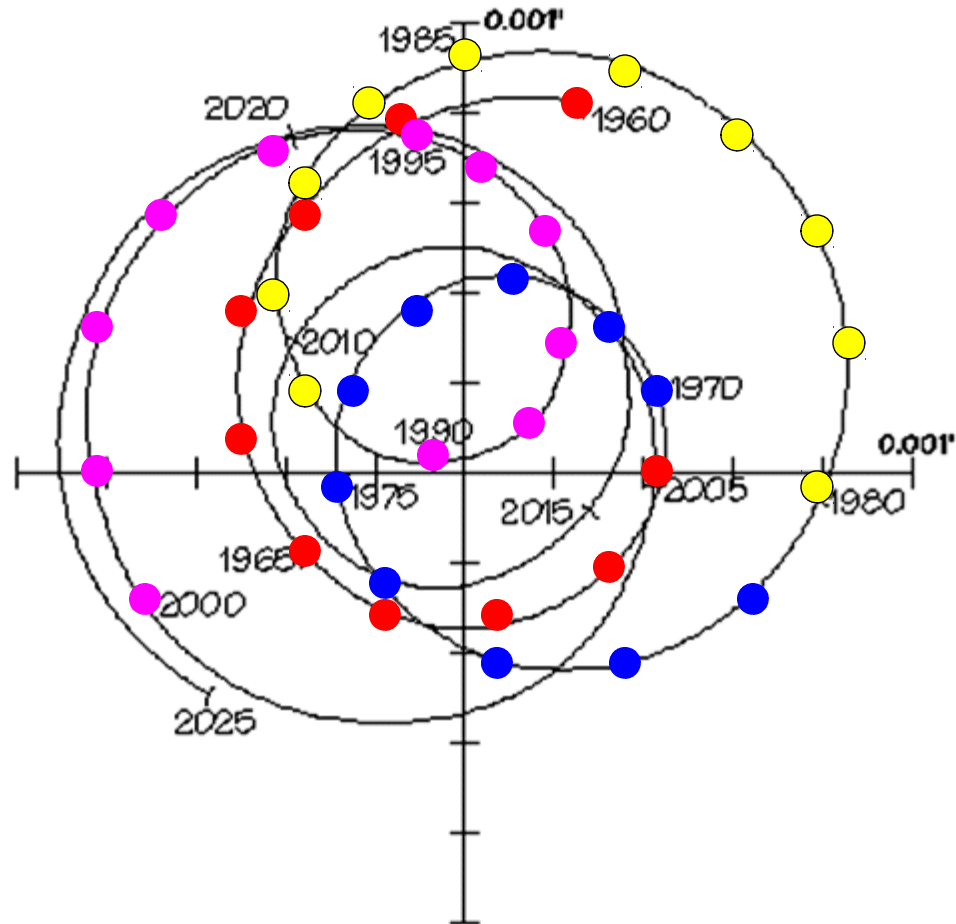
*Mayor & Queloz (1995)*

# RADIAL VELOCITY METHOD





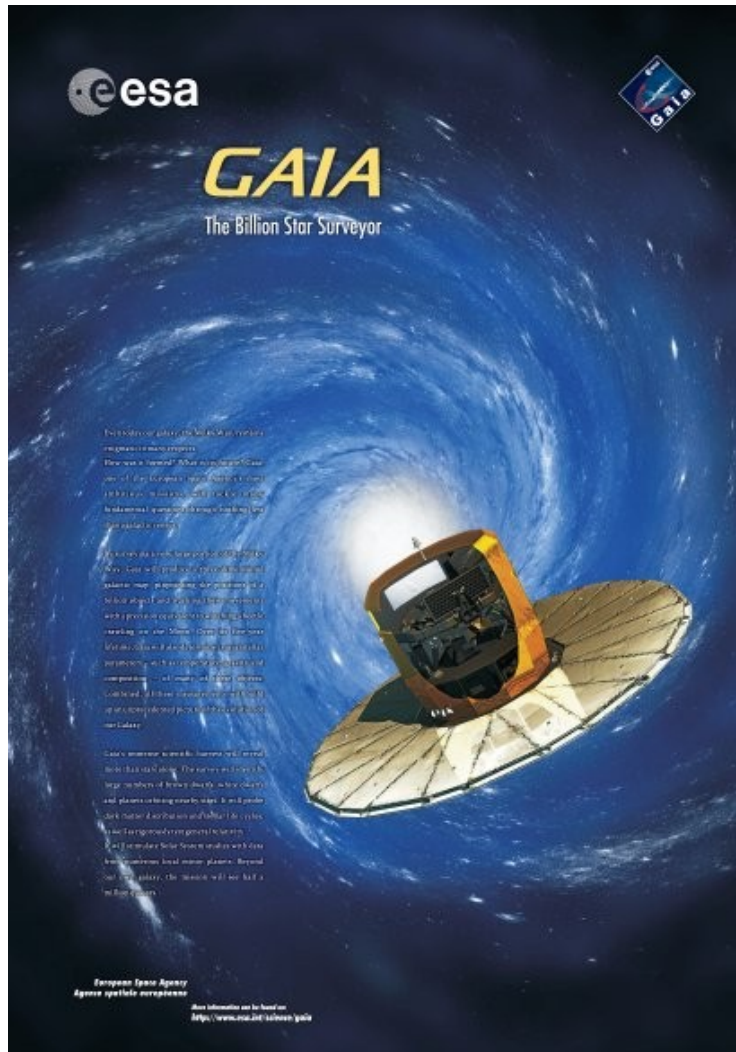
# STELLAR WOBBLE: THE SUN



We would not have detected Jupiter around our star using Radial Velocity  
We could detect Jupiter if we had been watching using Astrometry

# ASTROMETRY METHOD

No confirmed planet discoveries yet, but will be soon possible with GAIA (ESA, **2013 December 19**;  $\mu$ -arcsec astrometry)



Combining Astrometry and Radial Velocity methods

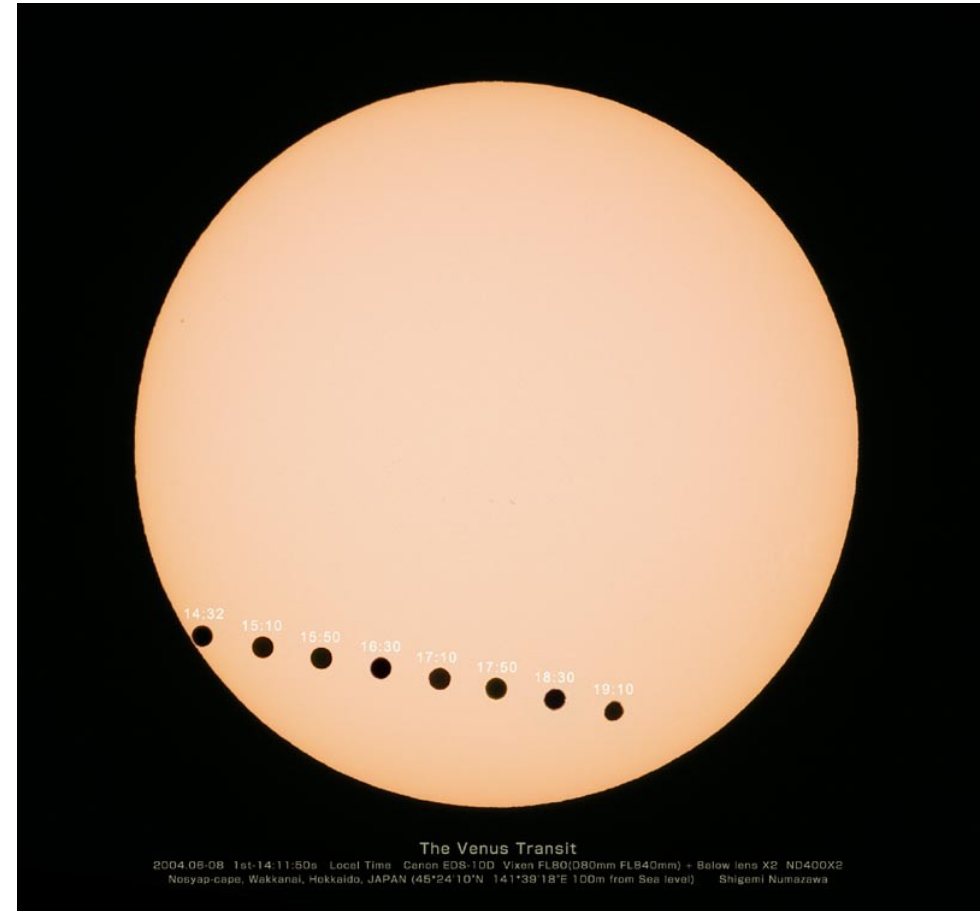
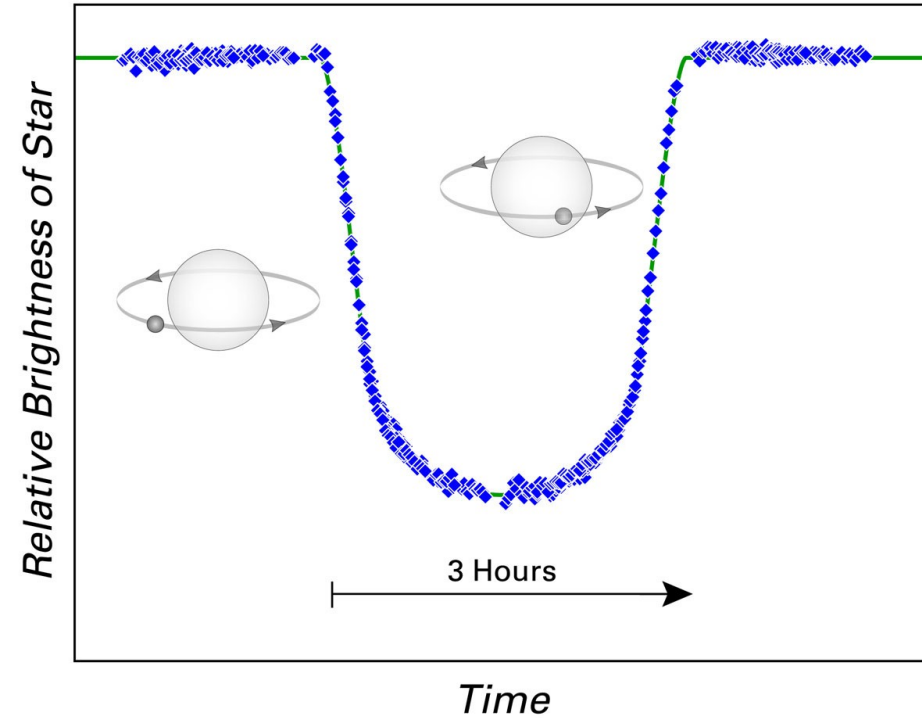
⇒ orbit **inclination**

⇒ planet **mass**

~**8000** (massive) planets should be discovered by GAIA (until 2020)

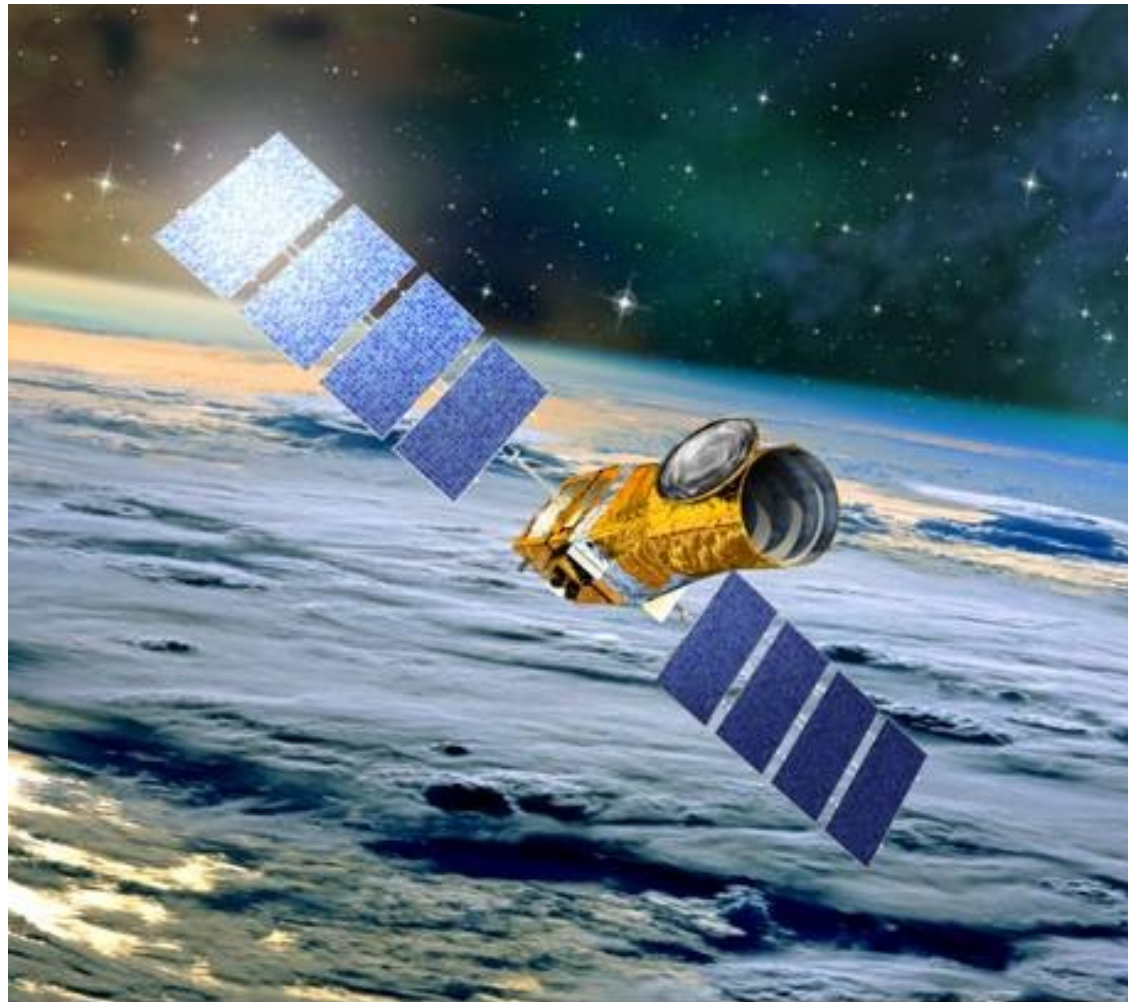
# Eclipse = transit

Planet Eclipsing Star HD 209458



- Planet **candidates** need to be confirmed by RV observations
- **Follow-up** observations are also needed to derive **planet mass** and to study **star properties**





© CNES - Octobre 2005/Illus. D. Ducros

*COROT (CONvection ROTation et Transits planétaires)* operated from 2006 December 27 to 2012 November 2. The project was led by CNES, in cooperation with ESA



# CoRoT 7b

Rocky planet

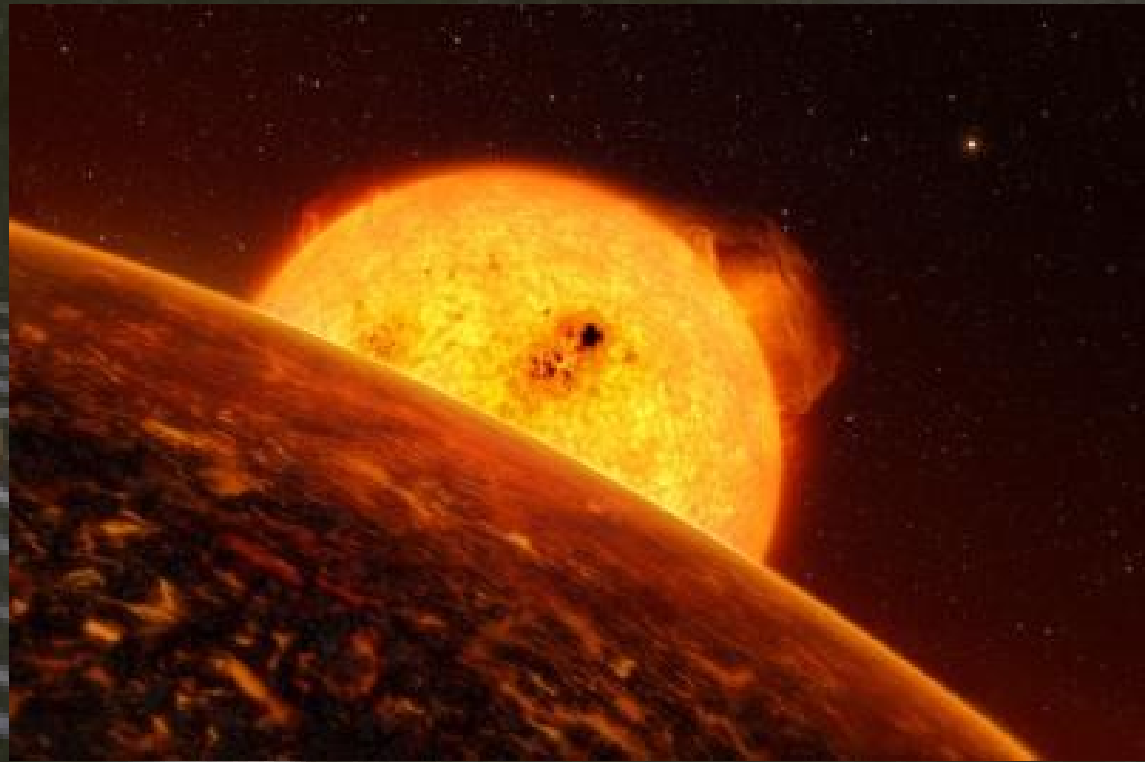
Mass = 5 Earth

$R = 2.5 \times 10^6$  km

(23 times closer than  
Mercury)

$P = 20.4$  h

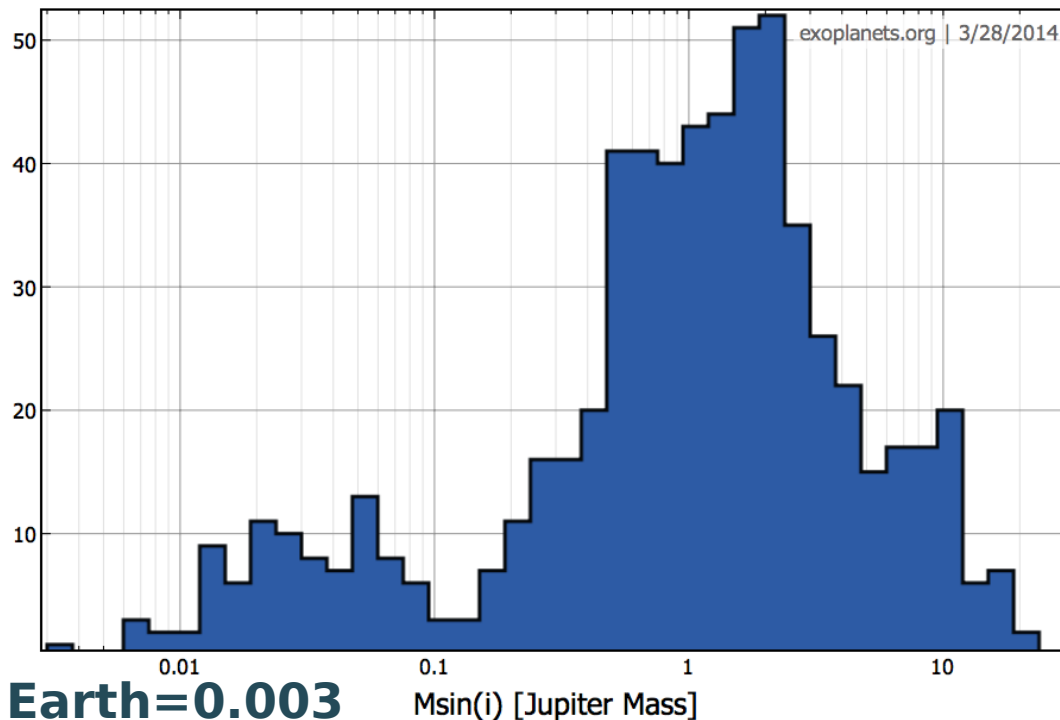
Star age = 1.5 Gy



- When discovered, Corot-7b was the closest known exoplanet to its host star, thus the fastest.
- *Day-face* temperature  $> 2,000^\circ$ , but  $-200^\circ$  on *night face*. CoRoT 7b may have lava or boiling oceans on its surface.
- The sister planet, Corot-7c, is more distant.

# RADIAL VELOCITY METHOD

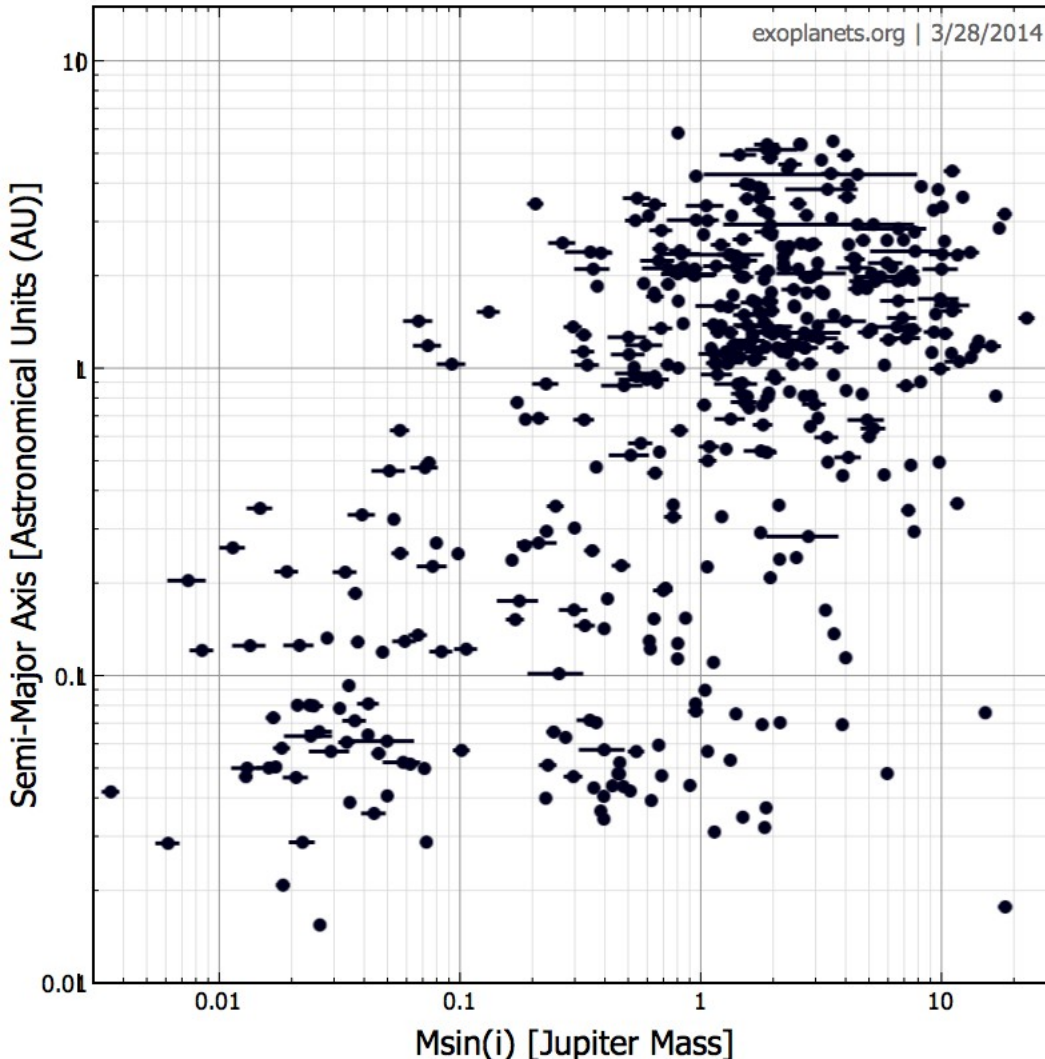
## Number of planets with a given “mass”



1. One cannot get the mass directly, if the **inclination** of the system is unknown
2. One determines combined quantity of planet mass and the inclination angle
3. Smaller “mass” planets are the hardest to find)  $\Rightarrow$  **small planets are very numerous**

# RADIAL VELOCITY METHOD

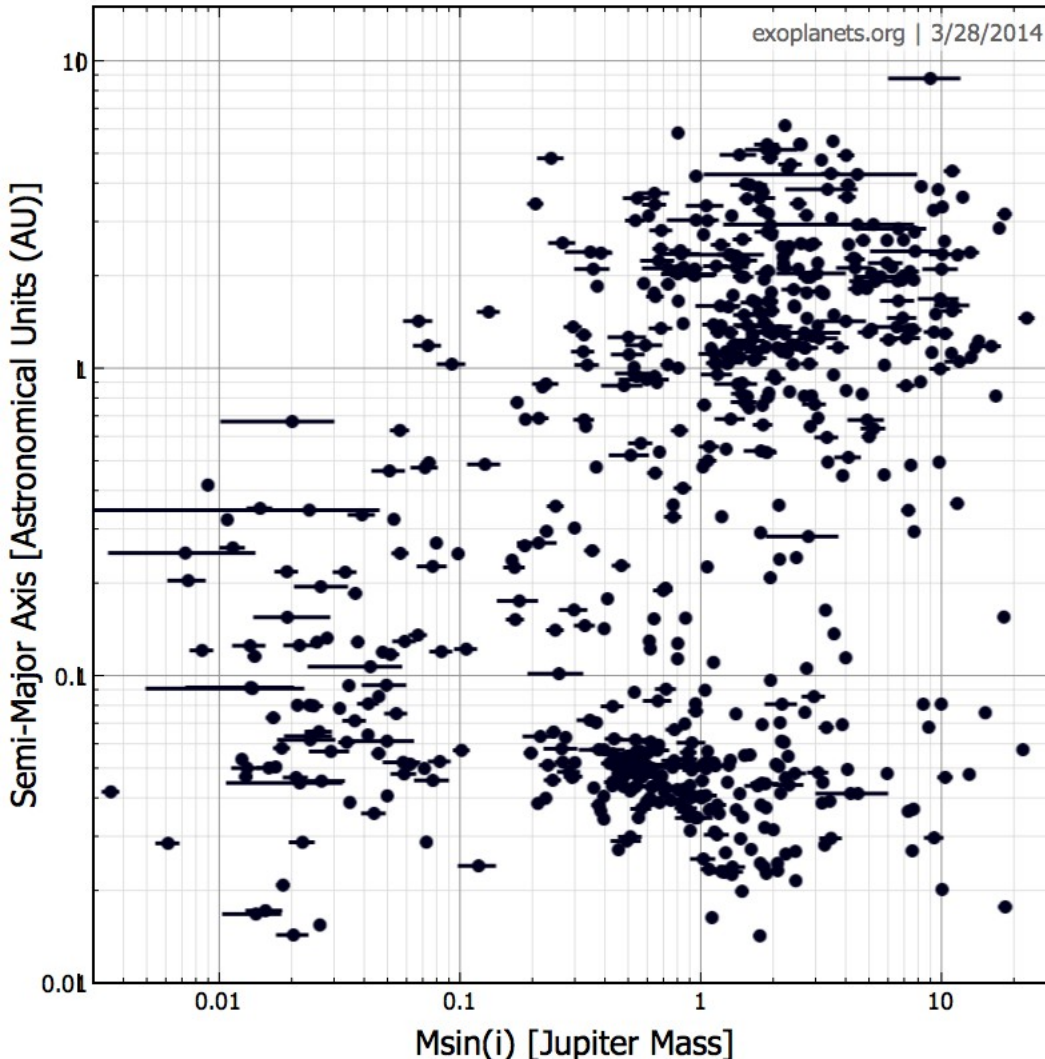
## Planets discovered with RV method



- 1) 440 planets (~**30%**) discovered since 1995 with **RV** method
- 2) **RV** method selects **high mass** planets with relatively small orbits

# RADIAL VELOCITY METHOD

## All confirmed planets

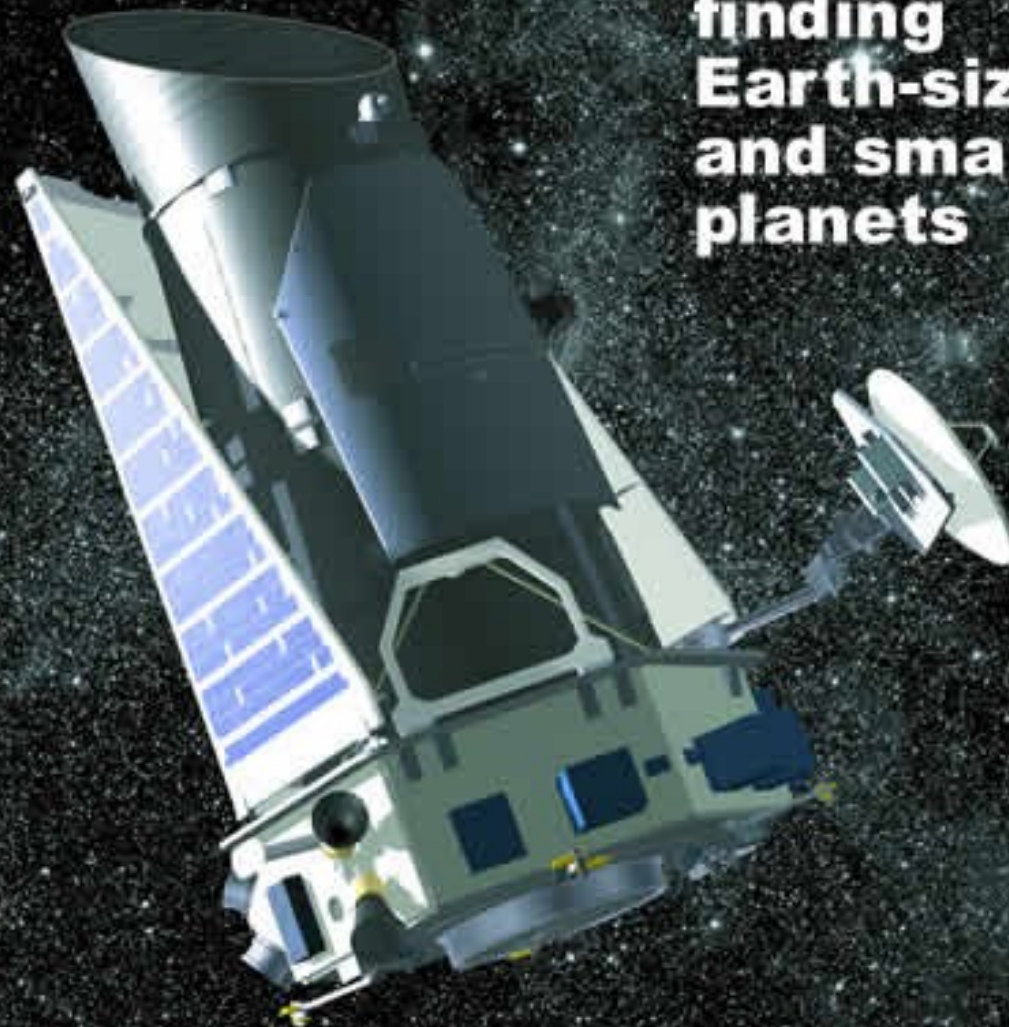


- 1) 440 planets (~**30%**) discovered since 1995 with **RV** method
- 2) **RV** method selects **high mass** planets with relatively small orbits
- 3) With **transits**, even **smaller orbits** (less dependent on mass)



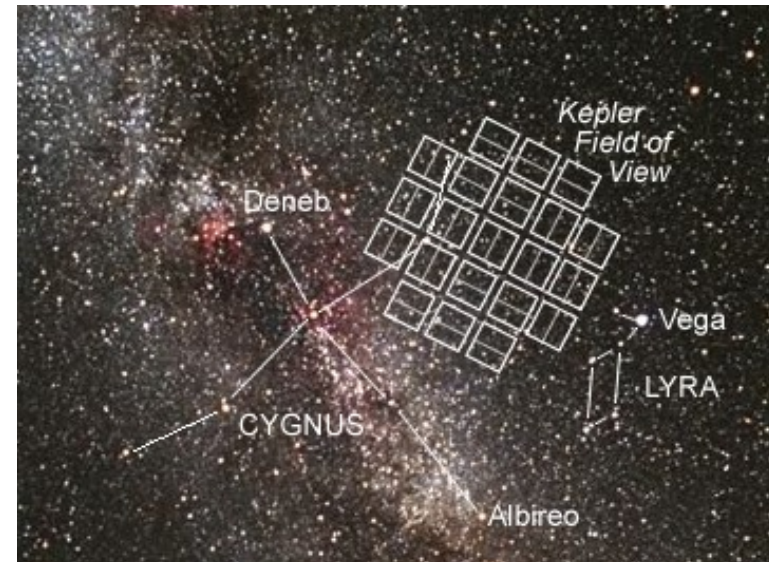
# *Kepler*

**NASA's  
first mission  
capable of  
finding  
Earth-size  
and smaller  
planets**



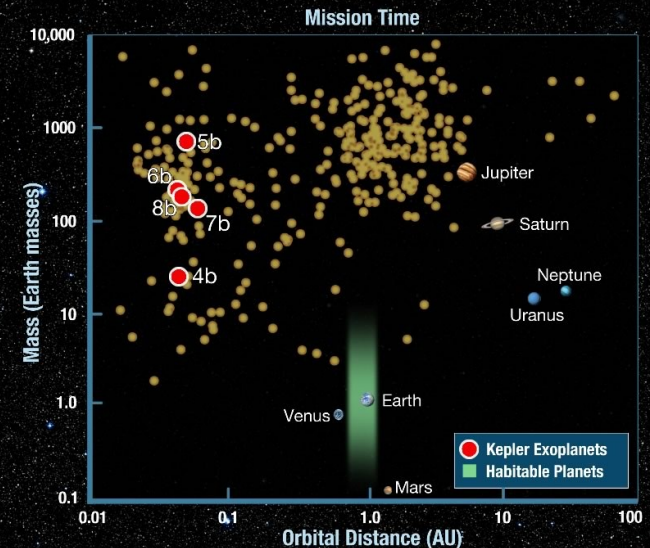
# Kepler

- Launched in March 2009
- Pointing sky region in Cygnus
- 4570 planet candidates
- 961 confirmed planets
- Multiple systems
- Earth-sized planet candidates



## First Five Planet Discoveries

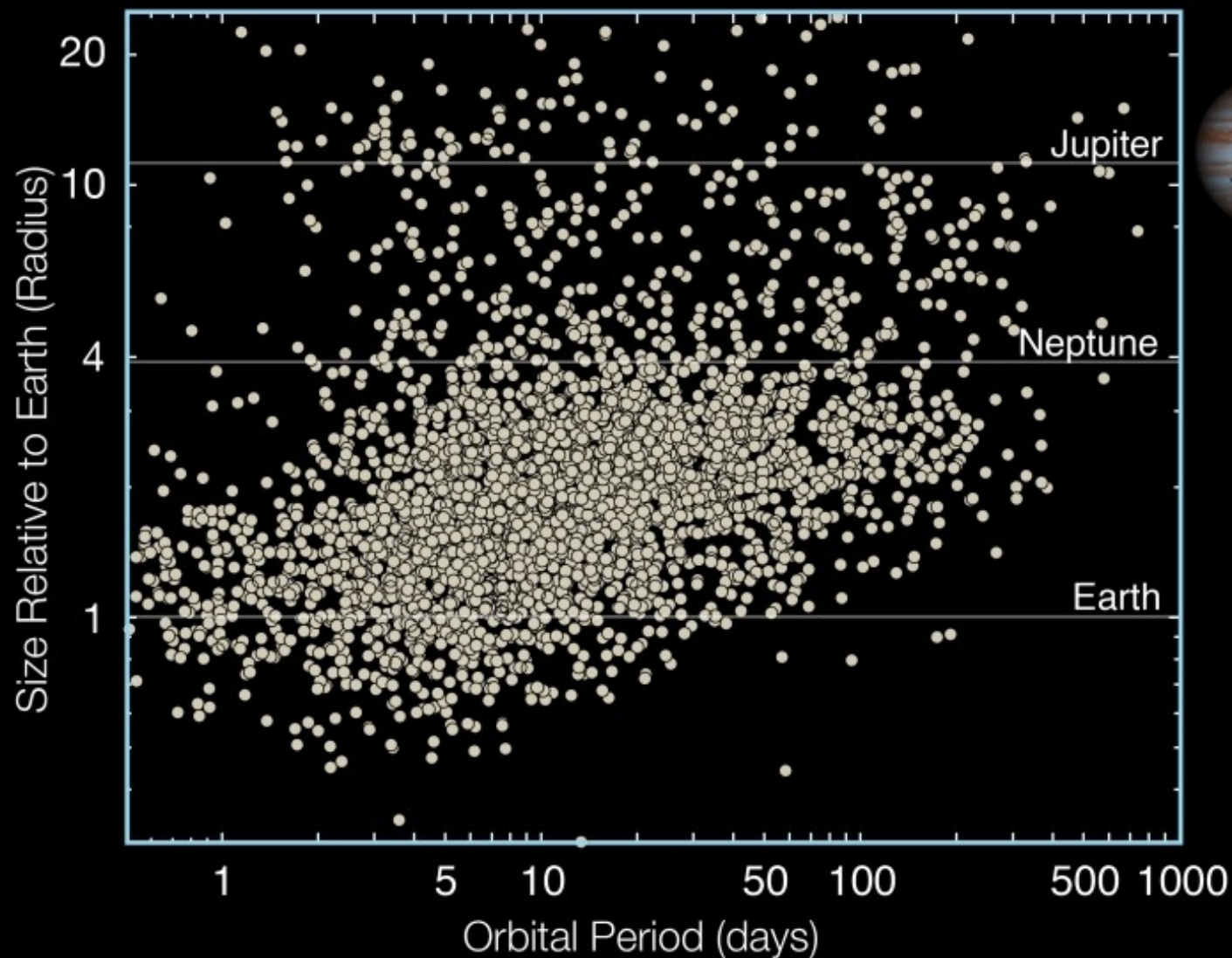
Made with First 43 Days of Data





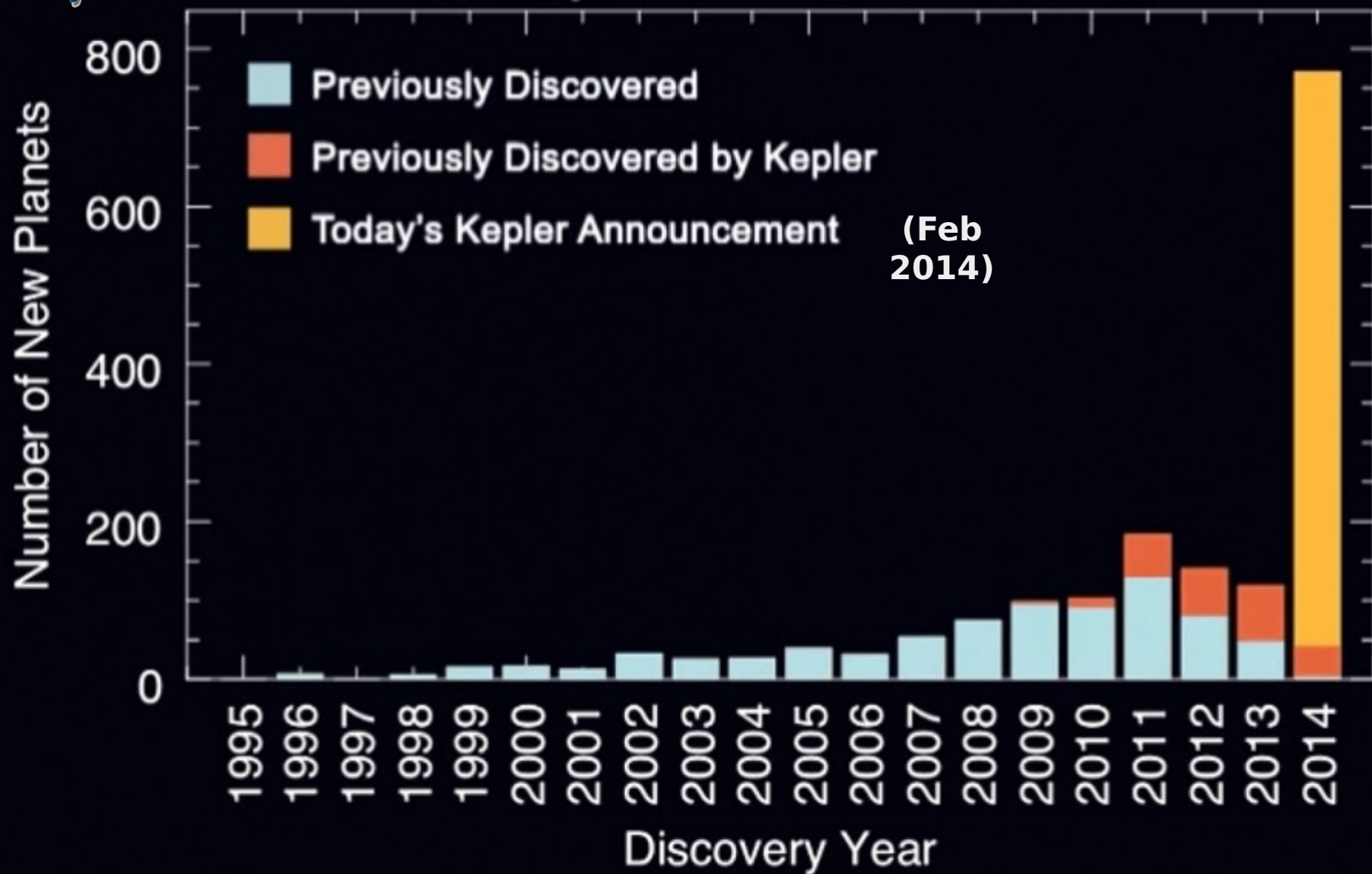
# Planet Candidates

As of November 4, 2013





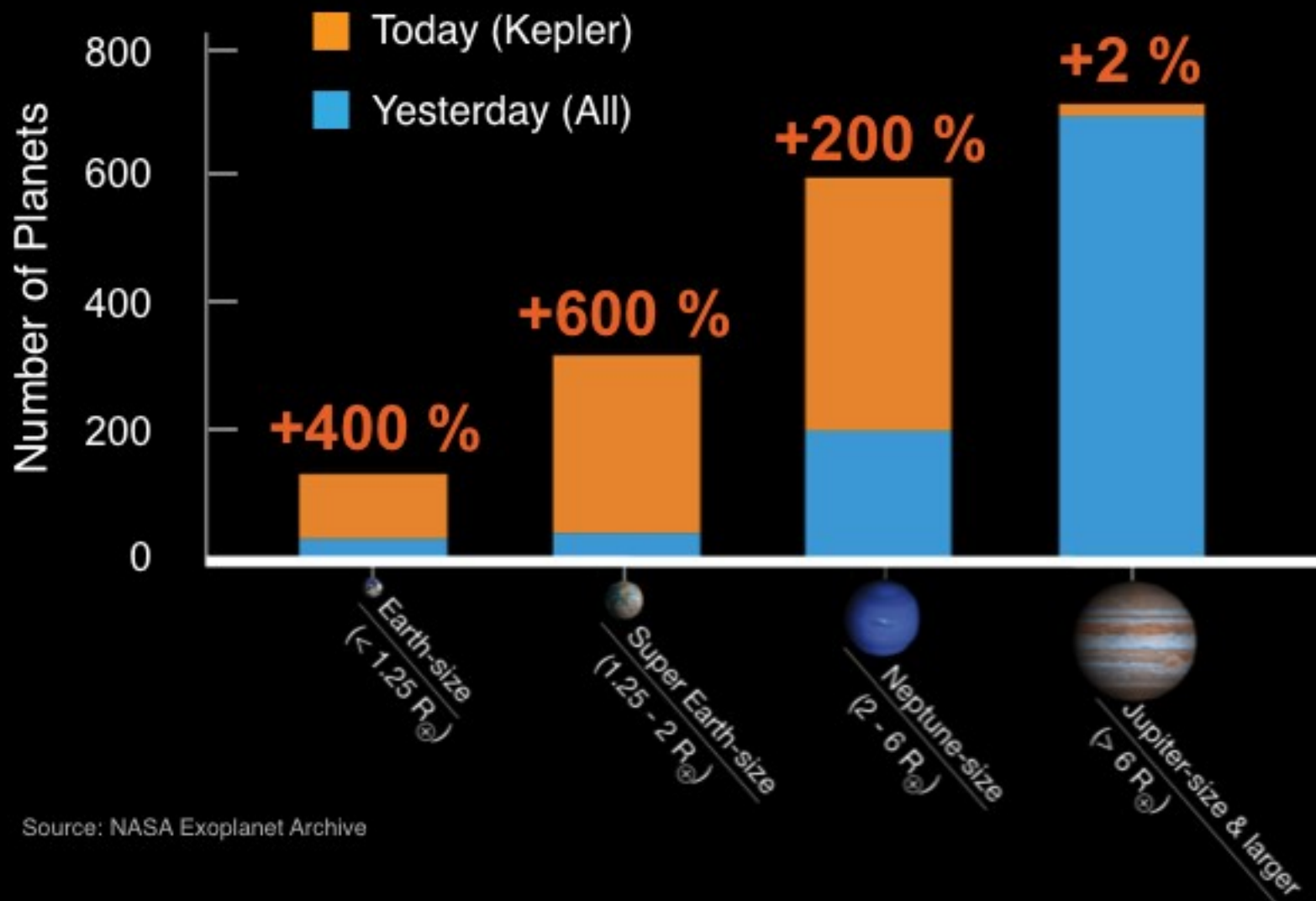
# Exoplanet Discoveries





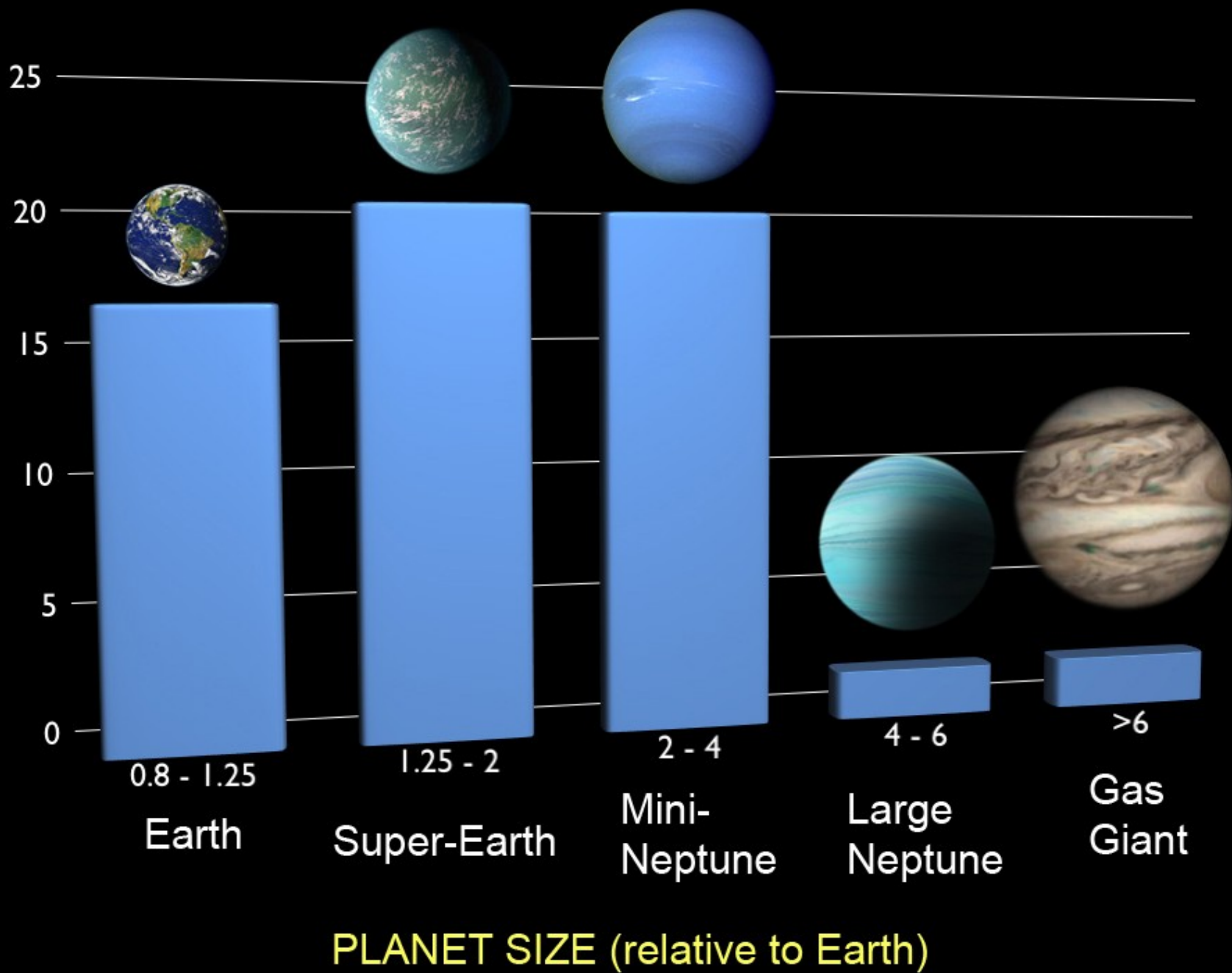
# Sizes of Known Exoplanets

As of February 26, 2014



Source: NASA Exoplanet Archive

FRACTION OF STARS  
WITH AT LEAST ONE PLANET

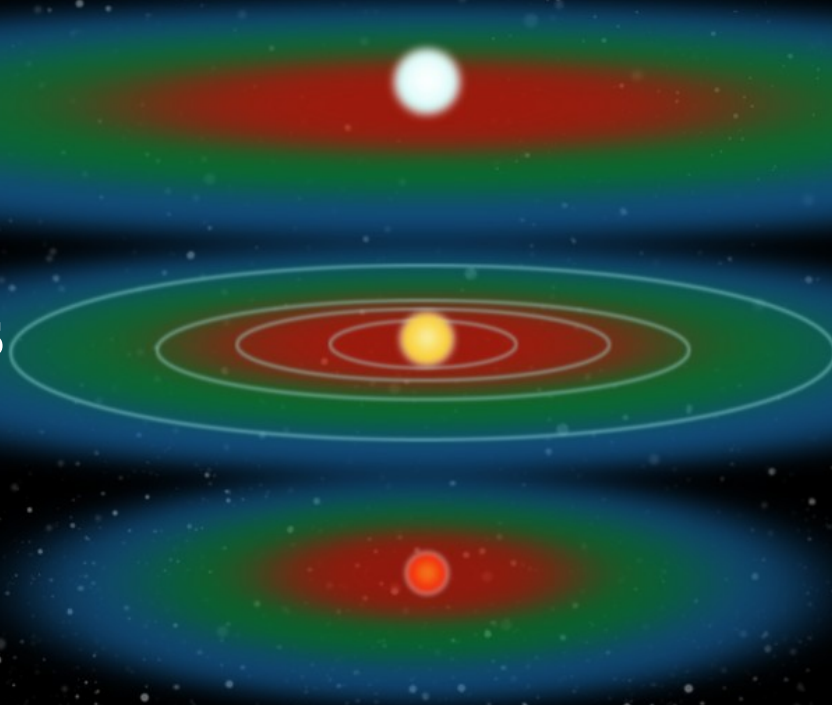


# The Habitable Zone *(where water is liquid)*

**Hotter Stars**

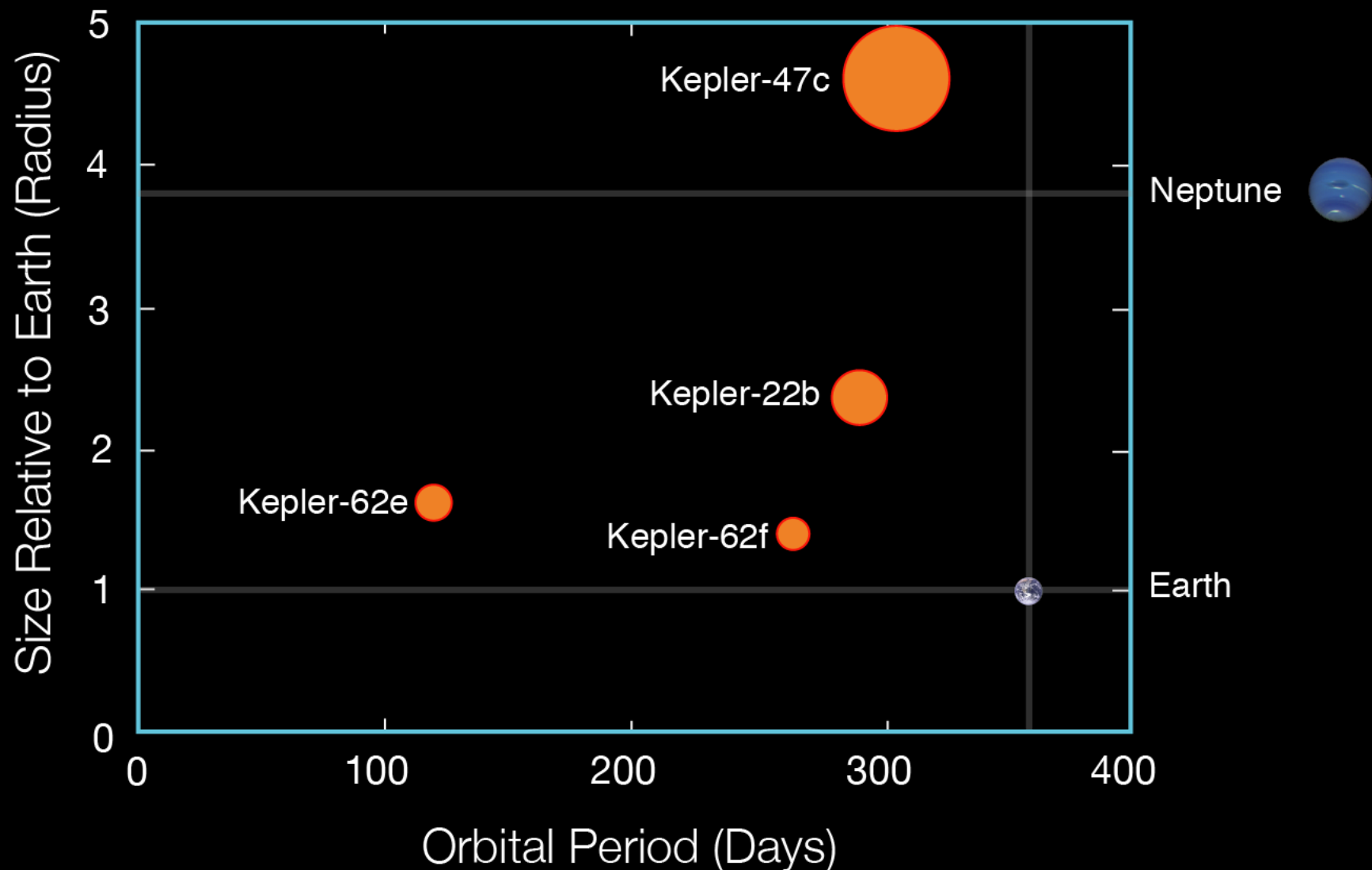
**Sun-like Stars**

**Cooler Stars**

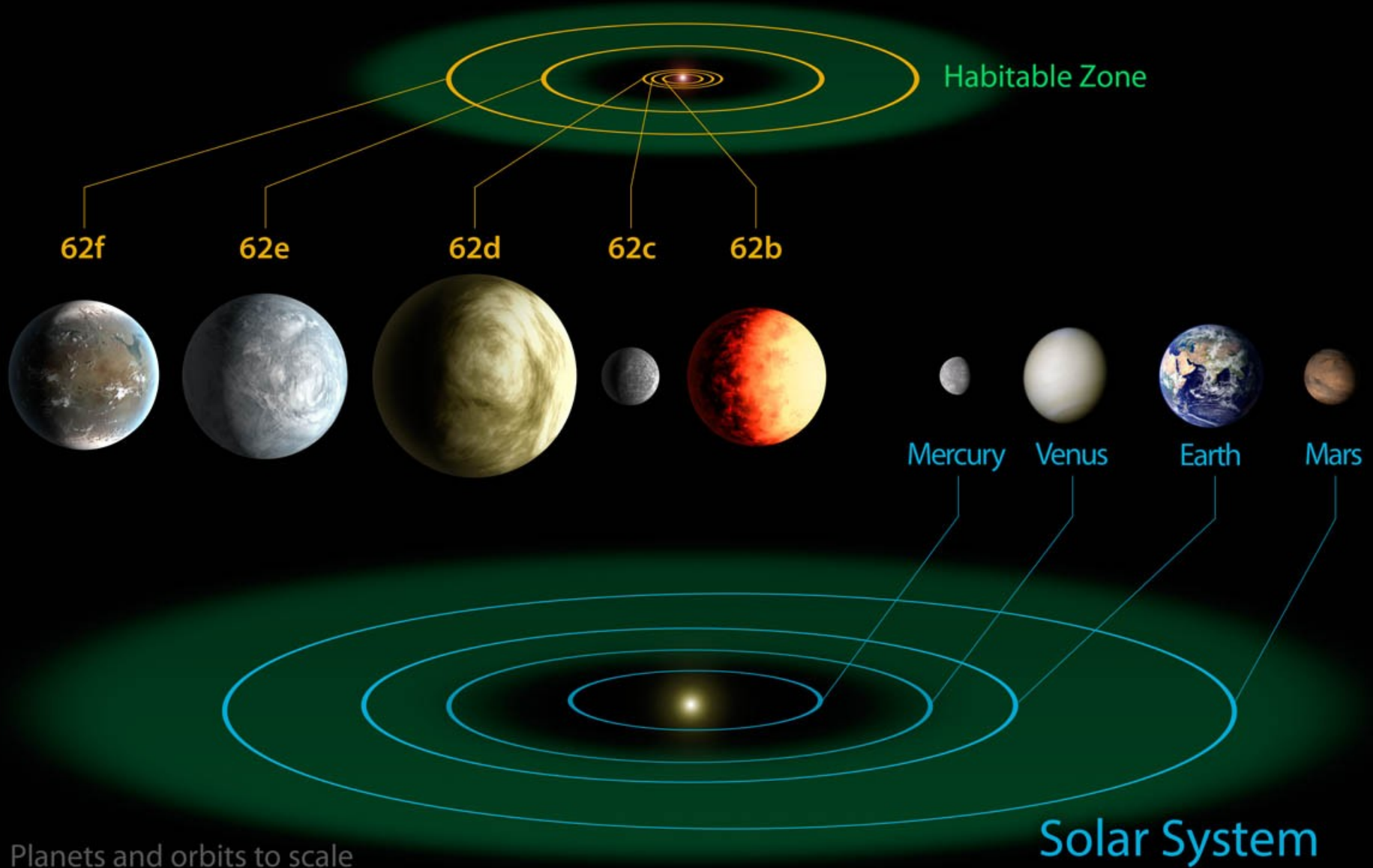




# Kepler's Habitable Zone Planets



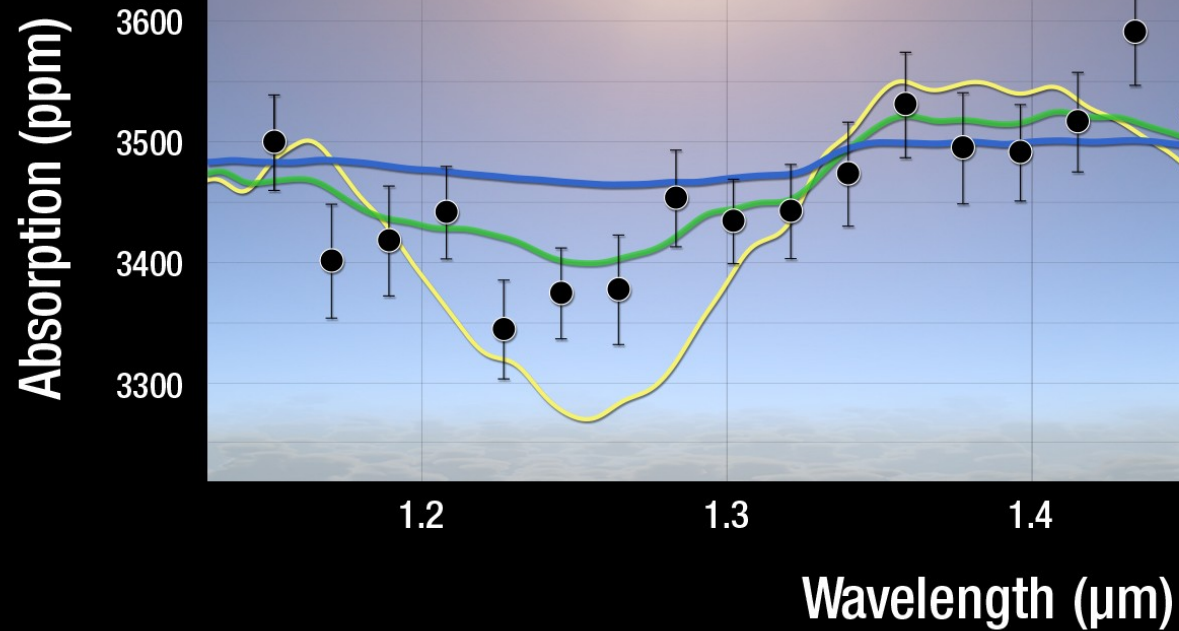
# Kepler-62 System





Artist's concept

# Transmission Spectrum of HAT-P-11b



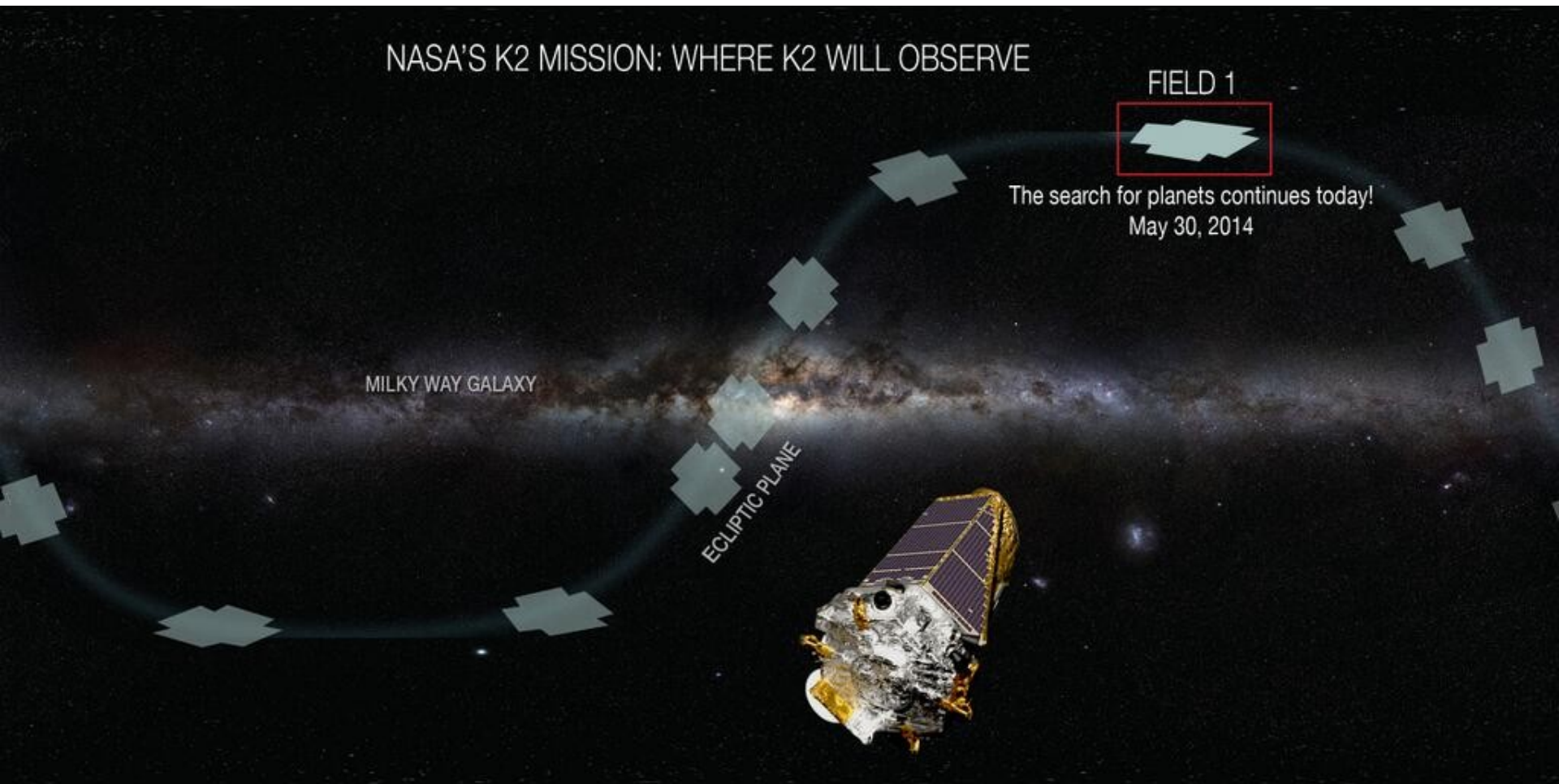
# NASA'S K2 MISSION: WHERE K2 WILL OBSERVE

FIELD 1

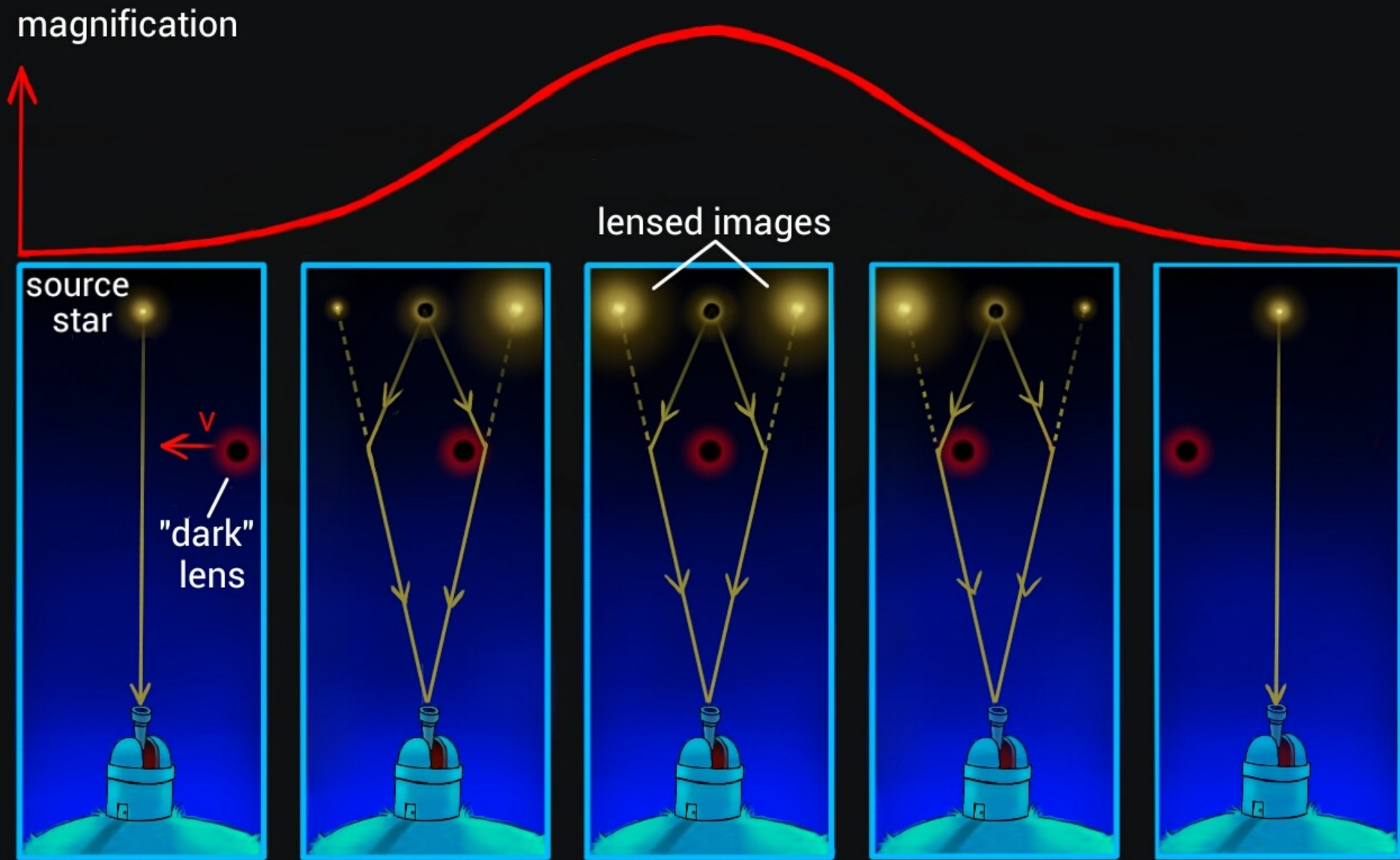
The search for planets continues today!  
May 30, 2014

MILKY WAY GALAXY

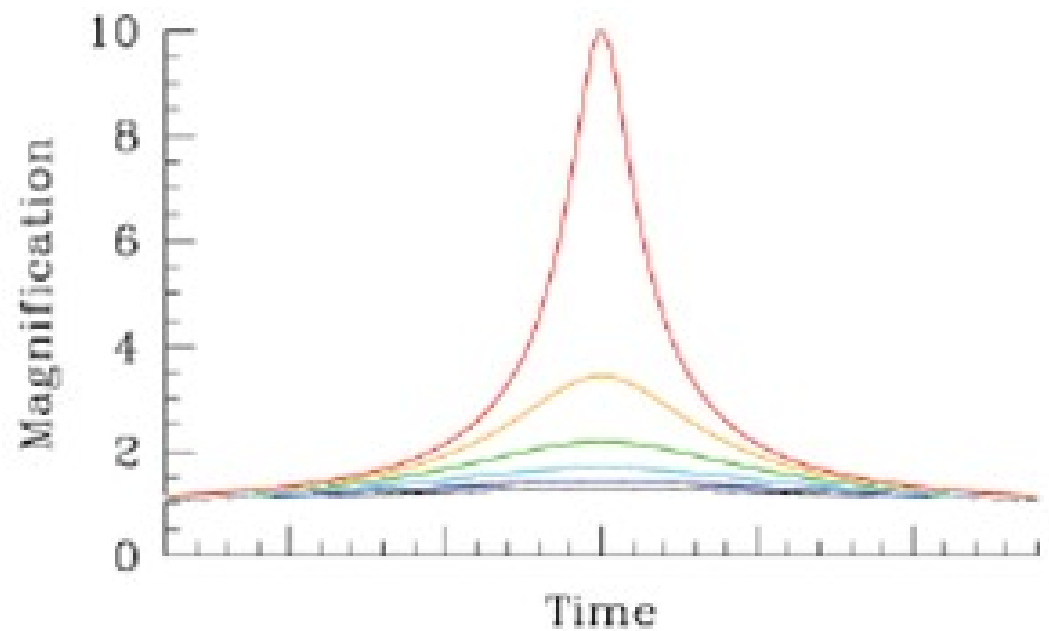
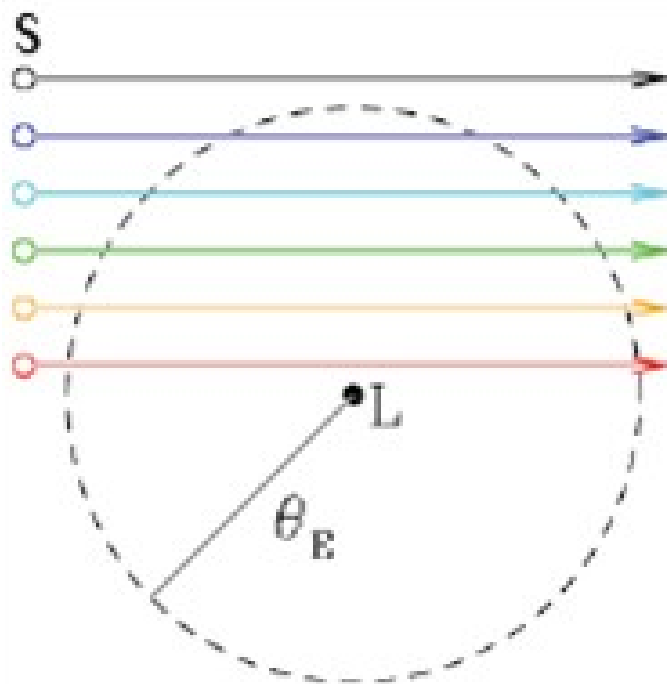
ECLIPTIC PLANE



# MICROLENSING METHOD







S ... source object

L ... lens object

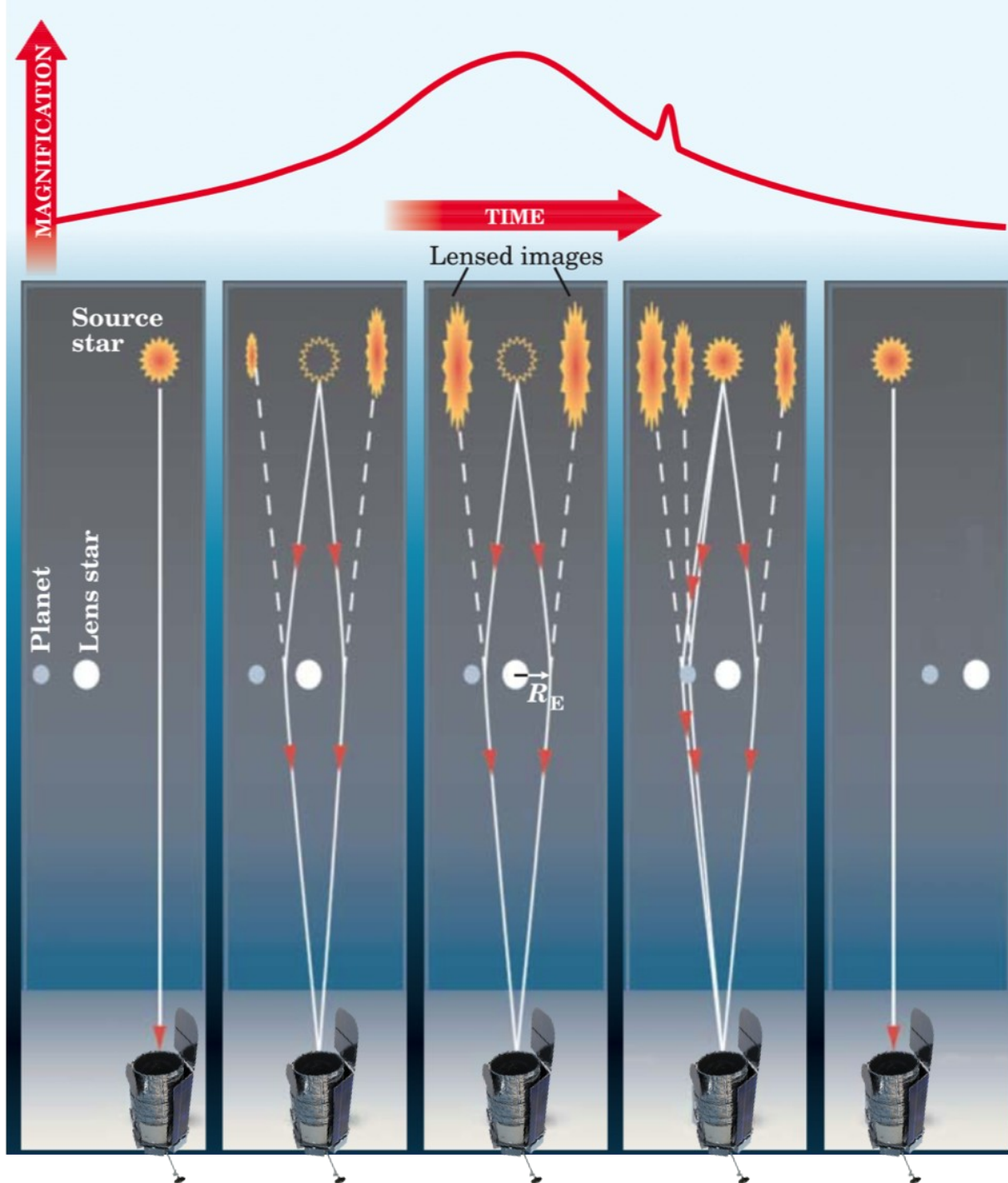
$\theta_E$  ... Einstein ring radius

if source much further away than lens ( $d_{LS} \approx d_S$ )

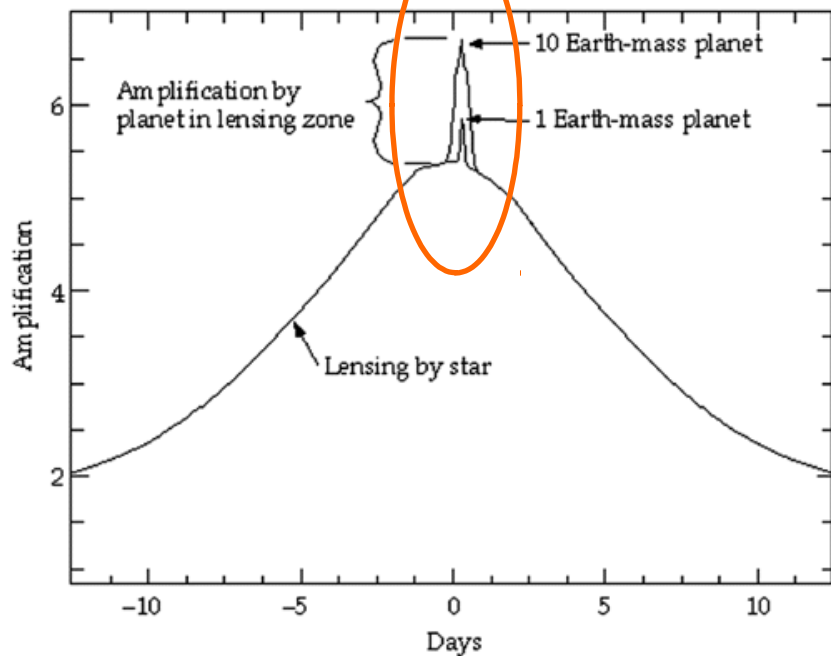
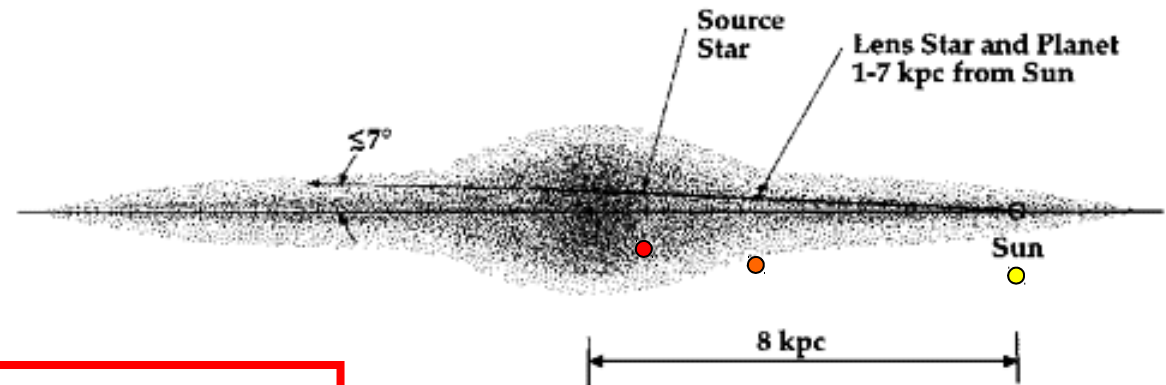
$$\theta_E \approx 0.1 \left( \frac{M \text{ in } M_\odot}{d_L \text{ in parsecs}} \right)^{1/2} \text{ arcsec}$$

$$\theta_E = \left( \frac{4GM}{c^2} \frac{d_{LS}}{d_L d_S} \right)^{1/2}$$

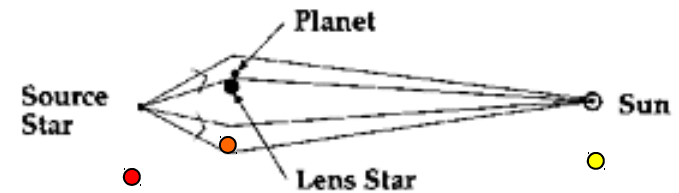
for galaxy with  $10^{15} M_\odot$  at 1 Gpc,  $\theta_E \approx 100$  arcsec,  
for star with  $1 M_\odot$  at 1 kpc,  $\theta_E \approx 3$  milliarcsec



# MICROLENSING METHOD



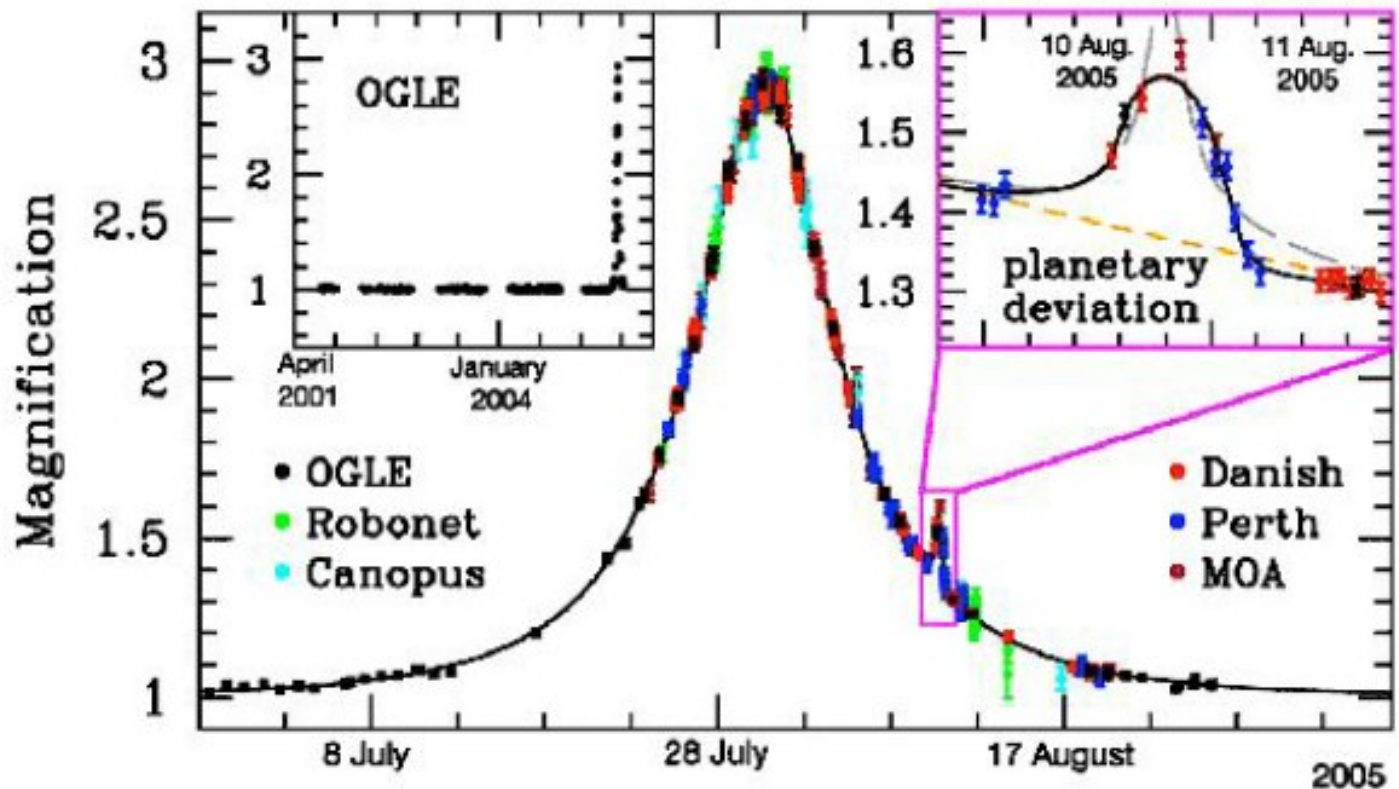
From Bennett and Rhie, 1995



**Pros:** All masses and orbits and independent of star brightness

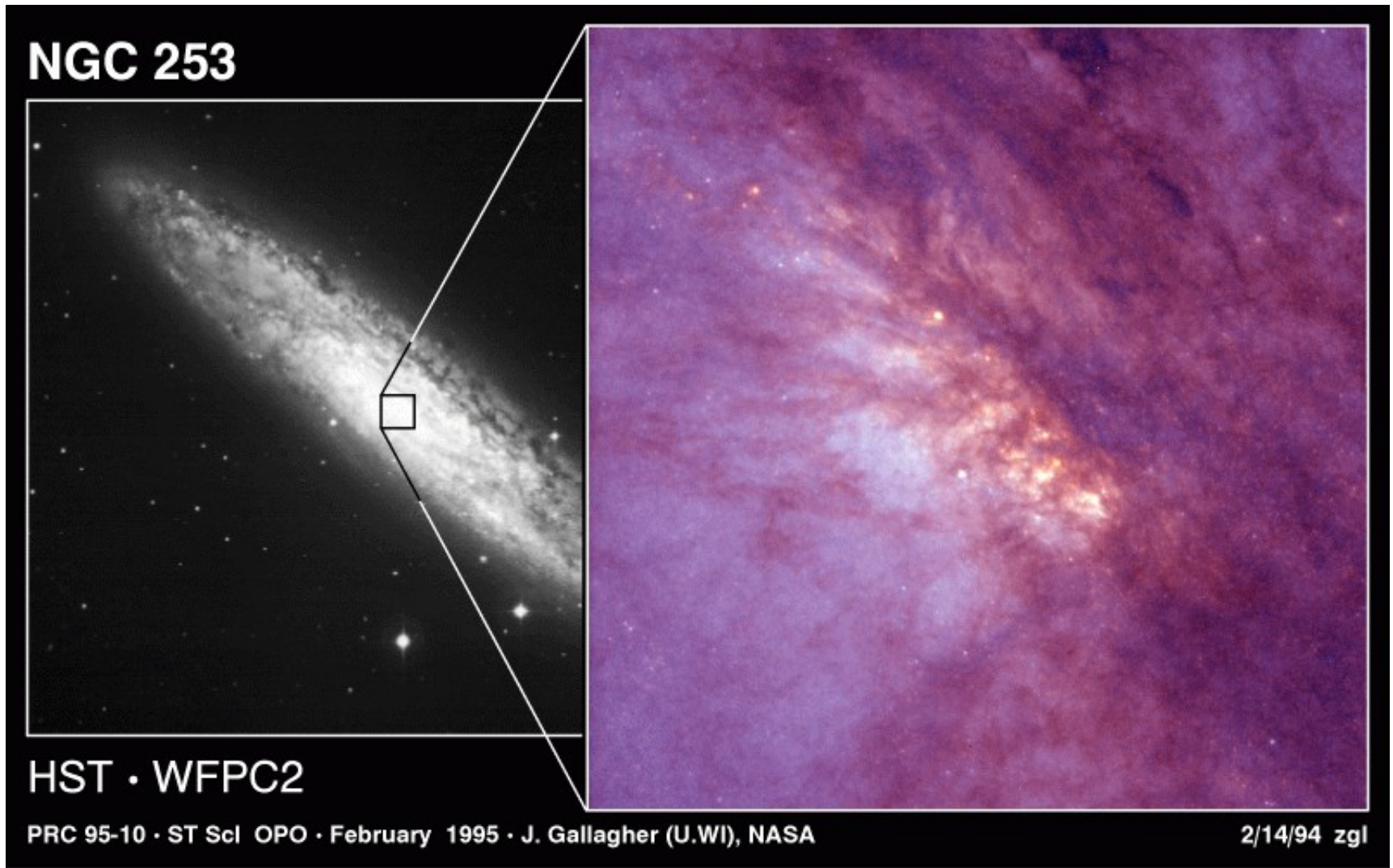
**Cons:** Distant planets and observation cannot be repeated

# Earth mass planet detected with microlensing



Light Curve of OGLE-2005-BLG-390

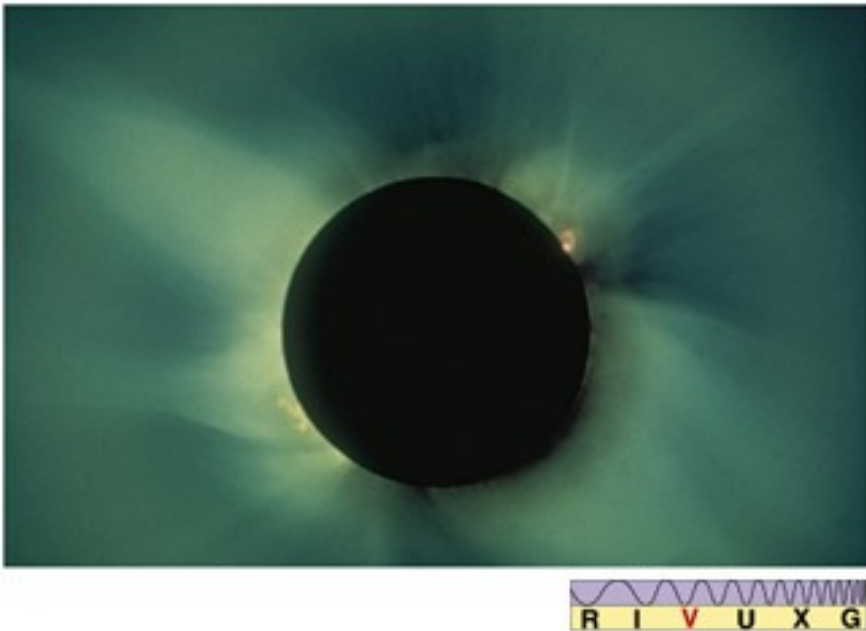
# MICROLENSING METHOD



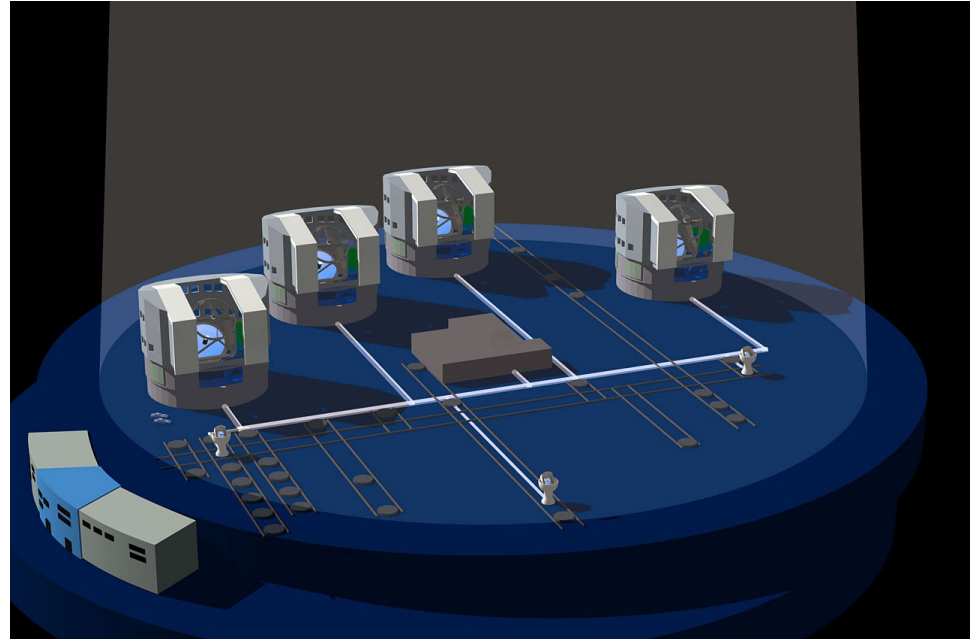
**In the future, one can do this in external galaxies!**



# IMAGING METHOD

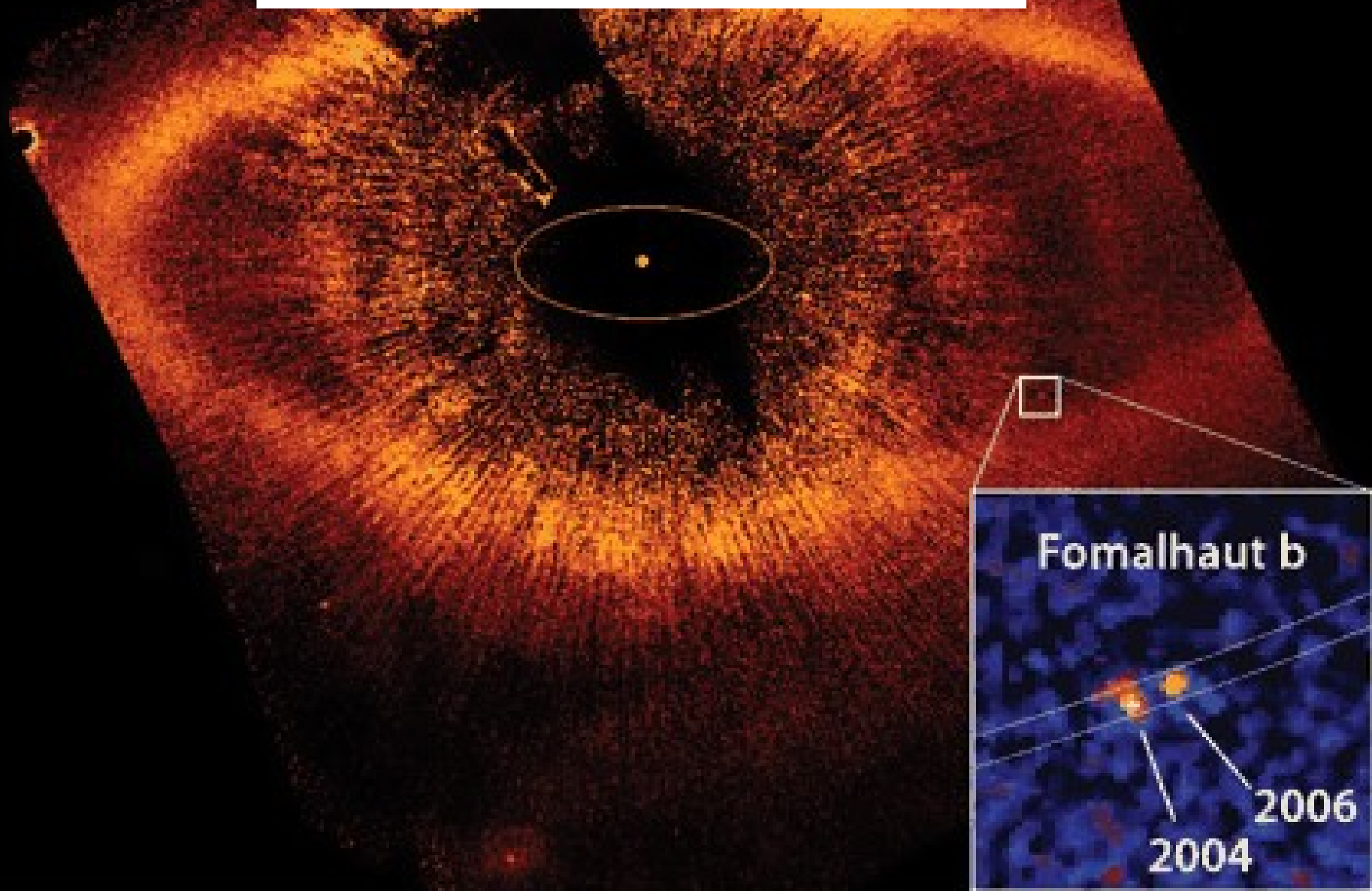


The star can be blocked out using a **coronagraph**

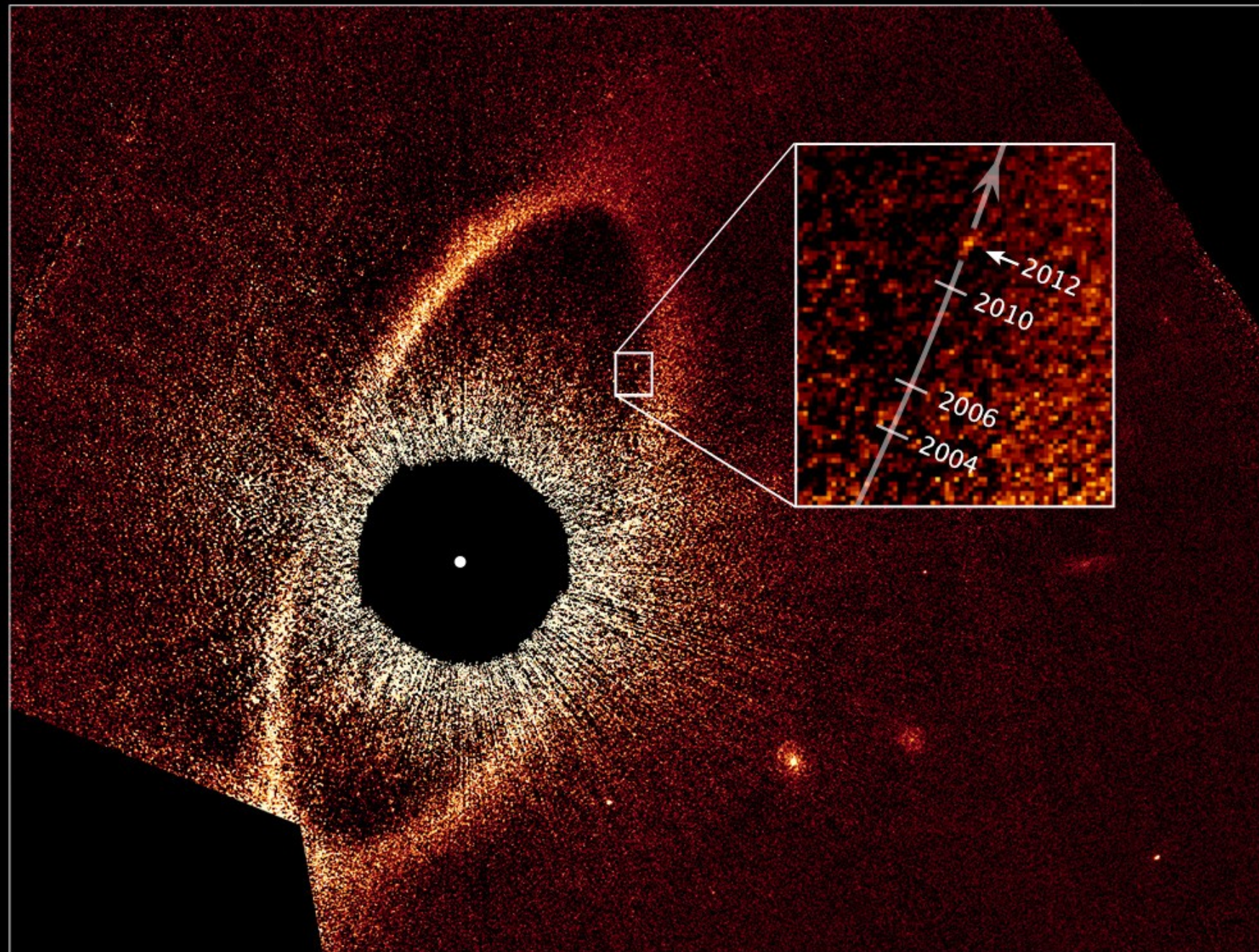


Now we can do it with **interferometers** (with excellent **spatial resolution** as a bonus!)

# Direct Imaging (HST)

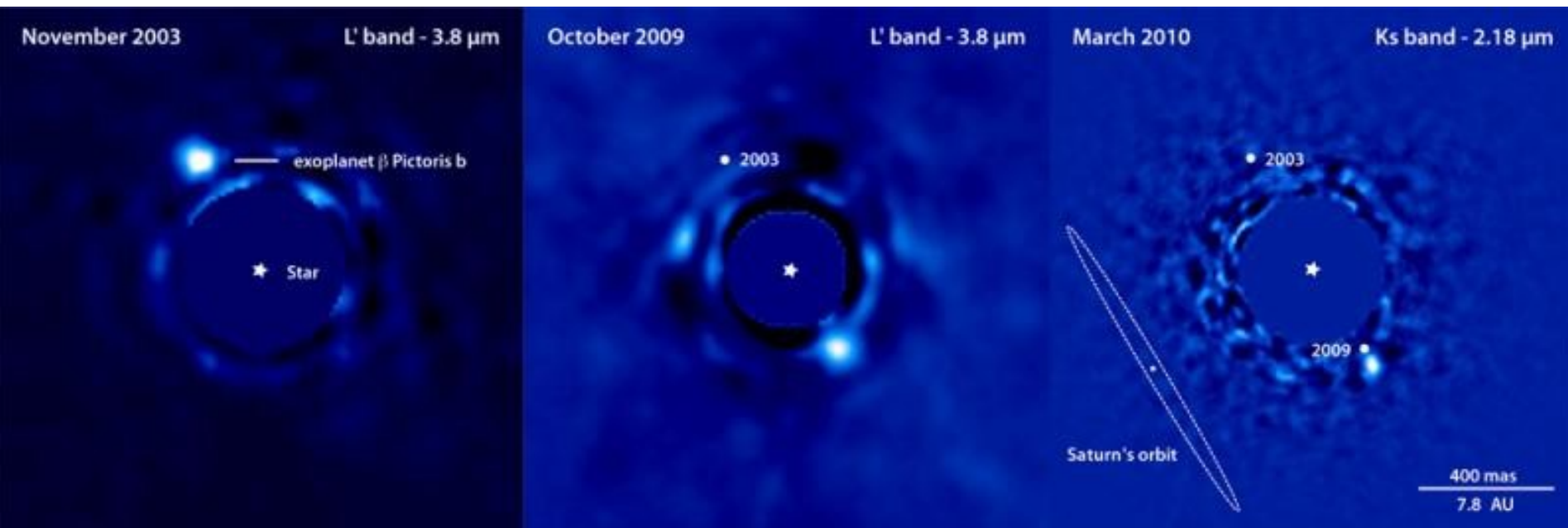








# Beta Pictoris b imaged with VLT, NaCo (infrared)



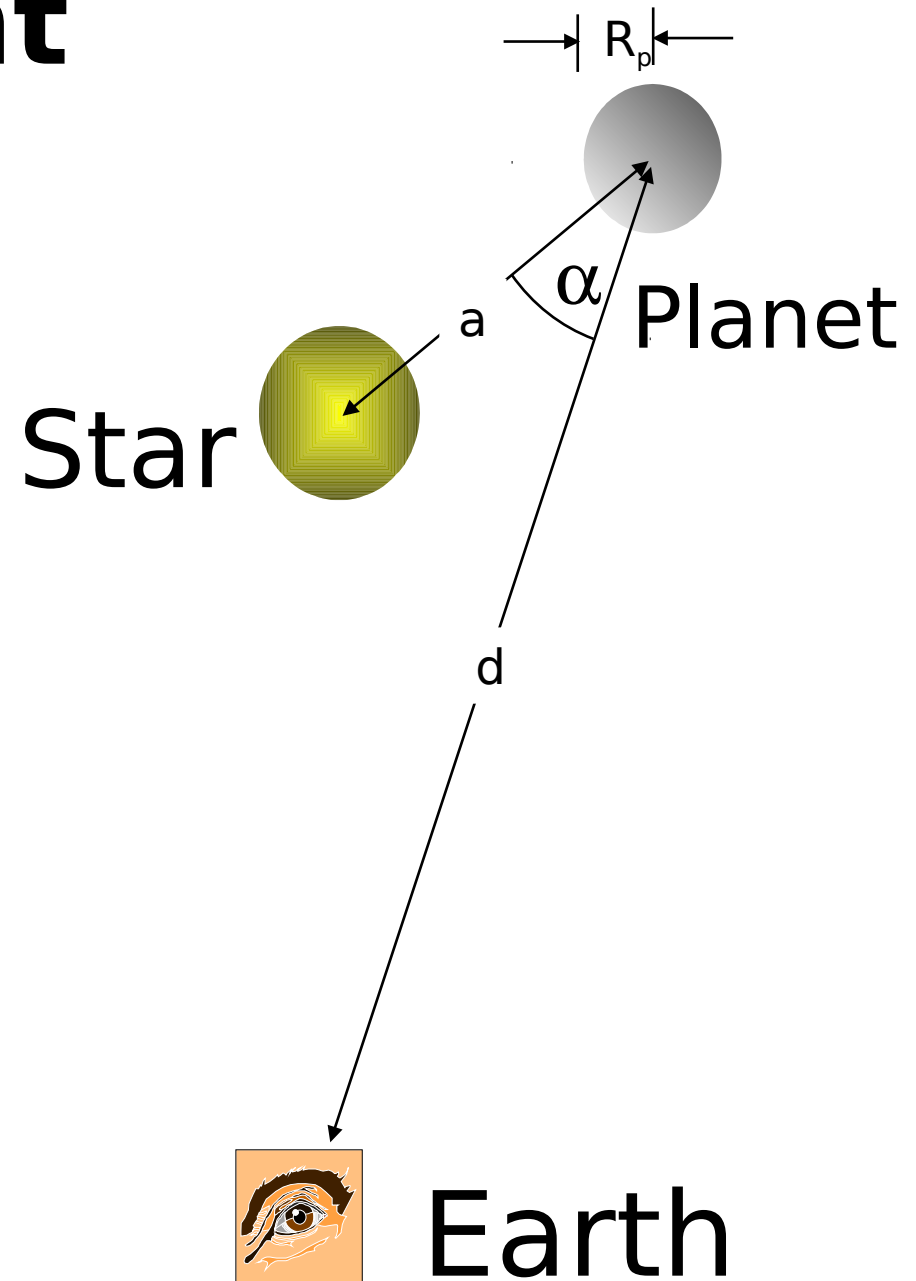
$M \approx 10$  Jupiter masses;  $T \approx 1500^\circ \text{C}$

# Reflected Light

planet/star flux ratio is:

$$\epsilon \equiv \frac{f_{\text{planet}}}{f_*} = p \frac{R_p^2}{a^2}$$

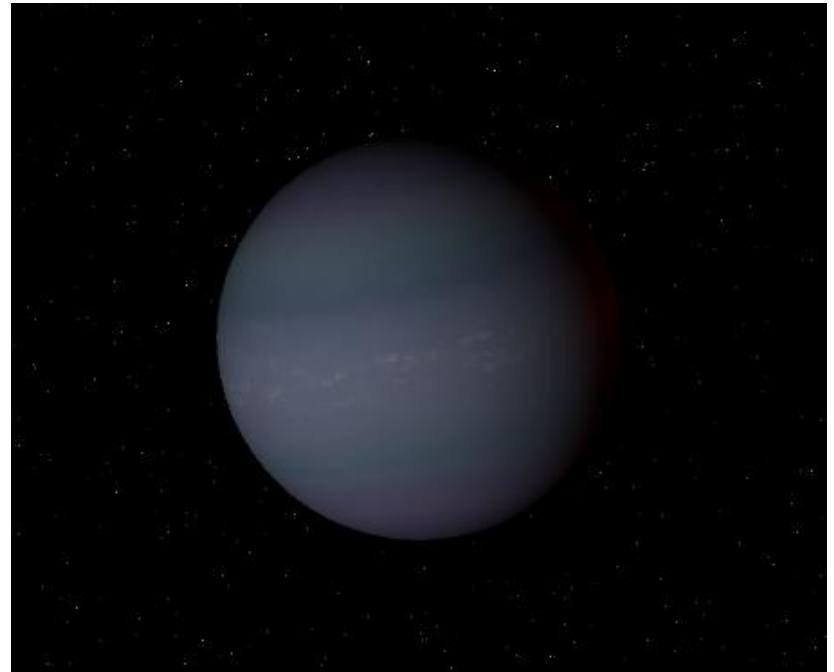
$p$  is albedo



# Atmospheric Probe

- Sudarsky Planet types
  - I : Ammonia Clouds
  - II : Water Clouds
  - III : Clear
  - IV : Alkali Metal
  - V : Silicate Clouds
- Predicted Albedos:
  - IV : 0.03
  - V : 0.50

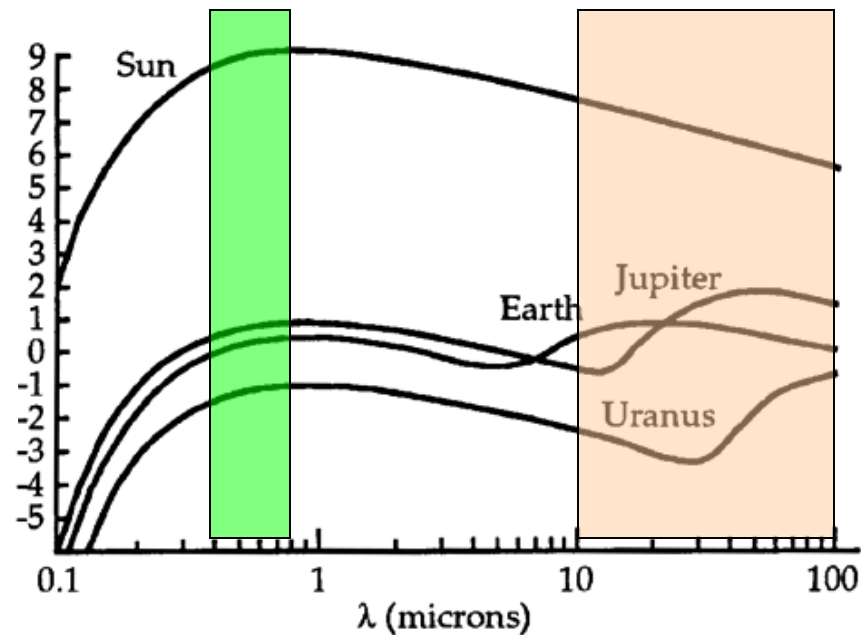
Sudarsky et al. 2000



Picture of class IV planet generated using Celestia Software

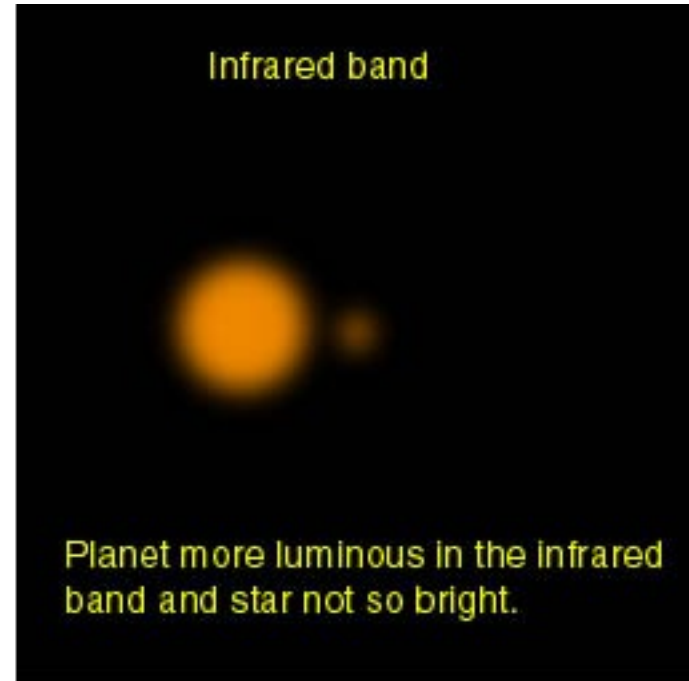
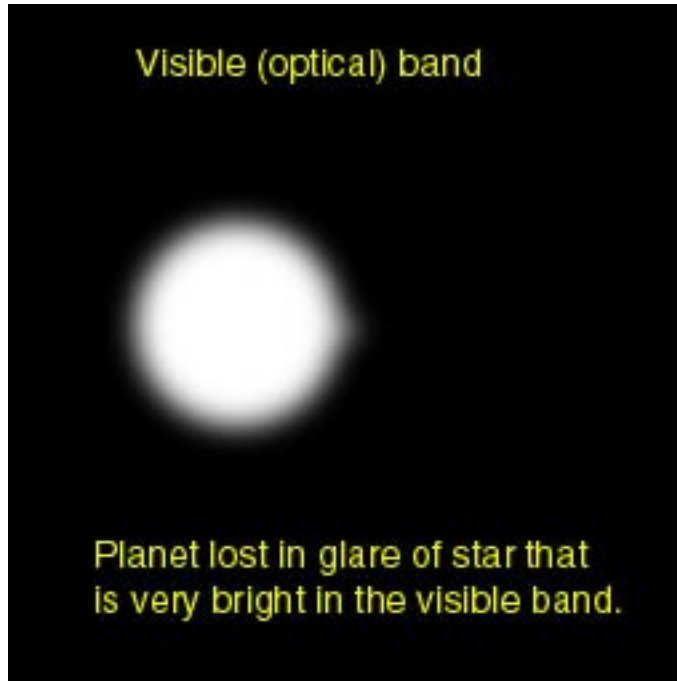
# IMAGING METHOD

Optical: star/planet = 1 billion =  $10^9$     Infrared: star/planet = 1 million =  $10^6$



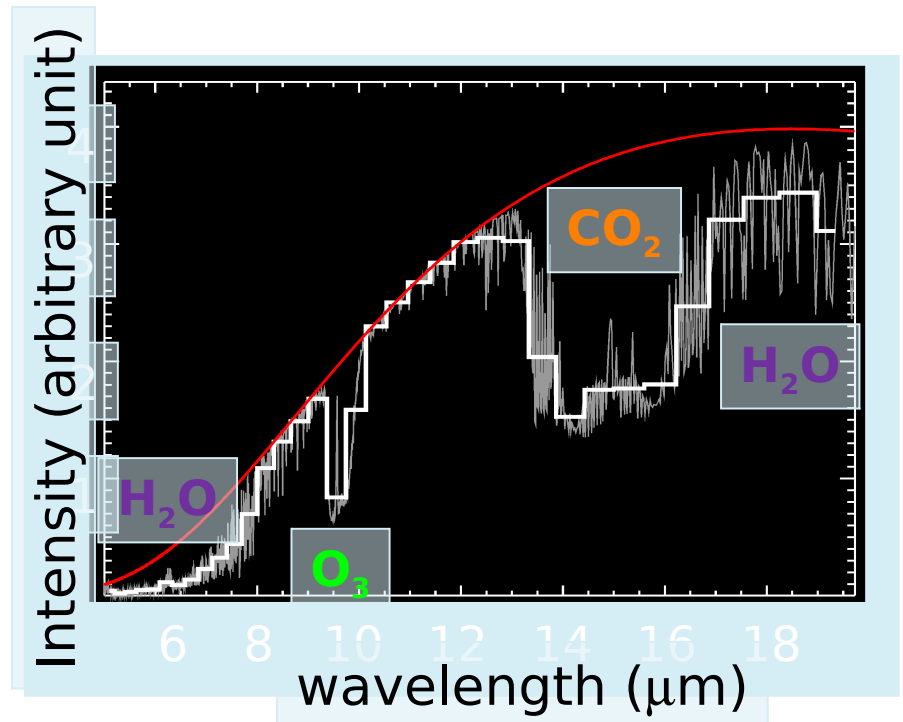
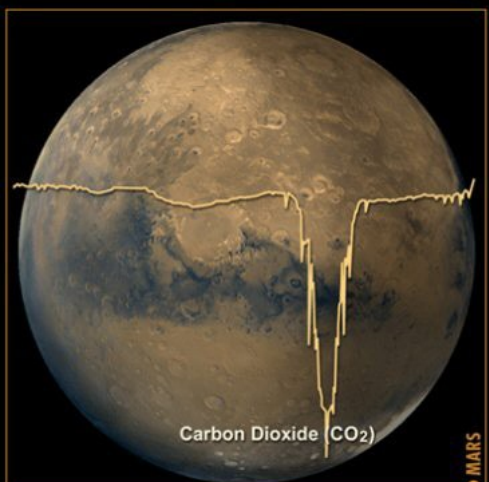
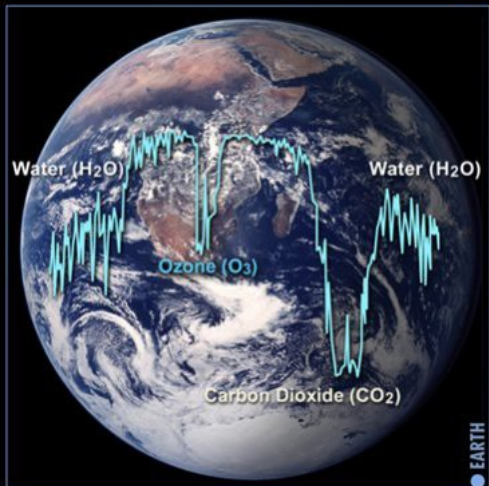
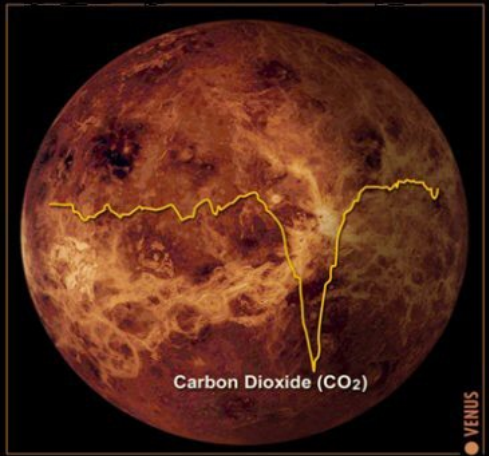
We need to search in the infrared and to lock out the star!

# IMAGING METHOD

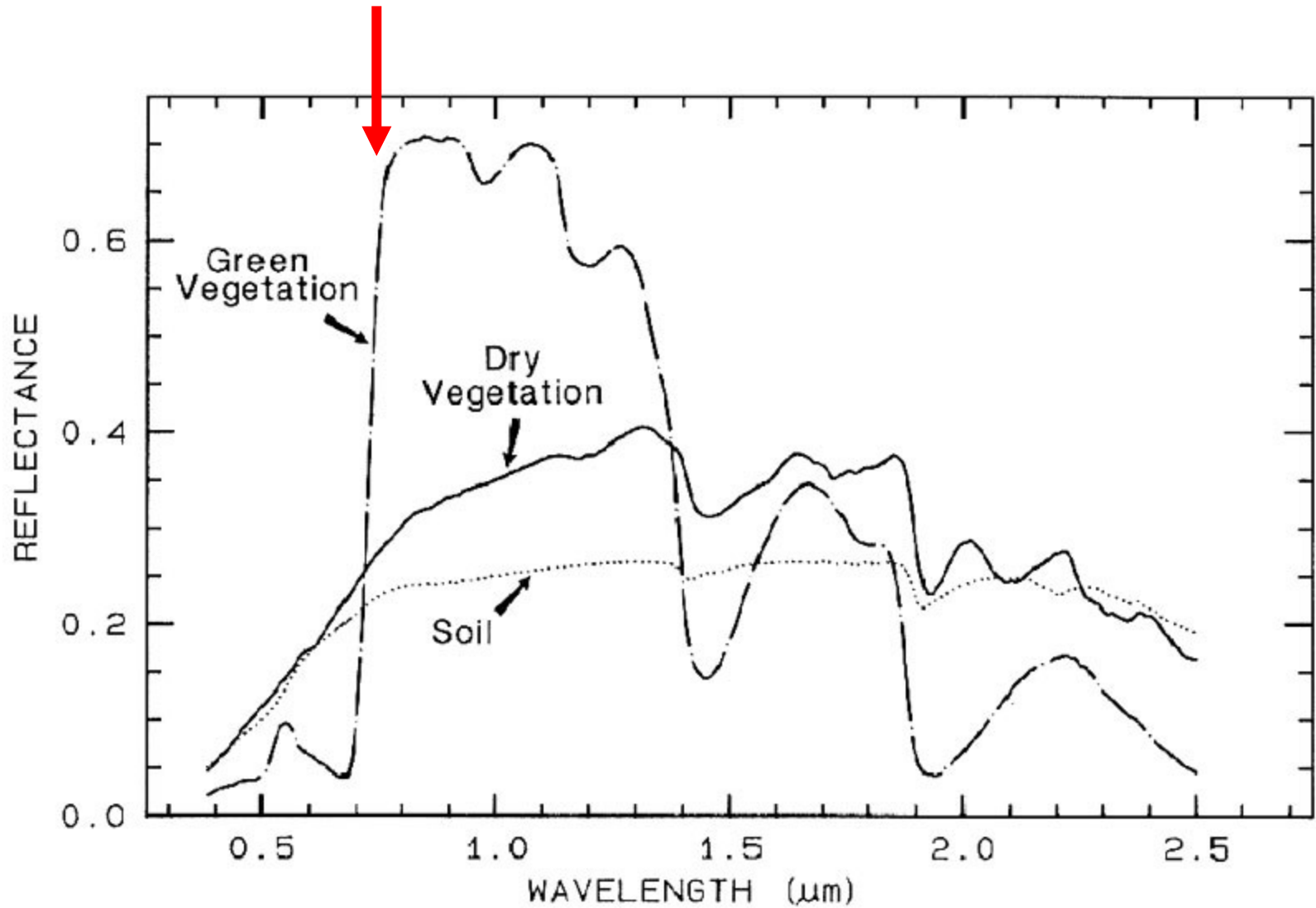


# Exoplanets Spectroscopy

## To look for key molecules



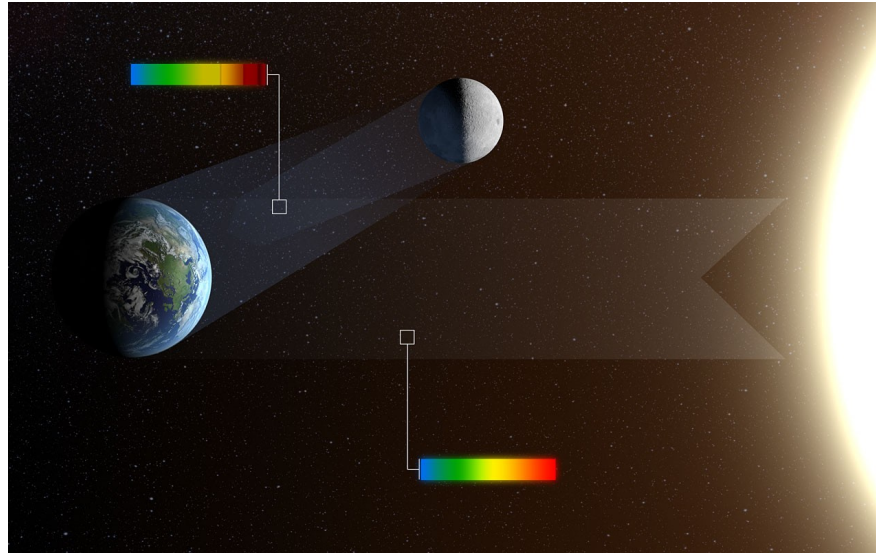




The “red edge” is a signature of vegetation on Earth.

# The first astronomical detection of life

*(Sterzik, Bagnulo & Palle, 2012, Nature 483, 64)*



- Moon observations from VLT (Chile) have studied Earth light (coming from the Sun) reflected from the Moon.
- Biosignatures in spectra ( $O_2$  and  $CH_4$  abundances outside equilibrium and vegetation bump) and polarization